Observation impact diagnostics in an Ensemble **Data Assimilation System**

1. Introduction: Forecast impact diagnostics developed so far

Motivation

Assessing the impact of observations in data assimilation systems is generally extremely expensive

- denial experiments
- observation system experiments (OSE)

Aim: Find diagnostic tools to

- indicate impact of observation subsets on analysis/forecast
- identify where observation impact is sub-optimal/negative

$J \stackrel{\text{defl}}{=} \frac{1}{2} \left(\left\| \mathbf{e}^{t|a} \right\|^2 - \left\| \mathbf{e}^{t|b} \right\|^2 \right)$ $u^{v;t}$: data used for verification (at time t) $m{y}^{t|a}, \ m{y}^{t|b}$: modelequivalent to $m{y}^{v,t}$ based on forecast from analysis $m{x}^{\mathrm{a}} ightarrow m{y}^{t|\mathrm{a}}$ background $m{x}^{\mathrm{b}} ightarrow m{y}^{t|\mathrm{b}}$

 $\|e^{t|a}\| = (e^{t|a})^T C(e^{t|a})$ "scalar product with metric C"

Cost-function

- gives impact of obs assimilated at time t = 0 can be written as **sum over the individual** observations y_i^o
 - $J = \sum_{i} \frac{1}{2} \left\langle \left(e^{i|a} + e^{i|b} \right)^{T} C H_{v} M_{0 \rightarrow t} K_{l} \left(y_{l}^{o} y_{l}^{b} \right) \right\rangle$
 - : time evolution operator : operator computing modelequivalent to $\boldsymbol{y}^{\mathbf{v}:t}$

Time evolution $M_{0 \rightarrow t}$:

Different DA systems use different approaches for computing the time evolution

4D Var (Langland and Barker 2004) → use linear (adjoint) model

Ensemble Kalman Filter (EKF)

Here: Ensemble Kalman Filter Verification with observations

2. Optimality condition

Consider the cost function J for different initial

$$\begin{aligned} \boldsymbol{y}^{ljmit}(\{\lambda_l\}) &= \boldsymbol{y}^l\left[\boldsymbol{x}^{init}(\{\lambda_l\})\right] \\ \boldsymbol{x}^{init}(\{\lambda_l\}) &= \boldsymbol{x}^{b} + \sum_{l \in \{obs\}} \mathbf{K}_l \lambda_l\left(\boldsymbol{y}_l^o - \boldsymbol{y}_l^b\right) \\ \boldsymbol{x}^a &= \boldsymbol{x}^{init}(\{\lambda_l - 1\}) \end{aligned}$$

If J has a minimum for $x^{\text{init}} = x^{\text{i}}$

$$\langle J_i^{(o)} \rangle \equiv \langle (e^{i\phi})^T CH_v M_{0 \rightarrow i} K_l (y_i^o - y_i^b) \rangle$$

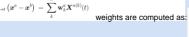
= 0 for all $l \in \{obs\}$

3. Our System

- LETKF (Hunt et al. 2007) 40 ensemble members
- verification vs obs. (Sommer and Weissmann 2014)
- time evolution via analysis ensemble (Kalnay et al. 2012) 2 2 2 2 2 observation operator for y_{v}^{o}



 $\mathbf{X}^{a(k)}$: k^{th} incr. analysis



4. Results - What is shown?

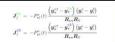
So far only results for t=0 ("impact on analysis").

 $\sum \left(-J_l^{0|a}\right) = \sum P_{vl}^a \frac{\left(y_v^o - y_v^i\right)\left(y_l^o - y_l^b\right)}{R_{ll}R_{vv}}$

 $\sum \left(-J_{l}^{0|b}\right) = \sum P_{vl}^{a} \frac{\left(\mathbf{y}_{v}^{o} - \mathbf{y}_{v}^{b}\right)\left(\mathbf{y}_{l}^{o} - \mathbf{y}_{l}^{b}\right)}{R_{ll}R_{vv}}$

- impact variable :





Statistics have been computed for different cost-function components separately:

← should be small

 $\sum \left(-J^{0|a}\right)$

- "normalised" : $\sum \left(-J^{0|a|}\right) / \left(\sum \frac{|P_{vl}^a|}{\sqrt{R_{vv}R_{D}}}\right)$

- effective number : $(\sum |P_{vl}^a|)^2 / \sum |P_{vl}^a|$

← should be positive (and large) --- "potential benefit"

 $\sum \left(-J^{0|b}\right) / \left(\sum \frac{|P_{vl}^a|}{\sqrt{R_{vv}R_B}}\right)$

$$H_v$$
: observation operator for y_v^o
 $C = R_{vv}^{-1} = \frac{1}{r_v}$

$$egin{aligned} \mathbf{w}_k^a &= \sum_{lpha,eta\in\{obs\}} Y_lpha^{a[k]} R_{lpha\beta}^{-1} \left(\mathbf{y}_eta^o - \mathbf{y}_eta^b
ight) \ Y_lpha^{a[k]} &= H_lpha X^{a[k]} &: X^{a[k]} ext{ in obs space} \end{aligned}$$

$$P_{\mathbf{v}^{l}}^{a}(t) = \sum_{i=1}^{n_{ms}} \left(\mathbf{Y}_{\mathbf{v}}^{a(k)}(t)\mathbf{Y}_{l}^{a(k)}\right) \rho_{loc}[\mathbf{v}, l]$$

analysis covariance matrix in obs space (estimated from ensemble)

--- "optimality condition"

5. Results: Impact on analysis (t=0)

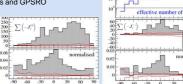
Temps verified by GPSRO

Excellent correspondence/consistency between Temps and GPSRO

 $\sum_{i} \left(-J_{i}^{(b)}\right)$: clearly positive everywhere

 $\sum \left(-J_{i}^{\scriptscriptstyle (p)}
ight)$: is 1.) much smaller than $\sum \left(-J_{i}^{\scriptscriptstyle (p)}
ight)$ →optimality condition largely fulfilled 2.) mostly positive
 → weight on TEMPS in assimilation

could be slightly increased in tropical regions

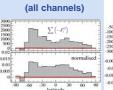


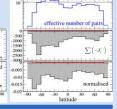
AMSU-A verified by GPSRO

 $\sum (-J_i^{(i)})$: generally positive \rightarrow strong potential

 $\sum (-J_i^*)$: clearly negative \Rightarrow obs have too strong weight AMSU-A observation errors are too small (also according to Desroziers diagnostics)

> Increased observation errors have been tested for operational implementation.
> But: Positive impact on forecast only after reduced thinning of AMSU-A





Data from individual AMSU-A channels $(\sum (-J_i^{(i)})$ - normalised)

The correspondence between AMSU-A channels and GPSRO is positive or neutral for most channels and most latitudes $(\sum (-J_i^{(a)})$ is mostly positive).

In some regions the dark shaded areas are negative or

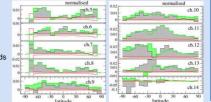
neutral but the green curve (bias removed a posteriori) is clearly positive. This indicates that **AMSU and GPSRO** have opposite bias.

In both cases (i) and (ii), GPSRO has *strong bias vs model*. Most likely the GPSRO is correct → **model bias**.

Ch. 9+10 are the lowest channels used over land. As seen (on the right below) bias problems are much stronger over land than over sea (Model biases are different over land and sea)

Significant bias problems occur for :

- (i) ch.14 (everywhere)
- (ii) chs. 9+10 (esp.towards



data over sea/land only ch.11 (la

6. Outlook:

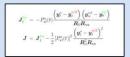
Assessing impact of individual observations

Work so far: Cost-function J gives impact of all observations assimilated at time t = 0.

Interpretation of different components (corresponding to individual observations) is suggestive but not rigorous ([$x^a - x^b$] depends on all observations used in assimilation). More rigorous approach:

Cost-function for data denial experiment. Replace: $x^b \rightarrow x^{a/l}$ (analysis not using y^o_l)





7. Discussion

The interpretation of observation impact diagnostics is often not trivial. Statistical significance is a big issue (particularly for large forecast lead times). To facilitate the interpretation and to differentiate between model and DA issues the work presented here has been (so far) restricted to t=0 (impact on the analysis).

It is explained that different parts of the cost function $J = \frac{1}{2} \left(J^{t|a} + J^{t|b} \right)$ should be considered (interpreted)

Examples are given for how the diagnostics could be linked to the following observational problems:

- The use of too small observation errors in the DA system for AMSU-a Biases of AMSU-A channels ← → Bias of GPSRO

Bias problems only show up if the bias is opposite to the bias which the verifying obs (here GPSRO) have with respect to the model.

The diagnostics reveal inconsistencies. The separation into contributions from different observations is, however, not rigorous. Particularly for strongly overlapping observations the interpretation in terms of impact (on analysis or forecast) is problematic. A method is under development to show the "denial impact" for individual observations (e.g., a single AMSU channel). See sec. 6.

- References
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