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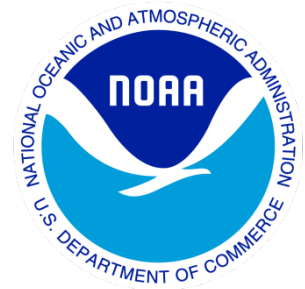
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Climate Data Record (CDR) Program

Climate Algorithm Theoretical Basis Document (C-ATBD)

Extended AVHRR Polar Pathfinder (APP-x)



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1. Introduction

1.1 Purpose

The purpose of this document is to describe the algorithms used in the generation of the Extended AVHRR Polar Pathfinder (APP-x) product suite. APP-x is a thematic climate data record (TCDR) derived from Advanced Very High Resolution Radiometer (AVHRR) satellite data. It uses the standard AVHRR Polar Pathfinder (APP) product, which was originally developed for the NASA Pathfinder Program in the early 1990s, to estimate surface, cloud, and radiative properties in both polar regions from 1982 to the present. There is a separate C-ATBD for the APP product.

1.2 Definitions

Following is a summary of the symbols used to define the algorithm.

Spectral and directional parameters:

$$\mu = \text{cosine of the solar zenith angle (degree)} \quad (1.1)$$

$$S_0 = \text{Solar constant (1362 Wm}^{-2}\text{)} \quad (1.2)$$

$$I_0 = \text{The solar radiation flux passing through the ice interior (Wm}^{-2}\text{)} \quad (1.3)$$

$$i_0 = \text{The ice slab transmittance (0~1, unit less)} \quad (1.4)$$

$$F_r^{clr} = \text{Clear-sky downward solar radiation flux at the surface (Wm}^{-2}\text{)} \quad (1.5)$$

$$F_r^{cld} = \text{Cloudy-sky downward solar radiation flux at the surface (Wm}^{-2}\text{)} \quad (1.6)$$

$$F_r \text{ and } F_r^{all} = \text{All-sky downward solar radiation flux at the surface (Wm}^{-2}\text{)} \quad (1.7)$$

$$F_l^{up} = \text{Upward longwave radiation flux from the surface (Wm}^{-2}\text{)} \quad (1.8)$$

$$F_{l,clr}^{dn} = \text{Clear-sky downward longwave radiation flux at the surface (Wm}^{-2}\text{)} \quad (1.9)$$

$$F_l^{dn} = \text{All-sky downward longwave radiation flux at the surface (Wm}^{-2}\text{)} \quad (1.10)$$

Atmospheric parameters:

$$T_a = \text{Near-surface air temperature at 2 m above the surface (K)} \quad (1.11)$$

$$C = \text{Fractional cloud cover (0~1, unit less)} \quad (1.12)$$

$$\tau = \text{Cloud optical depth (unitless)} \quad (1.13)$$

$$\epsilon_0 \text{ and } \epsilon^* = \text{The effective sky emissivity (0~1, unit less)} \quad (1.14)$$

ϵ_c = Cloud emissivity (0~1, unit less) (1.15)

w = Air mixing ratio (kg/kg) (1.16)

q = Air specific humidity (0~1) (1.17)

w_a = Air mixing ratio at 2 m (kg/kg) (1.18)

w_{sa} = Air mixing ratio at the surface (kg/kg) (1.19)

u = Surface wind speed (ms^{-1}) (1.20)

ρ_a = Air density (kgm^{-3}) (1.21)

P_a = Surface air pressure (hPa) (1.22)

T_v = Surface air virtual temperature (K) (1.23)

R_{gas} = Gas constant ($287.1 \text{ J kg}^{-1} \text{ K}^{-1}$) (1.24)

C_{pd} = Specific heat of dry air at constant pressure ($1004.5 \text{ J K}^{-1} \text{ kg}^{-1}$) (1.25)

C_p = Specific heat of wet air at constant pressure ($\text{J K}^{-1} \text{ kg}^{-1}$) (1.26)

f = Air relative humidity (%) (1.27)

Surface parameters:

α_s = Ice/snow surface broadband albedo (0~1, unit less) (1.28)

T_s = Ice/snow skin temperature (K) (1.29)

T_i = Ice interior temperature (K) (1.30)

T_f = Water freezing point temperature (K) (1.31)

σ = Stefan-Boltzman constant ($5.6696 \cdot 10^{-8} \text{ W m}^{-2} \text{ deg}^{-4}$) (1.32)

h_i = Ice thickness (m) (1.33)

h_s = Snow depth on ice (m) (1.34)

S_w = Sea water salinity (ppt) (1.35)

S_i = Sea ice salinity (ppt) (1.36)

K_s = Snow conductivity ($\text{Wm}^{-1}\text{K}^{-1}$) (1.37)

$$K_i = \text{Ice conductivity (Wm}^{-1}\text{K}^{-1}) \quad (1.38)$$

$$C_{pv} = \text{Specific heat of water vapor at constant pressure (1952 J K}^{-1}\text{ kg}^{-1}) \quad (1.39)$$

$$e_a = \text{Near-surface water vapor pressure (hPa)} \quad (1.40)$$

$$e_{sa} = \text{Near-surface saturation water vapor pressure (hPa)} \quad (1.41)$$

$$C_s = \text{Bulk transfer coefficients for turbulent sensible heat flux (0~1)} \quad (1.42)$$

$$C_e = \text{Bulk transfer coefficients for latent heat flux of evaporation (0~1)} \quad (1.43)$$

$$F_c = \text{Conductive heat flux within ice slab (Wm}^{-2}) \quad (1.44)$$

1.3 Document Maintenance

Table 1 defines the versions of the APP-x CDR product release, the corresponding software package, and the C-ATBD. The Production software package is maintained at NCDC Subversion version control system.

Table 1. Versions of the APP-x CDR product release, the corresponding software package, and the C-ATBD.

Release Date	Product Version	Software Version	C-ATBD Version	Subversion Branch	Remarks
2015-09-21	V01	V01	V1.0	TBD	Initial draft

2. Observing Systems Overview

2.1 Products Generated

APP-x contains 19 geophysical variables. All of them have undergone various degrees of validation, though all are not considered CDR quality. The APP-x variables include the following and those of CDR-quality are identified with an asterisk;

- Surface temperature, all-sky, snow, ice, and land*
- Surface albedo, all-sky*
- Sea ice thickness*
- Surface type
- Cloud mask*
- Cloud particle thermodynamic phase
- Cloud optical depth
- Cloud particle effective radius
- Cloud temperature
- Cloud pressure
- Cloud type
- Downwelling shortwave radiation at the surface*
- Downwelling longwave radiation at the surface*
- Upwelling shortwave radiation at the surface*
- Upwelling longwave radiation at the surface*
- Upwelling shortwave radiation at the TOA*
- Upwelling longwave radiation at the TOA*
- Shortwave cloud radiative forcing at the surface
- Longwave cloud radiative forcing at the surface

APP-x data products are mapped to a 25 km EASE grid at two local solar times: 04:00 and 14:00 for the Arctic, and 02:00 and 14:00 for the Antarctica. Using local solar time rather than standard UTC times provides better information on diurnal differences at all locations.

2.2 Instrument Characteristics

The series of NOAA Polar Orbiting Environmental Satellites (POES) started with TIROS-N (launched in October 1978), and continued with NOAA-A (renamed NOAA-6), NOAA-C (NOAA-7), NOAA-E (NOAA-8), NOAA-F (NOAA-9), NOAA-G (NOAA-10), NOAA-H (NOAA-11), NOAA-D (NOAA-12), NOAA-I (NOAA-13), NOAA-J (NOAA-14), NOAA-K (NOAA-15), NOAA-L (NOAA-16), NOAA-M (NOAA-17), NOAA-N (NOAA-18), MetOp-A, NOAA-N' (NOAA-19), and MetOp-B (Table 2) (Kidwell et al. 1995, 2009). The continuity of the instrument payload onboard the NOAA POES series provide an uninterrupted flow of global environmental information for establishing long-term data sets for climate monitoring.

Table 2: NOAA POES series.

Satellite Number	Launch Date	Ascending Node ¹	Descending Node	Service Date ²
TIROS-N	10/13/78	1500	0300	10/19/78 – 01/30/80
NOAA-6	06/27/79	1930	0730	06/27/79 – 11/16/86
NOAA-7	06/23/81	1430	0230	08/24/81 – 02/01/85
NOAA-8	03/28/83	1930	0730	05/03/83 – 10/31/85
NOAA-9	12/12/84	1420	0220	02/25/85 – 11/07/88
NOAA-10	09/17/86	1930	0730	11/17/86 – 09/16/91
NOAA-11	09/24/88	1340	0140	11/08/88 – 06/16/04
NOAA-12	05/14/91	1930	0730	09/17/91 – 08/10/07
NOAA-14	12/30/94	1340	0140	04/10/95 – 05/23/07
NOAA-15	5/13/98	1930	0730	12/15/98 - present
NOAA-16	09/21/00	1400	0200	03/20/01 - present
NOAA-17	06/24/02	2200	1000	10/15/02 - 04/10/2013
NOAA-18	05/20/05	1400	0200	08/30/05 - present
NOAA-19	02/06/09	1400	0200	06/02/09 – present
MetOp A ³	10/19/06	2130	0930	06/20/07 – present
MetOp B ³	09/17/12	2130	0930	04/24/13 – present

¹An ascending node would imply a northbound Equatorial crossing while a descending node would imply a southbound Equatorial crossing.

²Service date is according to Kidwell et al. (1995) and POES Status at Office of Satellite Operations, NESDIS. Information from the latter is used if there is any discrepancy between these two.

³Operated by European Space Agency (ESA) and is part of EUMETSAT's Polar System (EPS).

The Advanced Very High Resolution Radiometer (AVHRR) is one of the instruments that fly on all NOAA POES satellites. The AVHRR onboard TIROS-N, NOAA-6, NOAA-8, NOAA-10 and NOAA-12 are AVHRR/1 has four spectral channels. The AVHRR onboard NOAA-7, NOAA-9, NOAA-11, and NOAA-14 are AVHRR/2 has five spectral channels. AVHRR/3 is used on NOAA-15 and beyond and has 3a and 3b channels. Channel 3a has a central wavelength at 1.61 μm and operates in the daylight part of the orbit. Channel 3b has a central wavelength at 3.74 μm and operates in the night portion of the orbit. Channels 3a and channel 3b cannot operate simultaneously. The specifications of the AVHRR channels are listed in Table 3.

The AVHRR instruments scan in the cross-track direction and have a Field Of View (FOV) of $\pm 55.37^\circ$ from nadir and an Instantaneous FOV (IFOV) of 1.1 km at nadir (1.3-1.4 milliradians

by 1.3-1.4 milliradians for all channels). The full resolution AVHRR data are stored and processed in the High Resolution Picture Transmission (HRPT) and Local Area Cover (LAC) outputs with the LAC being the recorded HRPT. The full resolution data is also processed onboard the satellite into the Global Area Coverage (GAC) data. To produce the GAC data, LAC data is subsampled and averaged. More specifically, GAC data contain only one out of three of the original AVHRR lines. The data volume and resolution are further reduced by averaging every four adjacent samples and skipping the fifth sample along the scan line. As a result, the spatial resolution of the GAC data is 1.1 km by 4.4 km with a 3.3 km gap between pixel across the scan line at nadir. Generally, the GAC data are considered to have a 4 km resolution. Details of the instruments and data can be found in Kidwell et al. (1995, 2009).

Table 3: Spectral specifications of AVHRR/1, /2, and /3.

Channel	TIROS-N	NOAA-6,8,10	NOAA-7,9,11,12,14	NOAA-15 and onward	HRPT nadir resolution (km)	GAC nadir resolution (km)
	AVHRR/1	AVHRR/1	AVHRR/2	AVHRR/3	1.1	4.0
1	0.55-0.90 μm	0.58-0.68 μm	0.58-0.68 μm	0.58-0.68 μm	1.1	4.0
2	0.725-1.10 μm	0.725-1.10 μm	0.725-1.10 μm	0.725-1.00 μm	1.1	4.0
3A				1.58-1.64 μm	1.1	4.0
3B	3.55-3.93 μm	3.55-3.93 μm	3.55-3.93 μm	3.55-3.93 μm	1.1	4.0
4	10.50-11.50 μm	10.50-11.50 μm	10.30-11.30 μm	10.30-11.30 μm	1.1	4.0
5	Ch4 repeated	Ch4 repeated	11.50-12.50 μm	11.50-12.50 μm	1.1	4.0

The AVHRR GAC data are the inputs used to generate the APP CDR. To produce a consistent data set across all the AVHRR instruments, it is important to consider any variations in the equatorial crossing time (ECT) of each satellite. These variations will impact the time series due to potential diurnal cycles of the data. There have been considerable drifts in the NOAA POES ECT as shown in Figure 1. To keep the data set consistent and the satellite equatorial crossing time as close as to the Solar Local Times (SLT) that the APP data are composited using only AVHRR instruments with 5 channels were selected. It should be noted that NOAA-16 has Channel 3A/3B switch, while NOAA-18 has only Channel 3B after August 5, 2005.

Table 4: NOAA satellites used in the APP and APP-x CDRs.

NOAA satellite	Time range	Note
NOAA-7	01/01/82 – 12/31/84	
NOAA-9	01/01/85 – 11/07/88	
NOAA-11	11/08/88 – 12/31/94	
NOAA-14	01/01/95 – 12/31/00	
NOAA-16	01/01/01 – 08/09/05	NOAA-16 has Channel 3A/3B switch.
NOAA-18	08/10/05 – present	On 08/05/05, automatic channel 3A/3B switch was disabled. Channel 3B is permanently on NOAA-18.

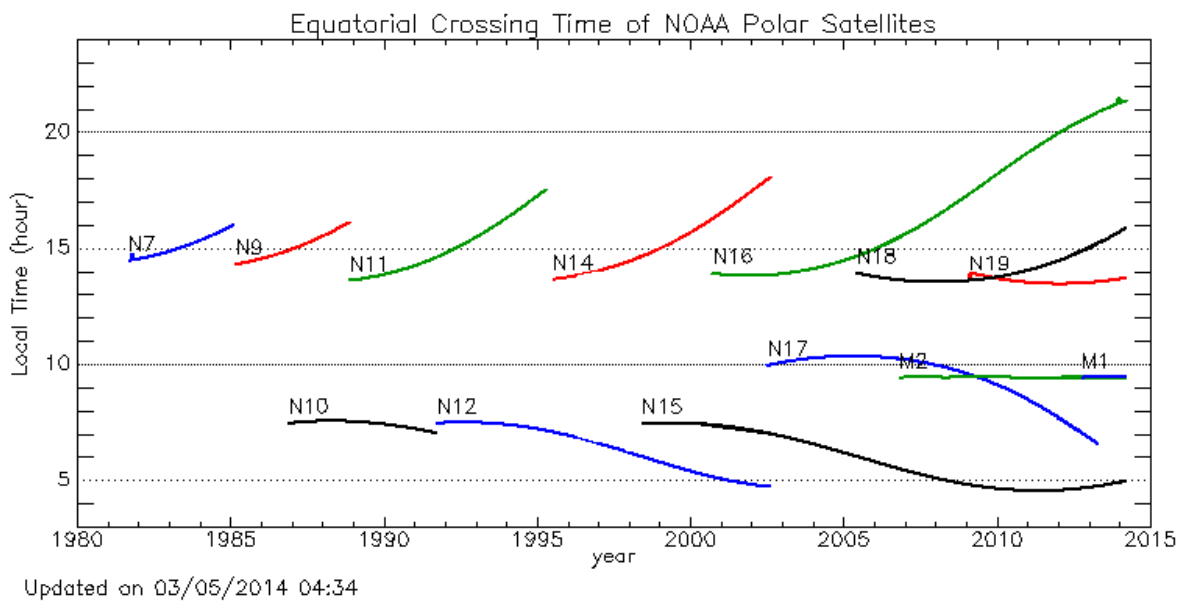


Figure 1: Equatorial crossing time of NOAA POES. (from NOAA).

3. Algorithm Description

3.1 Algorithm Overview

APP-x processing starts with input from the standard APP product (see corresponding C-ATBD) and ancillary data. Cloud detection is then performed and the cloud mask feeds into most of the other algorithms. Cloud properties, surface temperature, and surface albedo are then retrieved. Cloud and surface properties are used as input to a parameterized radiative transfer model (a neural network) to calculate radiative fluxes and cloud radiative forcing. Ice thickness is calculated from the One dimensional Thermodynamic Ice Model (OTIM) using many of the previously-calculated variables as input. All variables are then output in a single file for each of the two times per day.

3.2 Processing Outline

The APP-x code README (README_APP.txt) describes the overall process for generating the APP-x variables provided in Section 2.1. The overall processing for APP-x is shown in Figure 2.

APP-x Processing Overview

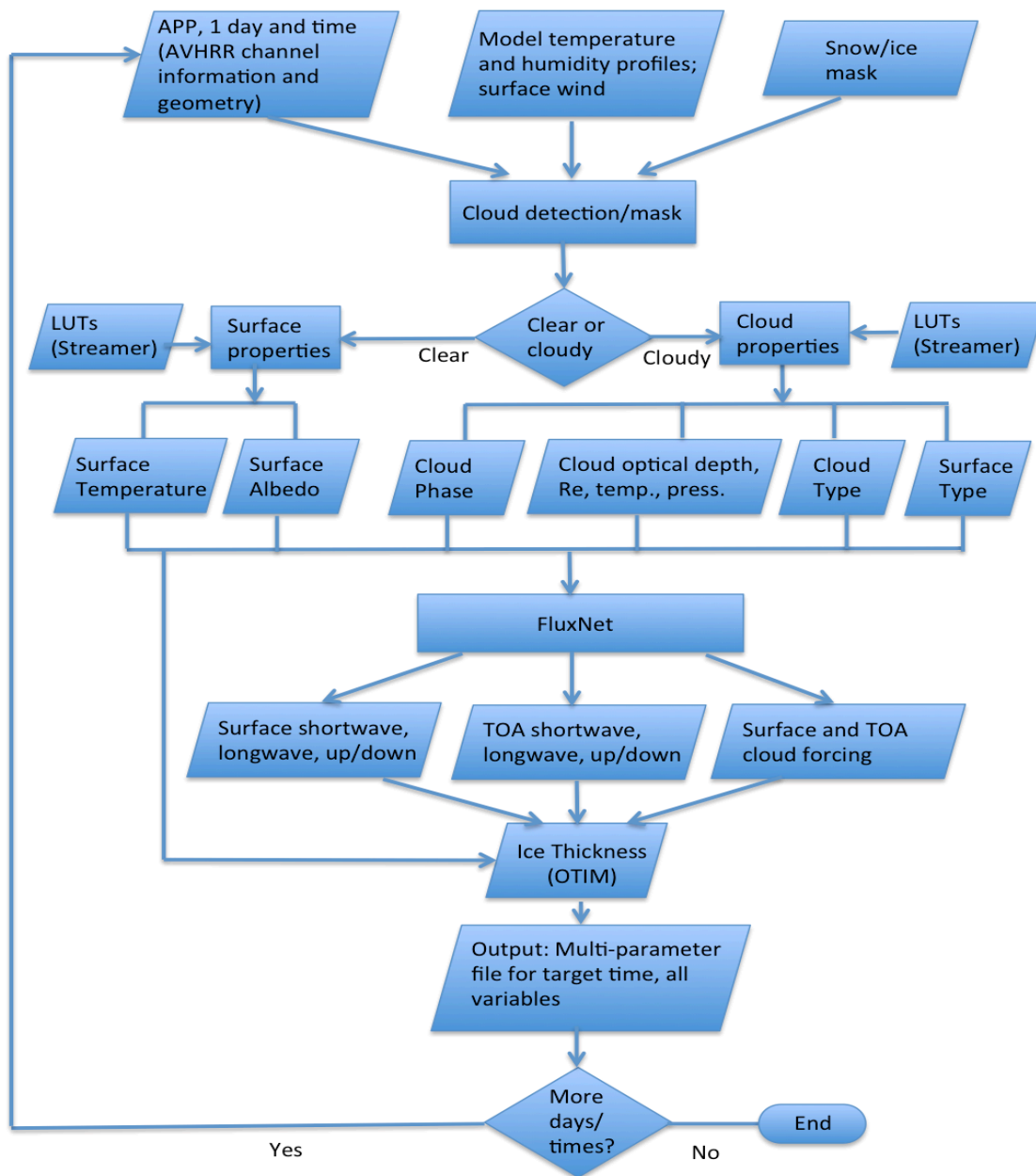


Figure 2: High-level processing flow for the production of APP-x. “LUT” is lookup tables generated with the use of the Streamer radiative transfer model; “Re” is cloud particle effective radius.

3.3 Algorithm Input

3.3.1 Primary Sensor Data

The list below contains the primary parameters data used by the APP-x:

- Channels 1-5 reflectances (channels 1, 2) and brightness temperatures (3-5)
- Sensor viewing zenith angle
- Solar zenith angle
- Relative azimuth angle
- Temperature and humidity profiles, surface winds

All of the above quantities except for the atmospheric data (temperature and humidity profiles, winds) are provided by the standard APP product, which is the primary input for APP-x processing. Atmospheric data are from a climate reanalysis product (see next section). The APP product is described in a separate C-ATBD.

3.3.2 Ancillary Data

The following ancillary data are required for APP-x.

- Surface air pressure
- Surface air Temperature
- Surface Humidity
- Surface Wind
- Atmospheric temperature profiles
- Atmospheric humidity profiles

These are supplied by the NASA Modern Era Retrospective-analysis for Research and Applications (MERRA) reanalysis products. Please see the file, README_Profile_Data and README_Surface_Data. MERRA data can be obtained from http://disc.sci.gsfc.nasa.gov/daac-bin/DataHoldings.pl?LOOKUPID_List=MAT1NXSLV

3.3.3 Data Merging Strategy

The APP-x CDR production uses the APP data products that are mapped from 5 km to a 25 km Equal-Area Scalable Earth (EASE) grid at two local solar times (LST): 04:00 and 14:00 for the Arctic, and 02:00 and 14:00 for the Antarctica. Using local solar time rather than standard UTC times provides better information on diurnal differences at all locations. The mapping from 5 to 25 km is done by taking every fifth APP pixel in the row and column directions. It is subsampling, not an averaging. The final APP-x CDR is also twice daily on the 25 km EASE grid for both poles.

In addition, the NASA Modern Era Retrospective-analysis for Research and Applications (MERRA) (Rienecker et al, 2011) data products are also used in various parts of APP-x processing. Surface air pressure, surface air temperature, surface air humidity, surface wind speed, and atmospheric temperature and humidity profiles are used. The MERRA daily data are on its native grid of the Finite-Volume dynamic core with a resolution of 2/3 degree longitude by 1/2 degree latitude and variables are provided at 20 different levels. The daily MERRA data are regrided to APP-x 25 km EASE grid for use with APP-x data to generate the sea ice thickness (SIT) CDR. Again, MERRA data can be obtained from http://disc.sci.gsfc.nasa.gov/daac-bin/DataHoldings.pl?LOOKUPID_List=MAT1NXSLV.

3.3.4 Derived Data

The characteristics of the merged data product are given in Table 5.

Table 5. Characteristics of the APP-x dataset.

Name	Twice Daily APP-x
Content	Twice daily suite of surface, cloud, ice thickness, and radiative properties on 25 km x 25 km EASE grid for the Arctic and Antarctica from 1982 to present.
File Format	NetCDF4
Specific Data	appx_s025_1982354_0200_v01r01.nc (note that “s” stands for the Antarctic, and “n” for the Arctic, “1982354” designates julian day no. 354 of the year 1982, and “0200” means local solar time of 02:00, they all will change accordingly)
Size	42.5MB per day, four files per day (two times, two poles), for approximately 500 GB for 33 years.

3.3.5 Forward Models

A radiative transfer model, “Streamer”, was used to generate reflectances and brightness temperatures in the AVHRR channels over a broad spectrum of surface, cloud, and atmospheric conditions. The simulated data are used in a number of lookup tables (LUTs) for cloud and surface property retrieval (see Figure 2). The model is not a part of the algorithms included in the CDR code package, but rather was an off-line tool. Streamer can be accessed at <http://stratus.ssec.wisc.edu/streamer/>.

A neural network implementation of a radiative transfer model is used to compute radiative fluxes and cloud forcing. The model, called “FluxNet”, is used because it is approximately 10,000 times faster than a 2-stream radiative transfer model, and is therefore ideal for processing large satellite datasets. See Key and Schweiger (1998) for a detailed description of the model.

A number of separate algorithms are used to derive the 18 output quantities, as described in Section 3. Most were part of the software package called the “Cloud and Surface Parameter Retrieval (CASPR) System for AVHRR” (Key 2002), though the original algorithms have been updated and additional products have been added, e.g., ice thickness. (CASPR is no longer publically available.) The algorithms have been described in scientific journals, as indicated in the following sections.

3.4 Algorithm Output

The following quantities are derived and output (those considered to be of CDR-quality are identified with an asterisk):

- Surface temperature, all-sky, snow, ice, and land*
- Surface albedo, all-sky*
- Sea ice thickness*
- Surface type
- Cloud mask*
- Cloud particle thermodynamic phase
- Cloud optical depth
- Cloud particle effective radius
- Cloud temperature
- Cloud pressure
- Cloud type
- Downwelling shortwave radiation at the surface*
- Downwelling longwave radiation at the surface*
- Upwelling shortwave radiation at the surface*
- Upwelling longwave radiation at the surface*
- Upwelling shortwave radiation at the TOA*
- Upwelling longwave radiation at the TOA*
- Shortwave cloud radiative forcing at the surface
- Longwave cloud radiative forcing at the surface

3.5 Theoretical Description: Surface Temperature

3.5.1 Physical and Mathematical Description

For the retrieval of clear_sky surface temperature a simple regression model is used to correct for atmospheric attenuation. For high-latitude ocean and snow-covered land we use the equation

$$T_s = a + bT_4 + c(T_4 - T_5) + d[(T_4 - T_5)(\sec\theta - 1)] \quad 3.1$$

where T_s is the surface temperature, T_4 and T_5 are the satellite measured brightness temperatures in channels 4 and 5, θ is the sensor scan angle, and a , b , c , and d are regression coefficients. To determine the empirical relationship above, radiosonde data from drifting ice and land stations in the Arctic and Antarctic were used with a radiative transfer model to simulate the sensor brightness temperatures.

The regression method of relating modeled brightness temperatures to surface temperature was also used for a snow-free land algorithm (ref). But because spectral emissivities for vegetation in channels 4 and 5 are variable and generally unknown, they are variables in the regression. Additionally, scan angle is not a variable in the regression since its dependence on angular emissivity is unknown. The regression equation for snow-free land has the form:

$$T_s = a + bT_4 + cT_5 + d\varepsilon_4 + e\varepsilon_5 \quad 3.2$$

where ε_i is the emissivity in channel i . The surface temperature retrieval methods for both sea ice/snow and snow-free land are described in detail in Key, et al. (1997).

The cloudy sky surface temperature calculation is based on empirical (linear regression) relationships between the clear sky temperature, wind speed, and solar zenith angle (daytime), determined using surface observations from the SHEBA (Surface HEat Budget of the Arctic) experiment. It applies only to sea ice. The clear sky surface temperatures are interpolated to cloudy pixels with a kriging function, and then the cloudy sky temperatures are estimated from the clear temperatures and one or two other variables, depending on the time of year. For the polar night and before the melt season (November through April) there are two equations:

solar zenith angle 80 degrees or more:

$$T_{cld} = a_1 + b_1 * T_{clr} + c_1 * u_{cld} \quad 3.3$$

solar zenith angle less than 80 degrees:

$$T_{cld} = a_2 + b_2 * T_{clr} + c_2 * \cos(Z) + d_2 * u_{cld} \quad 3.4$$

During the warm season, defined as May-September with the surface temperature greater than 255K, the following apply for solar zenith angles less than 90 degrees:

$$T_{cld} = a_3 + b_3 * T_{clr} + c_3 * \cos(Z) + d_3 * t_{cld} \quad 3.5$$

or:

$$T_{cld} = a_3 + b_3 * T_{clr} + c_3 * \cos(Z) \quad 3.6$$

During nighttime only:

$$T_{cld} = a_4 + b_4 * T_{clr} + c_4 * u_{cld} \quad 3.7$$

where T_{cld} is the cloudy sky surface temperature (K), T_{clr} is the clear sky surface temperature (K), u_{cld} is the cloudy sky wind speed (m s^{-1}), Z is the solar zenith angle, t_{cld} is the number of hours that it has been cloudy. Because t_{cld} will not generally be known to better than six hours with satellite data, the alternate equation is used.

3.5.2 Numerical Strategy

Not applicable.

3.5.3 Calculations

AVHRR reflectances, brightness temperatures, and viewing geometry are used in the application of the equations above. Surface temperature is the output.

3.5.4 Look-Up Table Description

There are no lookup tables in the surface temperature algorithm.

3.5.5 Parameterization

There are no parameterizations beyond those that are described above.

3.6 Theoretical Description: Surface Albedo

3.6.1 Physical and Mathematical Description

The retrieval of surface albedo involves four steps:

1. Convert channels 1 and 2 narrowband reflectances to a broadband reflectance.
2. Correct the top-of-atmosphere (TOA) broadband reflectance for anisotropy.
3. Convert the TOA broadband albedo to a surface broadband albedo.
4. Adjust the surface clear sky broadband albedo for the effects of cloud cover in cloudy pixels (over snow/ice only).

The general methodology described by steps 1-3 was used by Csiszar and Gutman (1999) for global land studies. Relationships for land and ocean were developed independent of that study, and methods for snow/ice and ocean were added. DeAbreu et al. (1994), Lindsay and Rothrock (1994), and earlier versions of this algorithm used a procedure where the anisotropic reflectance correction was applied to channels 1 and 2, an atmospheric correction was done on those channels, then narrowband albedos were converted to broadband. That procedure tended to overestimate the albedo of snow/ice.

Terminology for albedo varies. Here it is important to distinguish between "inherent" and "apparent" surface albedos. The inherent albedo is the "true", no-atmosphere, or "black-sky" albedo of the surface and is independent of changes in atmospheric conditions. The apparent albedo is what would be measured by up- and down-looking radiometers in the field. It varies with atmospheric conditions. Both vary with solar zenith angle and are directional in that regard. The difference between them is very small for the ocean but can be large for vegetation and snow. Figure 3 gives an example of the difference between these two albedo types for ocean, vegetation, and snow. As the figure illustrates, differences can be up to 10%. APP-x contains the directional-hemispherical apparent albedo, although it also contains code to calculate the inherent albedo. After the apparent albedo is calculated it is adjusted for cloud cover. The complete procedure is detailed in Key et al. (2001).

The first step is to convert the narrowband reflectances in AVHRR channels 1 and 2 to a TOA broadband reflectance. This is necessary because the anisotropic reflectance correction in step 2 requires a broadband reflectance. The narrow-to-broadband conversion takes the form:

$$\rho_{toa} = a + b\rho_{1, toa} \quad 3.8$$

where $\rho_{1, toa}$ is the channel 1 reflectance, $\rho_{2, toa}$ is the channel 2 reflectance, ρ_{toa} is the broadband TOA reflectance, and a , b , and c are regression coefficients. To develop the regression relationship *Streamer* (Key and Schweiger, 1998) was used to simulate the TOA reflectances over a broad range of viewing and illumination angles, atmospheric conditions (aerosol optical depth and water vapor amount), and surface types and albedos. Separate sets of coefficients were determined for snow/ice and snow-free land (generic vegetation in *Streamer*). For open ocean the broadband reflectance is set to the channel 1 reflectance.

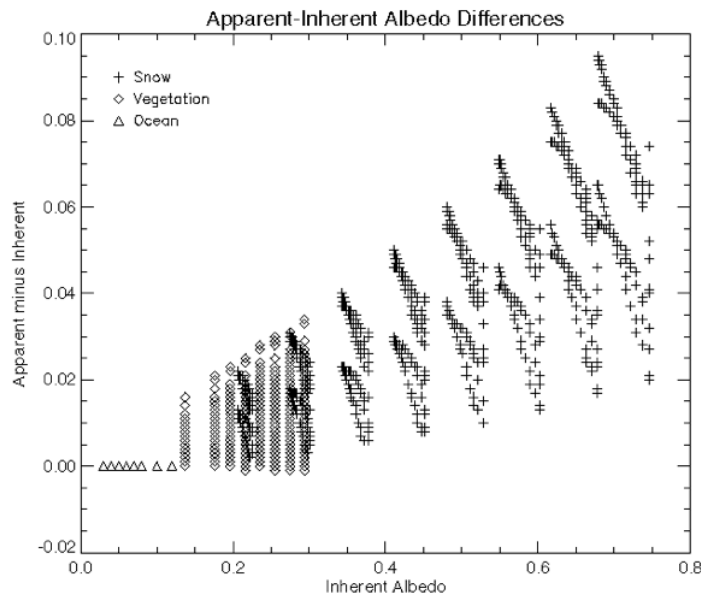


Figure 3. The difference between the apparent (atmosphere dependent) and inherent surface albedos of unfrozen ocean, snow-free land (vegetation), and snow. Data are from radiative transfer model calculations (Streamer) for two precipitable water amounts (0.5 and 5 g cm⁻²), two aerosol optical depths (0.05 and 0.5), and solar zenith angles from 0 to 87 degrees.

The next step is to correct for the dependence of the sun-satellite-surface geometry on reflectance. This is done with data presented in Suttles et al. (1988). That study used ERBE and GOES data to determine TOA anisotropic reflectance factors (ARF) for the broad shortwave band over various surfaces. It updates the earlier work of Taylor and Stowe (1984). Both the ERBE and GOES instruments measure radiances and are therefore a function of viewing and illumination geometry. To convert the directional reflectance to albedo, the ERBE/GOES ARFs are used:

$$\alpha_{toa} = \frac{\rho_{toa}}{f} \quad 3.9$$

where ρ_{toa} is the reflectance observed at the sensor (simulated by *Streamer* in step 1), f is the anisotropic reflectance factor, and α_{toa} is the TOA albedo, which is only a function of solar zenith angle. A trilinear interpolation routine was used to retrieve f as a function of satellite zenith angle, solar zenith angle, and the relative azimuth angle.

Next, the broadband, clear sky, apparent surface albedo is estimated with a regression relationship of the form

$$\alpha_{toa} = a + b\alpha_s \quad 3.10$$

where α_s is the surface reflectance, and a and b are a function of water vapor, aerosol amount, and solar zenith angle. There is a different set of coefficients for each solar zenith angle, aerosol optical depth, and precipitable water bin. This method was used by Koepke (1989) for AVHRR channels 1 and 2 separately. Here the coefficients were determined with *Streamer* for a variety of surface and atmospheric conditions and illumination angles. Viewing geometry is not important in this step. Snow/ice and vegetation surface types were used in the radiative transfer calculations, and the regression coefficients are based on the combined surface type data. For ocean surface albedo a simpler approach is used:

$$\alpha_s = a + b\alpha_{toa} + c\cos Z + dPW + e\tau_{aer} \quad 3.11$$

where PW is precipitable water (cm), τ_{aer} is aerosol visible optical depth (unitless), Z is the solar zenith angle, and a , b , c , d , and e are regression coefficient based on modeled albedos.

The surface albedo under clear and cloudy conditions can be very different. This is illustrated in Figure 4, which shows the change in surface albedo with increasing optical depth. The values are fractional change, where 1 means no difference between clear and cloudy values. While the cloudy sky albedo can be 15% more or less than the clear sky value for both surface types, it is consistently higher for snow, with a mean difference near 10%. For vegetation, the cloudy albedo may be higher or lower, so that the mean difference is very small. For this reason, only the snow albedo is adjusted for cloud cover.

The albedo of cloudy pixels is determined using the clear sky albedo, interpolated to fill in the entire image, and adjusted by the cloud optical depth and the solar zenith angle. This conversion is also based on model calculations, where *Streamer* was used to compute upwelling and downwelling fluxes for a snow/ice surface over a range of cloud and atmospheric conditions. The empirical relationship between the clear sky broadband albedo, cloud optical depth, and the cloudy sky broadband surface albedo is

$$\alpha_{s,cld} = a + b\alpha_{s,clr} + c\ln(\tau + 1) + d\cos Z \quad 3.12$$

where τ is the cloud visible optical depth (unitless), $\alpha_{s,clr}$ is the clear sky **apparent** albedo (see above), Z is the solar zenith angle, and a , b , and c are regression coefficients. As aerosol and water vapor amounts are not explicit in this relationship, this adjustment assumes that their effect on the surface albedo is small relative to that of clouds. Note, however, that this adjustment is to the apparent albedo, which is a function of aerosol and water vapor amounts. No distinction is made between water and ice clouds, although both were included in the model data for the regression analysis. This relationship

works best when the snow surface is bright ($\alpha > 0.5$) and clouds have small to moderately large optical depths ($1 < \tau < 50$). For snow-free land and open water the cloudy sky broadband albedo is set to the clear sky broadband value.

In the model calculations of steps 1, 3, and 4, the variable ranges were as follows: solar zenith angle: 0 - 87 degrees, aerosol visible optical depth: 0.05 - 0.5, precipitable water: 0.5 - 5 g m⁻³, snow visible albedo: 0.5 - 0.99, and vegetation visible albedo: 0.07 - 0.15. In all cases ozone amount was prescribed 325 Dobson units.

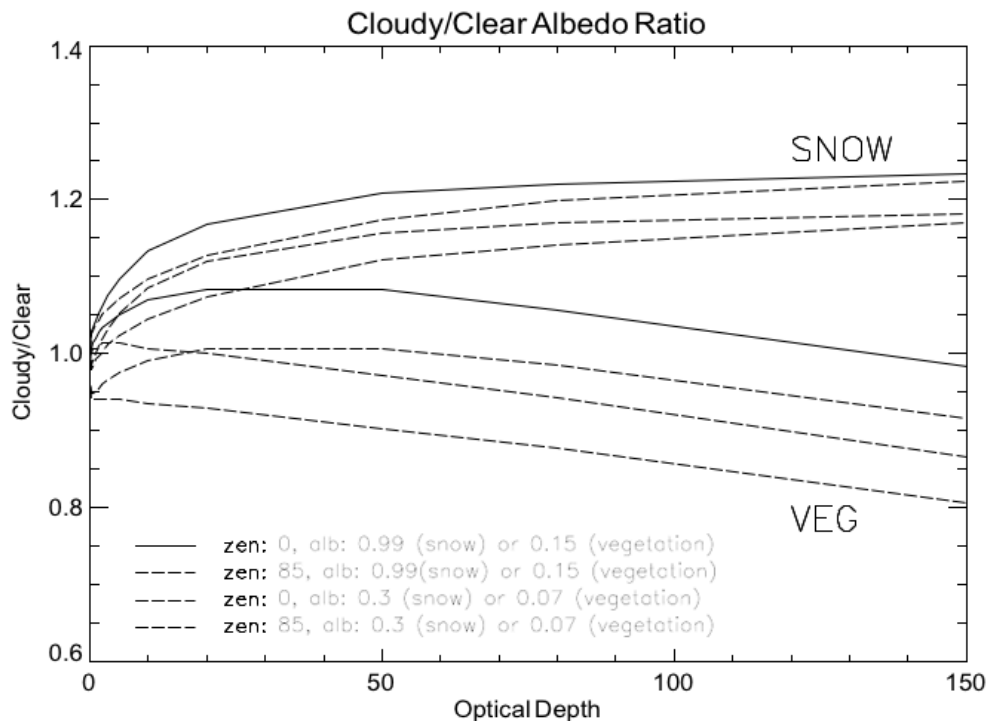


Figure 4. Differences between clear and cloudy surface albedos expressed as a fraction (cloudy divided by clear; 1 means no difference) for snow (top set of lines) and generic vegetation (bottom set), given as a function of cloud optical depth. Results were generated with a radiative transfer model for water and ice cloud under varying atmospheric conditions. The lines are for different solar zenith angles (0 and 85 degrees) and visible surface albedos (0.3 and 0.99 for snow; 0.07 and 0.15 for vegetation).

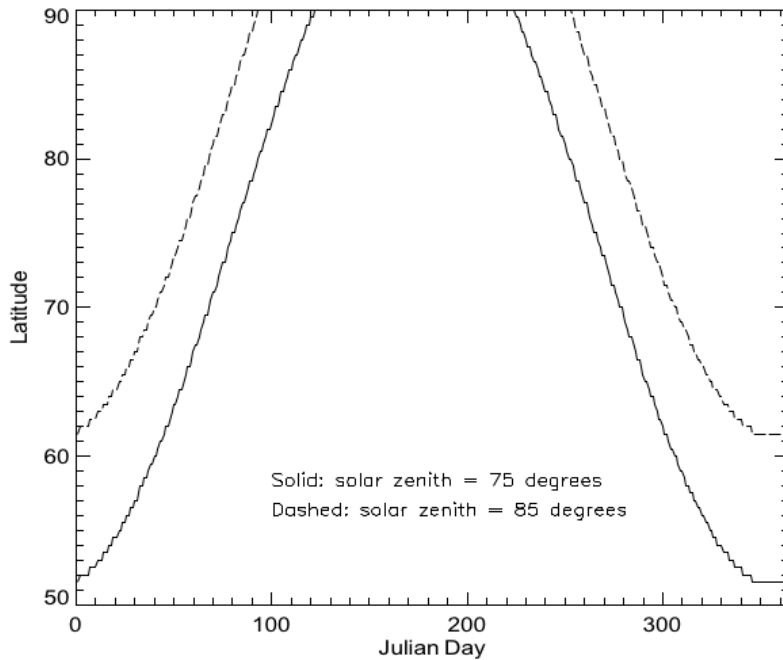


Figure 5. Latitudes and times of the year where zenith angles greater than 85 degrees and greater than 75 degrees are experienced at solar noon. All latitudes poleward of those shown will have solar zenith angles larger than 85 or 75 degrees. The 85 degree line is relevant to albedo retrievals; the 75 degree line is relevant to cloud optical depth retrievals.

3.6.2 Numerical Strategy

Not applicable.

3.6.3 Calculations

AVHRR reflectances, viewing and illumination geometry, and cloud optical depth are used in the application of the equations above. Broadband, all-sky surface albedo is the output.

3.6.4 Look-Up Table Description

There are no look-up tables in the albedo algorithm.

3.6.5 Parameterization

Anisotropic reflectance at the top of the atmosphere was parameterized by Suttles et al. (1988) and used as described above.

3.7 Theoretical Description: Sea Ice Thickness

3.7.1 Physical and Mathematical Description

The ice thickness retrieval will use the OTIM ([Wang et al, 2010](#)). The OTIM is based on the surface energy balance at thermo-equilibrium and contains all components of the surface energy budget to estimate sea and lake ice thickness up to 4 meters, though the uncertainty increases for very thick ice.

The advantage of this approach is that there is a solid physical foundation with all components of surface energy budget considered. It's capable of retrieving daytime and nighttime sea and lake ice thickness under both clear and cloudy sky conditions. It is very computationally efficient compared to more complex models such as the Climate System Model (CSM) and Community Sea Ice Model (CSIM). Its sole objective of retrieving ice thickness makes it easy to implement with the application of satellite products, flexible, fast and easy to maintain and improve later with more accurate satellite derived products including radiative fluxes, ice surface temperature, and the depth of snow on ice.

The disadvantage of this approach is that the accuracy of input parameters, e.g., snow depth, surface air humidity, temperature, and wind, can significantly impact the accuracy of ice thickness estimates. Daytime retrieval is sensitive to ice and snow optical properties associated with ice type and thickness, and is less reliable than nighttime retrievals.

The One-dimensional Thermodynamic Ice Model (OTIM) developed by [Wang et al \(2010\)](#) is applied to the APP data to generate all-sky sea and lake ice thickness products twice daily for the Arctic and the Antarctica. The current ice thickness algorithm, i.e. OTIM, has the ability to estimate sea and lake ice thickness up to 4 meters under both clear and cloudy conditions at night (no sunlight). It would also work during daytime, though the estimation is more uncertain due to the complexities of ice and snow optical properties in the solar spectrum.

Ice thickness is produced for each pixel that is identified as being ice covered. There are no direct AVHRR channel data related to the algorithm for ice thickness retrieval with the OTIM. The OTIM actually relies on some other retrieved products from APP-x as well as built-in parameterization schemes for radiation flux calculations.

The OTIM relies on the accuracy of the other products and parameterization schemes such as the cloud mask, ice surface temperature, ice surface albedo, and radiation fluxes. The performance of the ice thickness algorithm is therefore sensitive to the accuracy of the APP-

x retrieved products. We will detail the required input parameters and current validations in the following sections, and the algorithm sensitivity to input uncertainties.

Physical and statistical approaches are employed to estimate sea and lake ice thickness. In this document, the One-dimensional Thermodynamic Ice Model (OTIM) ([Wang et al, 2010](#)) based on the surface energy budget, containing all components of the surface energy budget has been developed to estimate sea and lake ice thickness. It inevitably involves parameterizations and assumptions of the sea and lake ice and associated snow characteristics, such as ice and snow conductivities, densities, and transmittances.

A slab model proposed by Maykut and Untersteiner (1971) is used here as a prototype model, the equation for energy conservation at the top surface (ice or snow) is

$$(1-\alpha_s)(1-i_0)F_r - F_l^{up} + F_l^{dn} + F_s + F_e + F_c = F_a \quad 3.13$$

where α_s is ice surface broadband albedo where ice may be covered with a layer of snow, F_r is downward solar radiation flux at the surface, i_0 is ice slab transmittance, F_l^{up} is upward longwave radiation flux from the surface, F_l^{dn} is downward longwave radiation flux from the atmosphere towards the surface, F_s is turbulent sensible heat flux at the surface, F_e is turbulent latent heat flux at the surface, F_c is conductive heat flux within the ice slab, F_a is residual heat flux that could be caused by ice melting and/or heat advection in ice. By the definitions of the terms in the equation (3.12), α_s , F_r , i_0 , F_l^{up} , F_l^{dn} should be always positive, and F_s , F_e , and F_c would be positive or negative in terms of the operational symbols used in the equation (3.12), and F_a is zero in the absence of a phase change and heat advection in ice. The details of each term will be addressed in the following subsections.

3.7.2 Numerical Strategy

The ice thickness output could have missing values if the input APP-x data and/or MERRA data have missing and/or bad values for a pixel. The missing value is also possible when the numerical solver using optimal Muller's method to solve non-linear equation is called by OTIM under certain conditions when surface albedo and/or ice transmittance have to be included and parameterized for daytime cases.

3.7.3 Calculations

The sea ice thickness (SIT) CDR production includes the following steps:

- 1) The main APP-x code is run with the input APP and MERRA data to generate twice daily APP-x data products, except ice thickness, on a 25 km EASE grid.
- 2) APP-x products surface, cloud, and radiative flux products are used as input to the OTIM main routine.
- 3) Ice thickness is generated using the OTIM code and is also generated twice per day.

3.7.4 Look-Up Table Description

Residual Heat Flux Regression Coefficients

Origin	Xuanji Wang, CIMSS/UW-Madison
Construction	11 coefficients in ASCII, for daytime retrieval. 10 coefficients in ASCII, for nighttime retrieval.
Usage	Define residual heat flux F_a estimation model.

Surface Broadband Albedo Estimation Coefficients

Origin	Thomas C. Grenfell (1979)
Construction	3 x 2 x 4 in ASCII, 4 sets of coefficients, each is 3 x 2 array.
Usage	Define surface broadband albedo model in case it's unknown.

Ice Slab Transmittance Estimation Coefficients

Origin	Thomas C. Grenfell(1979)
Construction	3 x 2 x 4 in ASCII, 4 sets of coefficients, each is 3 x 2 array.
Usage	Define ice slab transmittance model in case it's unknown.

3.7.5 Parameterization

1) Solar Radiation at the Surface

In daytime, surface broadband albedo and ice slab transmittance play important role on the incoming solar radiation for the thermo-equilibrium state at the surface. If the OTIM hybrid mode is not called or used, and the surface albedo and ice slab transmittance are unknown, then these two variables can be estimated using the methods developed by Grenfell (1979):

$$\alpha_s = 1 - A \exp(-Bh) - C \exp(-Dh) \quad 3.14$$

$$i_0 = A \exp(-Bh) + C \exp(-Dh) \quad 3.15$$

where A , B , C , and D are coefficients, respectively, and h is ice thickness or snow depth if ice is covered by snow. When the OTIM mode sets to using hybrid mode, which is recommended, those two formulas will not be used, and surface albedo and ice transmittance need not be known.

2) Upward Longwave Radiation from the Surface:

$$F_l^{up} = \varepsilon \sigma T_s^4 \quad 3.16$$

where ε is longwave emissivity of ice or snow surface, $\sigma = 5.6696 \times 10^{-8} \text{ W m}^{-2} \text{ deg}^{-4}$ is the Stefan-Boltzman constant. Here ice emissivity of 0.988 is used because snow emissivity at 0° scan angle (i.e., nadir) is 0.995, very close to the value of 0.987 for ice and 0.988 for water (Rees, 1993).

3) Downward Longwave Radiation towards the Surface:

$$F_{l,clr}^{dn} = \sigma T_a^4 (8.733 \times 10^{-3} T_a 0.788) \quad 3.17$$

$$F_l^{dn} = F_{l,clr}^{dn} (1 + 0.26 c) \quad 3.18$$

where Eq. (3.4) was developed by Ohmura (1981), and Eq. (3.5) by Jacobs (1978), and c is cloud fractional cover.

4) Downward Solar Radiation towards the Surface (Bennett, 1982):

$$F_r^{clr} = 0.72 S_0 \mu \quad 3.19$$

$$F_r^{all} = F_r^{clr} (1 - 0.52 c) \quad 3.20$$

where c is cloud fractional cover.

5) Sea Ice Salinity:

$$S_i = 2.619 + 1.472/h_i \quad \text{for } 0.10 \text{ m} \leq h_i \leq 5.0 \text{ m} \quad 3.21$$

where h_i is sea ice thickness. This is based on the work done by Jin et al (1994) and Kovacs (1996).

3.8 Theoretical Description: Cloud Detection

3.8.1 Physical and Mathematical Description

Methods of detecting clouds in satellite data range from simple thresholding procedures to complex neural networks. No attempt is made here to survey the tremendous breadth of this field; instead, a few examples from the literature are given. Ebert (1987) described one of the first polar-specific cloud retrieval algorithms, one that utilized a

variety of spectral and textural measures. Key and Barry (1989) implemented a high-latitude method similar to that used in the global algorithm of the International Satellite Cloud Climatology Project (ISCCP) (Rossow and Garder, 1993) based on spectral, spatial, and temporal variations of clouds. A number of studies have exploited the high reflectivity of liquid water clouds at 3.7 μm during the day (e.g., Allen et al, 1990; Welch et al., 1992; Sakellariou et al., 1993), while only a few have been developed specifically for nighttime retrievals (e.g., Yamanouchi et al., 1987). Most of the cloud detection algorithms are based on empirical relationships derived from a small sample of satellite data.

The cloud masking procedure presented here consists of thresholding operations that are based on modeled sensor radiances. The AVHRR radiances are simulated for a wide variety of surface and atmospheric conditions, and values that approximately divide clear from cloudy scenes are determined. Examples are given in Figures 6 and 7 where the channel 3 reflectance and the thermal channel differences, respectively, are shown as a function of cloud optical depth. Clear sky is represented as having a cloud optical depth of zero.

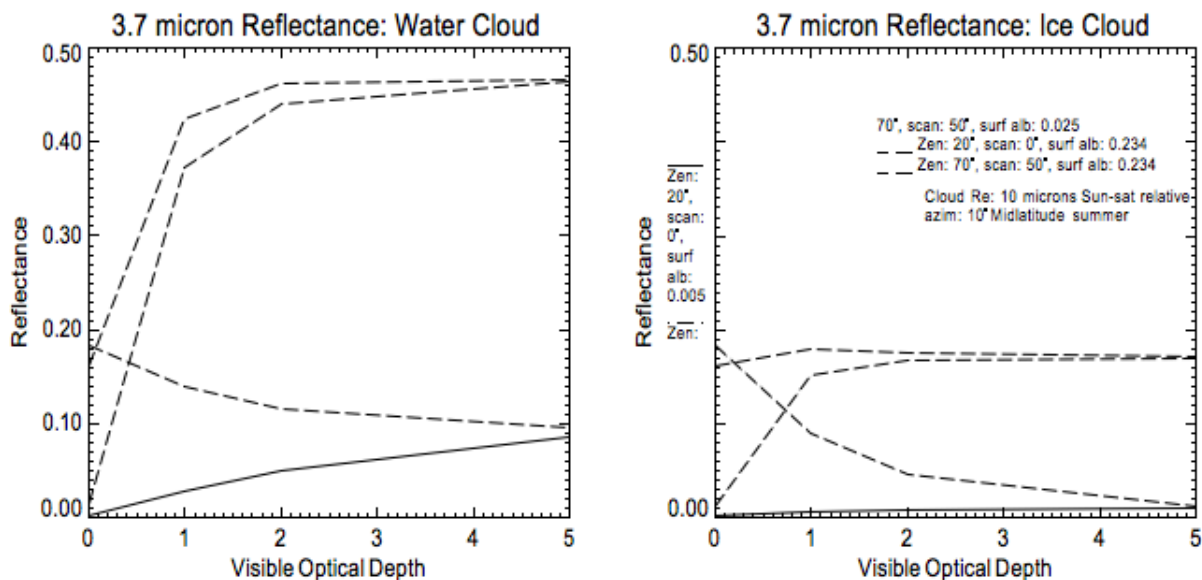


Figure 6. Channel 3 reflectance as a function of liquid (often simply "water") cloud optical depth for a variety of surface and viewing conditions.

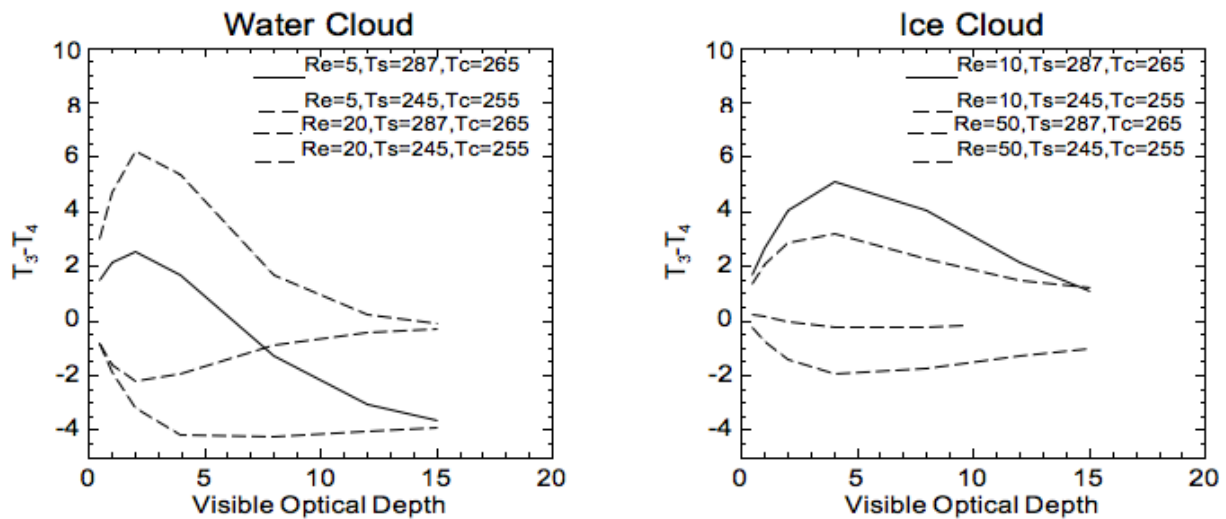


Figure 7. The brightness temperature difference (BTD) of AVHRR channels 3-4 as a function of cloud optical depth for water cloud (left) and ice cloud (right). T_c is the cloud top temperature, Re is the cloud particle effective radius.

3.8.1.1 Radiative Transfer Model

Cloud detection and the retrieval of cloud optical depth and particle effective radius rely heavily on modeled TOA albedo and brightness temperature. Before detailing those procedures, the radiative transfer model Streamer ([Key and Schweiger, 1998](#)) is briefly described. TOA radiances (intensities) are computed for use in the cloud property retrievals while irradiances (fluxes) are computed in order to examine the surface radiation budget. For radiances, Streamer uses the Discrete Ordinates Radiative Transfer (DISORT) solver described in [Stamnes et al. \(1988\)](#). For irradiances the two-stream method following [Toon et al. \(1989\)](#) is employed. In both cases there are 24 shortwave and 105 longwave spectral bands. Gas absorption for water vapor, ozone, CO₂ and oxygen is parameterized using an exponential sum fitting technique ([Tsay et al., 1989](#)).

Cloud optical properties are based on parameterization schemes from three different sources. For water clouds, the data are taken from [Hu and Stamnes \(1993\)](#). Effective radii range from 2.5 to 60 μm for shortwave and longwave portions of the spectrum. For ice clouds in the shortwave the parameterization of [Fu and Liou \(1993\)](#) is used. Longwave ice cloud optical properties are based on Mie calculations using spherical particles. This parameterization is unpublished but follows the methodology of [Hu and Stamnes](#). Both the water and ice cloud parameterizations are based on the empirical relationship between the particle effective radius and extinction, single scatter albedo, and the asymmetry parameter.

3.8.1.2 Single-Image Masking

The underlying philosophy of the single-image cloud detection procedure is that it should work as well as possible without requiring ancillary information. The target user is one who has a few individual images that are not necessarily part of a time series, and no additional information such as model fields of surface temperature or an elevation database. The single-image cloud mask procedure could certainly be improved with such information, but it would be unreasonable to require it.

The single image cloud mask uses four primary spectral tests and an optional secondary test. Many of the cloud test concepts can be found in the Air Force SERCAA procedures (Gustafson et al., 1994); some appear in the NOAA Clouds from AVHRR (CLAVR) algorithm (Stowe et al., 1991); most were developed and/or used elsewhere but refined and extended for use in the polar regions. The application of the spectral tests is conceptually simple: initialize the cloud mask to clear, then apply the spectral cloud tests to label cloudy pixels. The primary spectral cloud tests are described in the following paragraphs. Three of the five tests are applied under all solar zenith angle (SZA) conditions. See Table 6 for SZA cutoffs.

3.8.1.3 Cloud Tests

Split-Window Cirrus test, 11-12 μm (all SZA) - Ice clouds absorb and scatter less at 11 μm than at 12 μm , so their transmittances are higher at 11 μm . Water clouds also absorb less at 11 μm but they scatter more. Nevertheless, both ice and liquid clouds have higher transmittances at 11 μm . For cold cirrus clouds and thin water clouds the result is higher brightness temperatures at 11 μm . However, water vapor affects this difference and must be considered. This is accomplished indirectly through the use of the scan angle and brightness temperature. The brightness temperature differences between channels 4 and 5 (BTD45) are corrected for viewing angle effects before being used in any of the cloud tests. Individual pixels are labeled as cloudy if the corrected BTD45 is greater than the CT_THRESH thresholds (Tables 6, 7).

CT_THRESH values are from Saunders and Kriebel (1988) for temperatures of 260 K and greater, with minor adjustments at the low end of the temperature range (Table 7). For lower temperatures the table was extended by simulating clear sky values with *Streamer* and adding a small offset to account for unmodeled effects. The nadir thresholds are shown in Figure 8. A function that adjusts for the scan angle dependence of BTD45 was then determined empirically, with the same functional form as that given by Yamanouchi et al. (1987):

$$BTD45' = BTD45 - \frac{(23.6 - ZC)(1 - \cos\theta)}{1 - 0.1589(1 - \cos\theta)} \quad 3.22$$

where ZC is given in Table 7, BTD45 is the unadjusted brightness temperature difference, and θ is the scan angle. This effectively adjusts the raw brightness temperature difference to a nadir view. The angle adjustment functions are shown in Figure 9. Note that the sign of the correction changes at approximately 260 K. If BTD45' is greater than CT_THRESH then the pixel is cloudy. The model simulations assumed that the surface emissivities were the same at 11 and 12 μm . This is probably not the case for snow, so the thresholds are increased by 0.3 K if the surface is known to be snow. This correction should actually be done to radiances, as the emissivity effect is nonlinear in brightness temperature.

Warm clouds, 11-12 μm (all SZA) - The transmittance relationships described in the previous test hold true regardless of the relationship between the cloud and surface temperatures. For warm clouds BTD45 may be negative, so an additional test is required (cf., Yamanouchi et al., 1987). A pixel is considered to be cloudy if BTD45' < WT_THRESH (Table 7). Temperature inversions and warm clouds are ubiquitous during the polar night, but also occur at other times of the year and in other locations outside of the polar regions; e.g., over cold ocean currents.

Water cloud test, 1.6 and 3.7 μm (SZA < NOREFZEN) - The single-scattering albedo of small droplets at 1.6 and 3.7 μm (AVHRR channels 3A and 3B) is considerably larger than that of ice crystals, including snow on the surface. Therefore, the 1.6 and 3.7 μm reflectances are very high relative to snow, open water, and vegetation. For sunlit scenes the application of reflectance tests depends on the solar zenith angle. For solar zenith angles less than DAYZEN (Table 6) constant thresholds in channels 1 and 3 are applied. A pixel is considered cloudy if REF3 > REF3_OCEAN and REF1 > REF1_OCEAN or REF3

> REF3_LAND and REF1 > REF1_LAND, where REF1 and REF3 are the channels 1 and 3 reflectances. There are actually REF3_OCEAN and REF3_LAND variables for the 3.7 and 1.6 μm channels, channels 3B and 3A, respectively: REF3A_OCEAN, REF3B_OCEAN, REF3A_LAND, and REF3B_LAND. The channel referenced by "3B" is channel 3 through NOAA-15 and channel 3B on NOAA-16 and beyond. The visible reflectance test reduces the mislabeling of clear snow-free land and silty water (near mouths of rivers) pixels that have relatively high reflectances at 3.7 microns.

If the zenith angle is between DAYZEN and NOREFZEN then these thresholds are scaled, increasing as a function of the zenith angle. A function was derived empirically:

$$REF3' = REF3 + \left(a \frac{REF3ADD}{b} \right) \quad 3.23$$

where REF3' is the adjusted threshold, REF3 and REF3ADD correspond to ocean or land types (Table 6; REF3*_ADD), $a=(SZA-DAYZEN)^3$, and $b=(90-DAYZEN)^3$. The same adjustment is done for the channel 1 reflectance. A pixel is cloudy if its reflectance is

greater than REF3' or REF1'. No reflectance tests are applied to for zenith angles between NOREFZEN and NIGHTZEN. Note: This effect is still under investigation.

Low stratus-thin cirrus tests, 3.7-11 μm (SZA \geq NIGHTZEN) - Both ice and water clouds have lower emissivities at 3.7 μm than at 11 or 12 μm . Additionally, small droplets scatter much more efficiently at 3.7 μm than at 11 or 12 μm . For optically thick water clouds, where transmittance is small, this translates into a lower brightness temperature in channel 3. Stratus clouds often exhibit this effect, as do thin, warm clouds (less frequent). For thin, cold clouds the brightness temperature at 3.7 μm can be greater than that at 11 μm because of transmitted radiation from the warm surface in the shorter wavelength band. This is typical of cirrus clouds. A pixel is cloudy (low stratus) if $\text{BTD34} \leq \text{LSTTCI_34LO}(a,b)$, where BTD34 is the brightness temperature difference between channels 3 and 4. This is a temperature dependent test (T11): temperatures less than 235 use a threshold of LSTTCI_34LOa, LSTTCI_34LOb is for temperatures greater than 265, and temperatures in between use a threshold between these two values. Also, a pixel is cloudy (cirrus) if $\text{BTD34} \geq \text{LSTTCI_34HI}$. Due to the large amount of noise in channel 3 at low temperatures, this test is only performed for temperatures greater than MINTEMP.

Cold clouds - Surface Temperature Tests, 11 μm or T_s (all SZA) - These tests are intended to detect very cold clouds by comparing the 11 μm brightness temperature to either a climatological surface temperature or a surface temperature estimate. The cold cloud over oceans test is most useful during the summer months at night. It has little effect in the winter or during the daytime, when reflective tests work well. In some sense it performs in a manner similar to the MODIS CO2 high cloud test. It tends to find the cold, optically thick clouds that the thick cirrus, warm cloud, and low stratus tests miss. It is a simple threshold test that utilizes a monthly climatological estimate of the lowest expected surface temperature over the ocean (frozen or unfrozen). If the 11 μm temperature is less than the climatological minimum surface temperature, the pixel is cloudy.

The other cold clouds - surface temperature test relies on an estimate of the surface temperature input by the user, and is only performed if an estimate of the surface temperature (or 11 μm brightness temperature, both are treated equally) is provided. It is a simple threshold test such that any pixel with an 11 μm brightness temperature less than 20 K below the surface temperature estimate is considered to be cloudy. This is most useful at night during the winter when some optically thick, cold clouds are misidentified as clear sky.

3.8.1.4 Clear Tests

To account for potential problems with the cloud tests, particularly the BTD45, tests that confidently identify clear pixels are used. The clear tests are only applied to those pixels labeled CLOUDY by the cloud tests.

Low Near Infrared (NIR) reflectance test (DAY and HISZA regions): This test is the complement of the reflectance cloud test, where pixels with 1.6 or 3.7 μm reflectances less than $\text{REF3} \times 0.4$ are considered clear.

Normalized Difference Snow Index (NDSI) test (DAY and HISZA regions): The Normalized Difference Snow Index (NDSI; Hall et al.) is used in conjunction with the NIR reflectance for the AVHRR/3 with the 1.6 μm channel (NOAA-16 and higher). If NDSI is large and the NIR reflectance is small, then the pixel is clear. NDSI is calculated as

$$NDSI = \frac{\rho_1 - \rho_3}{\rho_1 + \rho_3} . \quad 3.24$$

where ρ_1 is the channel 1 reflectance and ρ_3 is the channel 3 reflectance.

Rethresholding

The secondary threshold test is a rethresholding operation using only the channel 4 brightness temperatures. Using pixels labeled as clear by the primary tests, an average channel 4 temperature image is constructed with a kriging procedure for small regions (200 km over land; 300 km over ocean). During the day ($\text{SZA} \leq \text{NOREFZEN}$) the 95th percentile clear sky temperature is used; during dim and dark conditions ($\text{SZA} > \text{NOREFZEN}$) the median is used. During the day, if the channel 4 temperature is more than DEL4DAY degrees and less than the clear temperature then it is cloudy. While this test works well in identifying thin cirrus, it results in some false detections near coastlines and in areas with large variability in elevation it may actually create more problems than it solves. During dim and dark conditions when temperature inversions and warm clouds are common, the test is two-sided. If the channel 4 temperature is more than DEL4LO degrees and less than the clear temperature or if it is DEL4HI degrees greater than the clear temperature then it is cloudy.

At night this rethresholding can be important for two reasons: (1) there is less spectral information available and (2) AVHRR channel 3 tends to be noisy at low temperatures, common during the polar night. Concerning the available spectral information, under most conditions optically thick clouds simply cannot be distinguished from clear sky with the three thermal channels alone. This is illustrated for a few cases in Figure 10. The result is false clear detections, i.e., cloudy pixels labeled as clear. Concerning noise in channel 3, it generally results in predictable errors - false cloud detections - so that those pixels not labeled as cloudy by the primary cloud tests are usually clear. So the primary spectral cloud tests at night are expected to result in some false detections for noisy pixels and for optically thick clouds.

The thresholds can be adjusted collectively through the *threshadj* keyword to the procedures **caspr** and **cloudmask_1**. This keyword allows the user to adjust the algorithm to be "cloud-conservative" or "clear-conservative". The cloud/clear-

conservative decision is necessary because there will always be partly cloudy pixels, mixed phase clouds, mixed clear pixels, etc. that do not fall neatly into one class or the other. However, this is a somewhat crude in that not all thresholds scale linearly. For best results, change the individual thresholds until the desired results are achieved. The *threshadj* keyword is used in the single-image cloud masking mode when clear parameters are computed. A second, clear-conservative mask is generated to increase the likelihood that those pixels labeled as clear actually are clear.

It is assumed here that we have no a priori knowledge of surface characteristics (e.g., surface temperature from the previous day) and no a priori knowledge of the location of snow/ice. In fact, the only distinction between surface types is land and ocean. Land may be snow-free or snow-covered. Ocean can be open water or sea ice. Additionally, the nighttime procedure does not incorporate any surface type distinction. This severely limits single-image cloud masking accuracy. Having such information would allow the use of additional spectral cloud tests (e.g., the channel 2/1 ratio over snow-free land), and would allow "tighter" thresholds.

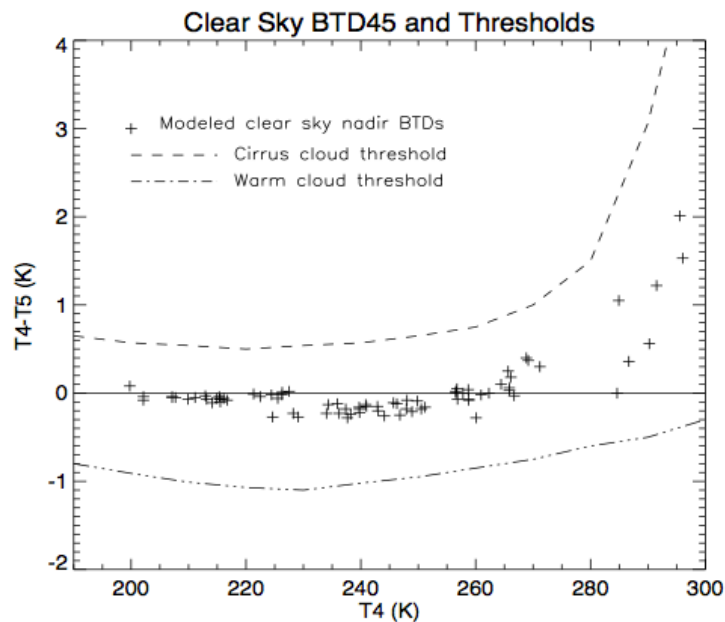


Figure 8. Modeled (*Streamer*) clear sky brightness temperature differences (plus signs) and the cirrus and warm cloud test thresholds (dashed and solid lines, respectively).

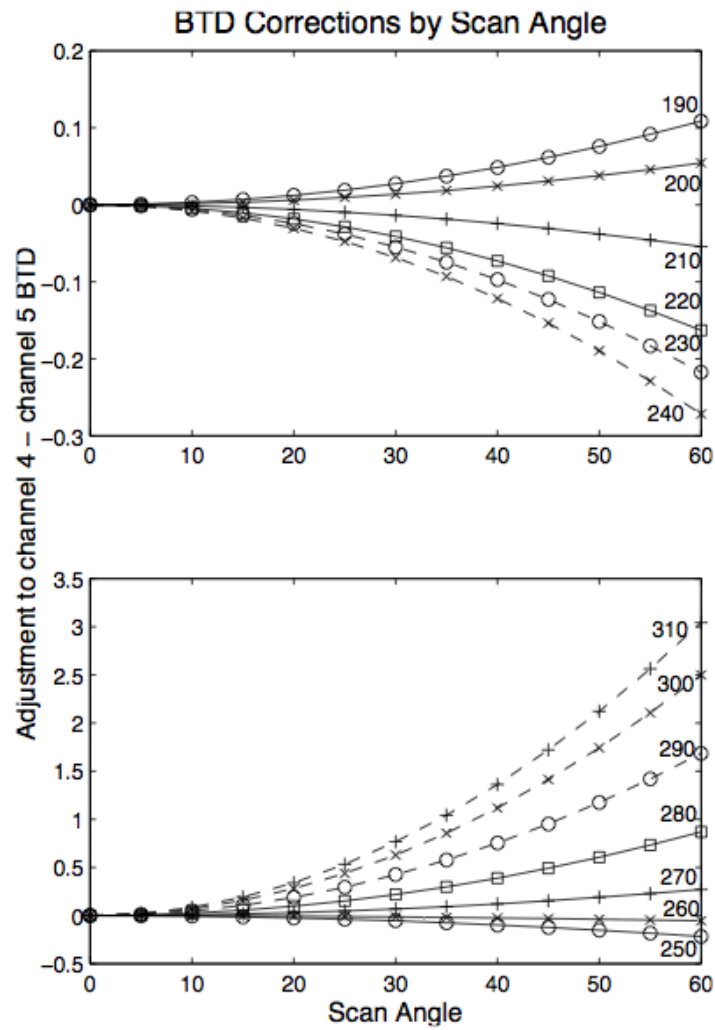


Figure 9. Brightness temperature difference dependence on scan angle. These functions are used to adjust brightness temperature differences before application of the cirrus and warm cloud tests.

Table 6. Thresholds used in cloud detection.

Threshold Variable	Value
DAYZEN	60
NOREFZEN	85
NIGHTZEN	88
DEL4DAY	8.0
DEL4LO	4.0
DEL4HI	4.0
REF3A_OCEAN	0.04
REF3B_OCEAN	0.1
REF1_OCEAN	0.35
REF3A_LAND	0.40
REF3B_LAND	0.09
REF1_LAND	0.35
REF3A_OCEAN_ADD	0.0
REF3B_OCEAN_ADD	0.0
REF3A_LAND_ADD	0.15
REF3B_LAND_ADD	0.15
REF3A_SNOW_ADD	0.5
REF3B_SNOW_ADD	0.5
REF1_OCEAN_ADD	0.10
REF1_LAND_ADD	0.15
LSTTCI_34Loa	0.3
LSTTCI_34Lob	-0.7
LSTTCI_34HI	3.5

Table 7. Brightness temperature difference thresholds for the cirrus cloud test as a function of temperature (K).

	190	200	210	220	230	240	250	260	270	280	290	300	310
CT_THRESH	0.45	0.37	0.34	0.34	0.34	0.40	0.50	0.75	1.00	1.50	3.06	5.77	9.41
WT_THRESH	-0.8	-0.91	-1.01	-1.07	-1.1	-1.02	-0.95	-0.85	-0.75	-0.6	-0.5	-0.3	-0.15
ZC	23.4	23.5	23.7	23.9	24.0	24.1	24.0	23.7	23.2	20.5	19.7	19.0	18.0

3.8.1.5 Time Series Masking

The time series cloud masking procedure operates on a sequence of images acquired on consecutive days at approximately the same solar time. It first applies spectral tests for an initial labeling of cloudy and clear pixels, then further refines the identification of clear pixels by examining changes in spectral characteristics from one day to the next. The clear pixels that result from these spectral and temporal tests are used to construct a clear sky radiance statistics over some number of days for various spectral channels. The statistics are then used in a final thresholding operation to label/relabel pixels as either clear or cloudy. More specifically the steps are:

1. Apply the single-image cloud mask procedure to identify pixels that are likely to be cloudy. This alleviates the problem of pixels with persistent cloudiness being labeled as clear in the time tests.
2. Examine the time change in spectral characteristics between pairs of days. A pixel is clear if the spectral tests (step #1) diagnose it as not cloudy and if its brightness temperature varies little from one day to the next (the TIMETHRESH* thresholds in Table 8). The channel 4 brightness temperature and the adjusted brightness temperature difference (4-5) are used in the dark parts of the image; these plus the channel 1 reflectance, and the channel 3 reflectance are used in the sunlit portions. Table 8 gives the thresholds used in this step.
3. Clear sky statistics are compiled for each pixel using all clear values within some distance of the pixel and over some number of days (typically 150x150 km cells and 5 days). Medians of the channels 1 and 3 reflectances (day only) and the channel 4 temperature (day and night) are computed. If a cell occurs along a coastline, only pixels with the same surface type (LAND or NOTLAND) as the center pixel are used. Pixels in the clear sky composite that did not have medians assigned due to the lack of clear values are filled with a kriging interpolation scheme. The probability of finding clear pixels can be increased by enlarging the cell size or using more days, but doing so also increases the variability of the statistics and may adversely affect the next step.

4. The clear sky composite statistics are used in a final threshold operation to label or relabel all pixels as clear or cloudy. A pixel can be labeled as cloudy if its brightness temperature is higher or lower than its mean clear value plus or minus, respectively, some value that reflects the natural variability for clear sky, or if its reflectance in either channel 1 or 3 (daytime) is higher than its mean clear reflectance plus (not minus) some value (DEL* in Table 8). However, the single-image spectral tests are run again in cloud-conservative mode and those pixels labeled as cloudy will also be cloudy in the final mask. This implies higher confidence in the spectral tests (with cloud-conservative thresholds) than in the final thresholding operation.

Table 8. Time and final thresholds used in cloud detection.

Threshold Variable	Value
TIMETHRESH3A	0.06
TIMETHRESH3B	0.04
TIMETHRESH1	0.07
TIMETHRESH4_LAND	3.0
TIMETHRESH4_OCEAN	2.0
TIMETHRESH45_LAND	0.40
TIMETHRESH45_OCEAN	0.35
DEL4LO_OCEAN	3.0
DEL4HI_OCEAN	3.0
DEL4LO_LAND	4.0
DEL4HI_LAND	4.0
DEL4LO_SNOW	6.0
DEL4HI_SNOW	6.0
DEL1	0.07
DEL3A_OCEAN	0.06
DEL3A_LAND	0.08
DEL3B_OCEAN	0.045
DEL3B_LAND	0.055

Cloud masks for images at the beginning and end of the time series have a much larger uncertainty than those at least $n_{\text{days}}/2$ places away from the ends. This results from the first and last few images being at the beginning or end of the n_{days} images on which the clear sky statistics were based. For example, given $n_{\text{days}} = 5$, the cloud mask for the first image is determined from the final thresholding based on clear sky statistics over days 1-5. The cloud mask for the third image is based on statistics from the same period. Obviously, the statistics are more representative of the third image of the first.

3.8.2 Numerical Strategy

Not applicable.

3.8.3 Calculations

The AVHRR reflectances, brightness temperatures, and viewing and illumination geometry are input in addition to a surface type mask. Cloud tests are executed sequentially. Time series cloud detection is applied as described above.

3.8.4 Look-Up Table Description

There are no look-up tables for cloud detection. The thresholds in the tables above are part of the code.

3.8.5 Parameterization

Parameterizations are described above.

3.9 Theoretical Description: Cloud Particle Phase

3.9.1 Physical and Mathematical Description

This section describes the algorithms used in the determination of cloud particle phase. In this algorithm, all clouds are composed of either liquid droplets ("water cloud") or solid ice crystals ("ice cloud"). No attempt is made to identify mixed-phase or multilayer clouds. The theoretical background for these procedures is detailed in Key and Intrieri (2000). Only a partial description is given here.

The determination of cloud particle phase, liquid or solid (generally referred to as "water" and "ice"), is based on both physical and spectral properties. Physically, liquid cloud droplets can exist at temperatures as low as -40 C, perhaps even lower, although clouds are likely to be composed of both liquid droplets and ice crystals at temperatures below -10 C. The spectral difference between water and ice clouds occurs because of differences in absorption and scattering. Based only on the imaginary index of refraction, which is an

indicator of absorption, more absorption will take place in ice clouds at 11 and 12 μm than in water clouds, so brightness temperature differences between 3.7 and 11 or 12 μm will be larger for ice clouds. However, absorption alone does not provide enough information to explain observed spectral differences. The single scattering albedo indicates how effective a volume of particles are at scattering incident radiation. Unlike the imaginary index of refraction, it applies to size distribution of particles. Scattering is greater at 3.7 μm than at 11 or 12 μm and the smaller the particle, the greater the scattering. But for typical ice crystals sizes there is very little difference in scattering across this portion of the spectrum. Furthermore, the single scattering albedo indicates that during the day, ice clouds will exhibit a lower reflectance at 3.7 μm than water droplets. At visible wavelengths, the single scattering albedo of both water and ice clouds is near unity and absorption is near zero.

For optically thick clouds, where the transmittance is near zero and the surface contribution to upwelling radiance is small, absorption and scattering define the spectral characteristics of a cloud. We expect the brightness temperature difference between channels 3 and 4 (BTD34) to be negative for water clouds with small effective radii. For thick ice clouds with particle effective radii of 30 μm or larger, the single scattering albedo indicates that BTD34 would be near zero. This is, in fact, the case, as demonstrated by the model calculations (Streamer) presented in Figure 10. Both plots show that for visible optical depths τ greater than 5, water cloud BTD34 is negative while ice cloud differences tend to be positive, at least for smaller water droplets and larger ice crystals. For larger optical depths BTD34 for ice clouds decreases. For optically thin clouds the transmissivity is not negligible and the surface temperature influences the brightness temperature measured at the satellite. BTD34 for cold, water clouds (surface is warmer than the cloud) is positive when the optical depth is small. BTD34 for ice clouds takes on larger positive values in these cases. The opposite occurs for warm ice clouds, where BTD34 is negative.

The brightness temperature difference between 11 and 12 μm , BTD45, is much smaller than BTD34 for both water and ice clouds, and there is considerable overlap in BTD45 for the two phases (Figure 10). The absolute value of BTD45 increases as cloud optical depth decreases (not shown). Therefore, large BTD45 differences (positive or negative) indicate thin clouds.

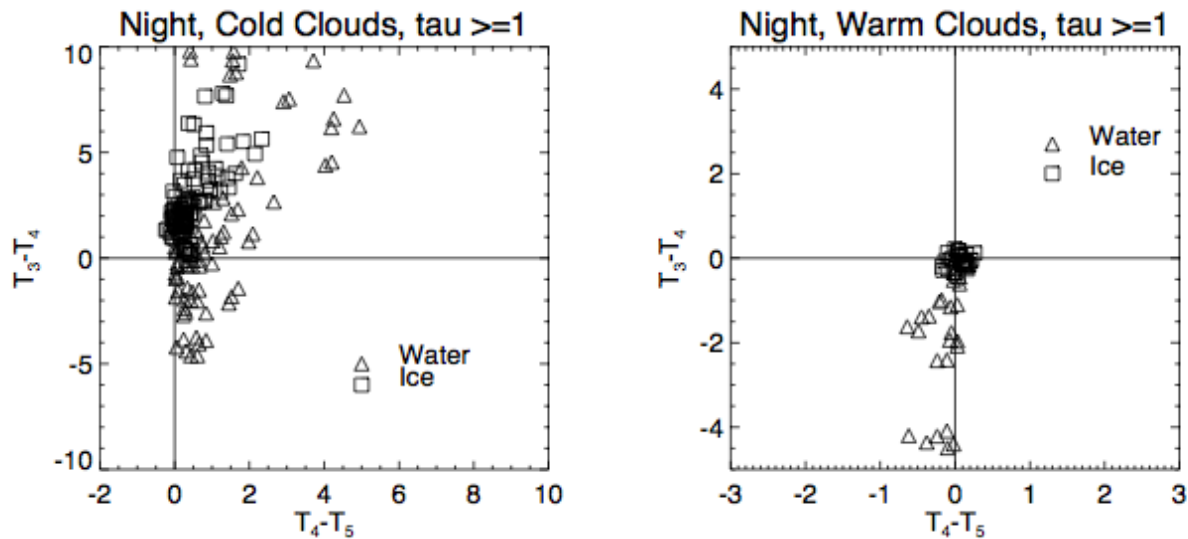


Figure 10. Modeled brightness temperature differences for AVHRR channels 3 minus 4 (3.7 minus 11 μm) and channels 4 minus 5 (11 minus 12 μm) for water and ice clouds. The visible optical depth for the data shown is one or greater. Water clouds have top temperatures greater than 250 K; ice clouds are less than 270 K. Calculations were done for tropical, midlatitude, and arctic conditions.

In the presence of solar radiation, the single scattering albedo at 3.7 or 1.6 μm is the primary spectral feature used in distinguishing ice and water cloud. Ice particles do not scatter as efficiently as water droplets at this wavelength, due to both their indices of refraction (the real part) and the fact that ice clouds are typically composed of larger particles, which scatter less efficiently, than water clouds. However, the actual reflectance depends not only on particle phase, but also on viewing and illumination geometry and surface reflectance. This is illustrated in Figure 11, which shows the 3.7 μm (NOAA-15 and earlier) and 1.6 μm (NOAA-16 and later) modeled reflectances as a function of the scattering angle. The scattering angle ψ is the angle between the incident and reflected beams:

$$\psi = 180 - \text{acos}(\cos\theta_{sun} \cos\theta_{sat} + \sin\theta_{sun} \sin\theta_{sat} \cos\phi) \quad 3.25$$

where θ_{sun} is the solar zenith angle, θ_{sat} is the satellite zenith angle, and ϕ is the relative azimuth angle (where 0 is looking away from the sun and 180 is looking into the sun); all angles are in degrees. A scattering angle of 0° implies forward scattering; 180° means backscattering. The figure gives reflectances for cloud visible optical depths between 2 and 5, and for snow and vegetation surfaces. These two surface types exhibit somewhat different 3.7 μm clear sky reflectances and very different clear sky reflectances at 1.6 μm . However, their effect on the reflectance of thick clouds is minimal. The smooth curves represent approximate upper limits for ice cloud reflectance at each wavelength, valid for ψ values

between 0° and 160° and for optically thick clouds. In the case of strong backscattering ($\psi > 160^\circ$), and in the case of thin clouds, the separation between water and ice cloud is less clear.

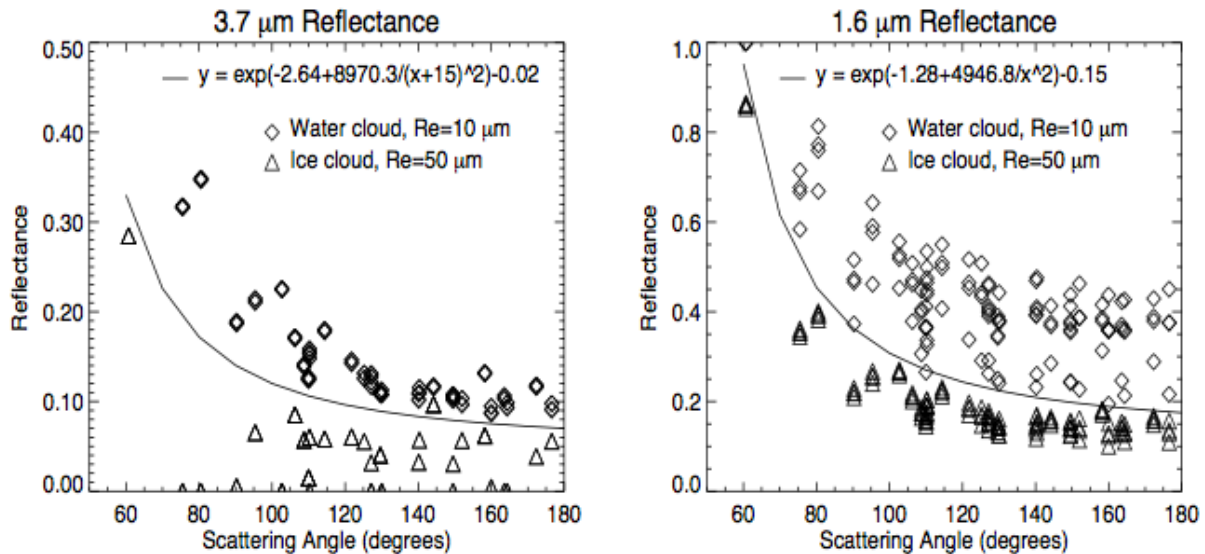


Figure 11. AVHRR channels 3 ($3.7 \mu\text{m}$) and 3A ($1.6 \mu\text{m}$) modeled reflectances as a function of scattering angle for water (diamond) and ice (triangle) clouds. All clouds have visible optical depths in the range 5-10. Also shown are the functions that approximately divide water and ice clouds at each of the two wavelengths. Calculations were done using midlatitude summer conditions.

The phase algorithm starts by exploiting the physical property that only ice crystals will exist below some threshold temperature and only liquid droplets will exist above some other threshold temperature. For optically thick clouds the $11 \mu\text{m}$ brightness temperature will be very close to the kinetic temperature and simple temperature thresholds can be used to distinguish particle phase. For example, if T_4 were less than some minimum value, $\gamma_{\min} = 243 \text{ K}$ (-30 C), then an optically thick cloud would almost certainly be composed of ice crystals. Similarly, if T_4 were greater than some maximum value, $\gamma_{\max} = 273 \text{ K}$ (0 C), then the cloud would be liquid. But for optically thin clouds surface emission is a significant part of the measured radiance and the relationship between the surface temperature and T_4 must be considered. Using the two thresholds above there are four relationships between the surface temperature T_s and T_4 that can be exploited to determine the phase, as listed in Table 9.

The clear sky temperature can be used as a proxy for T_s , although T_s will generally be somewhat lower than the clear sky value during the day (negative cloud radiative effect) and somewhat higher at night. The clear sky surface temperature can therefore be adjusted by a small amount δ . At night $\delta = -2 \text{ K}$ and during the day $\delta = +2 \text{ K}$ in this study.

The application of these four conditions constitutes the first step of phase determination. The tests in Table 9 do not handle water clouds with temperatures less than γ_{\max} or less than T_s , and ice clouds with temperatures greater than γ_{\min} or greater than T_s .

Table 9. Phase assignment based on temperature relationships.

Condition	Phase
$T_s - \delta < \gamma_{\max}$ and $T_4 > \gamma_{\max}$	Liquid
$T_s - \delta > \gamma_{\max}$ and $T_4 > T_s$	Liquid
$T_s - \delta > \gamma_{\min}$ and $T_4 < \gamma_{\min}$	Ice
$T_s - \delta < \gamma_{\min}$ and $T_4 < T_s$	Ice

If no estimate of T_s is available then an alternate, though less robust, method would be to apply simple thresholds; e.g., if T_4 is less than 243 K (-30°C) then the cloud is ice and if T_4 is greater than 303 K (+30°C) then the cloud is liquid. Hutchison et al. (1997) use -40°C for the lower threshold but suggest that -30°C is probably a reasonable lower bound. They do not suggest an upper bound for liquid clouds.

The second step employs the spectral properties described in the previous section and is different for day and night conditions. It is applied to the cloudy pixels that were not labeled in the first step. At night the tests are intended to identify optically thick ice cloud, thick water cloud, and most thin water cloud. The tests are: (a) if $T_3 - T_4$ is less than -0.5 K then it is a water cloud and (b) if $T_3 - T_4$ is greater than +1 K and $T_4 - T_5$ is between 0 and 1 K then it is an ice cloud.

During the day the tests in the second step are based on the 3.7 or 1.6 μm reflectance characteristics, utilizing the two reflectance functions shown in Figure 11. Only pixels with ψ less than 160 degrees and $T_4 - T_5$ less than 1 K are evaluated, as reflectances for strong backscattering and thin clouds are ambiguous. Observed 3.7 or 1.6 μm reflectances less than the threshold function values indicate ice cloud; those greater than the function values are water cloud.

The last step is to label any pixels that were not handled by the previous two steps. A simple temperature threshold is employed: if the 11 μm brightness temperature is less than 258.16 K (-15°C) then the cloud phase is ice, otherwise it is liquid. Because of the low precision and high uncertainty in T_3 (and therefore $T_3 - T_4$) when temperatures are very low, all pixels with T_4 less than 230 K are labeled as ice.

3.9.2 Numerical Strategy

Not applicable.

3.9.3 Calculations

The AVHRR reflectances, brightness temperatures, and viewing and illumination geometry are input. Cloud particle phase is retrieved based on the tests described above.

3.9.4 Look-Up Table Description

There are no look-up tables for the cloud particle phase algorithm.

3.9.5 Parameterization

There are no parameterizations for the cloud particle phase algorithm.

3.10 Theoretical Description: Cloud Optical Depth and Particle Effective Radius

3.10.1 Physical and Mathematical Description

The retrieval of cloud optical and microphysical properties from the AVHRR or AVHRR-like wavelengths has a long history; only a sample of the literature is given here. [Hunt \(1973\)](#) demonstrated the sensitivity of cloud emittance to changes in optical depth and particle size at thermal wavelengths. [Liou \(1974\)](#) showed that cirrus optical properties varied between 11 and 12 μm . [Arking and Childs \(1985\)](#) describe a technique for extracting a microphysical model parameter from AVHRR data. [Inoue \(1985\)](#) used the split-window channels to estimate cloud optical depth with an implicit particle size, while [d'Entremont \(1986\)](#) detected low clouds and fog at night using the variation of the 3.7-11 μm difference with particle size. Using a radiative transfer model and ground-based lidar for validation, [Stone et al. \(1990\)](#) discuss the problem of retrieving cirrus cloud optical depth from radiance measurements. [Lin and Coakley \(1993\)](#) used AVHRR channels 4 and 5 to simultaneously solve for the emittance and cloud fraction. [Ou et al. \(1993\)](#) developed a method to derive optical depth, cloud top temperature, and effective radius from nighttime observations in AVHRR channels 3 and 4. [Baum et al. \(1994\)](#) modeled brightness temperature differences for liquid and ice clouds over the ocean. A review of cloud observations using satellites was given by [Rossow \(1989\)](#).

The importance of cloud optical depth, τ and the particle effective radius, r_e for remote sensing lies in the fact that the optical properties of clouds used in the calculation of radiative fluxes, the single scattering albedo, the asymmetry parameter, and the extinction coefficient, are proportional to the optical depth and effective radius. Cloud optical depth (unitless) is a measure of the cumulative depletion of radiation as it passes through the cloud. It is related to the transmissivity, t via,

$$t = e^{-\tau} \quad 3.26$$

and is a product of the volume extinction coefficient and the physical thickness of the cloud.

The particle effective radius for liquid droplets is the ratio of the third to second moments of the drop size distribution $n(r)$:

$$r_e = \frac{\int_0^{\infty} r^3 n(r) dr}{\int_0^{\infty} r^2 n(r) dr} . \quad 3.27$$

For ice crystals the size parameter is better termed the "mean effective size". It is based on the parameterization of Fu and Liou (1993), which was developed from ray tracing calculations for scattering by randomly-oriented hexagonal crystals. The mean effective size is defined as:

$$D_e = \left(\int_{L_{min}}^{L_{max}} D^2 L n(L) dL \right) / \left(\int_{L_{min}}^{L_{max}} D L n(L) dL \right) \quad 3.28$$

where D is the width of an ice crystal, L is the length, $n(L)$ is the size distribution, and L_{min} and L_{max} are the minimum and maximum lengths of ice crystals, respectively. Here, "effective radius" refers to these two size parameters.

Cloud optical depth retrievals are done using a comprehensive database of modeled reflectances and brightness temperatures covering a wide range of surface and atmospheric conditions (Key, 1995). Figures 12 and 13 give a few examples of the modeled data used in the retrieval of cloud optical depth and particle effective radius.

The basic approach for daytime retrievals of water (liquid) cloud follows that of Nakajima and King (1990) as illustrated in Figure 12. In the presence of solar radiation the retrieval is done using the reflectance in channels 2 and 3 (or 3A for NOAA-16 and later). For ice clouds under solar illumination the channel 3 reflectance is so small that it is unreliable. So channels 4 and 5 are used to obtain a range of possible solutions and channel 2 is used to constrain the solution. A valid solution exists if the observed brightness temperatures and BTDs fall within the range of the modeled data. If no valid solution was found, MISSING values are assigned.

At solar zenith angles greater than about 75-80 degrees over bright surfaces, uncertainties in modeled radiances increase due to the unknown bidirectional reflectance of the surface and unmodeled 3-dimensional cloud effects. When the solar zenith angle is greater than 80 degrees but less than 90 degrees, and when the surface clear sky channel 2 reflectance is

high, only channels 4 and 5 are used in the retrieval. Solutions are obtained for all cloud top temperatures in the modeled data, and the effective radius/optical depth pair for the lowest cloud (arbitrary) that had a valid solution is given as the result. If no valid solution was found, MISSING values are assigned. Figure 5 shows the latitudes and times of the year where solar zenith angles greater than 75 degrees are experienced.

For nighttime retrievals, brightness temperature differences for channels 3 (or 3B) and 4 and 4 and 5 are employed (Figure 13). Both methods are based on the fact that the optical properties of clouds are different at each of the wavelengths examined. All three thermal channels are used for both liquid or ice clouds. The lookup table of brightness temperature differences is constructed for three different cloud top heights: 850, 650, 500 mb for liquid clouds and 700, 500, and 300 mb for ice clouds. The retrieval is done for each cloud top in both thermal channel combinations (3, 4 and 4, 5). The solution is the channel 4, 5 retrieval where the difference between the retrievals from both channel pairs is smallest.

In the lookup table procedure, values are interpolated according to the observed values of solar zenith angle (0-85 degrees), precipitable water (2987-29,879 g m⁻²), and surface visible albedo (daytime; 0.06-0.99) or temperature (nighttime; 228-283 K). Single values of aerosol optical depth (0.06) and total column ozone (325 Dobson units) are used in all cases. Bilinear interpolation is done between effective radius and optical depth value pairs in the lookup tables; i.e., between the four points of each polygon in Figures 12 and 13. Effective radii for liquid clouds are 2.5, 6, 10, 14, 20 μm and for ice clouds are 20, 40, 60, 90, 120 μm .

Optical depth values are 0, 1, 2, 4, 10, 20, 50, 80, and 150, with a maximum nighttime value of 15 and an ice cloud maximum of 50. The optical depth maximum for ice clouds is a result of their relatively low water contents. All clouds are modeled as either water or ice, with no mixed-phase clouds or overlapping combinations. Of course, it is entirely possible to have a liquid cloud under an ice cloud with a total optical depth greater than 50.

For the daytime retrievals the reflectance of the surface under the cloud is assumed to be known. Similarly, the surface temperature under the cloud is needed for the nighttime retrievals. Neither can be measured directly from the AVHRR so they must be estimated. The relationship between the clear and cloudy sky reflectances depends on the cloud optical depth, phase, and the particle size distribution, and the anisotropic and spectral reflectance characteristics of the surface. The cloudy sky surface temperature is related to the clear sky temperature through the cloud base temperature, the residence time of the cloud, and the turbulent fluxes. Given the complexity of these relationships, no attempt is made to relate clear and cloudy temperatures or reflectances. A kriging procedure is used to create relatively smooth surfaces from the existing clear sky reflectances and temperatures for each surface type in the image. These clear sky surfaces are used as proxies to the actual surface reflectance and temperature in the optical depth/effective radius retrievals. The effect of using the clear sky values in place of the cloudy sky values is probably minimal for the daytime retrievals. At night, however, the effect can be significant, generally resulting in

a positive bias in optical depth (i.e., the optical depths are too large) because clear sky surface temperatures may be considerably lower than cloudy sky temperatures.

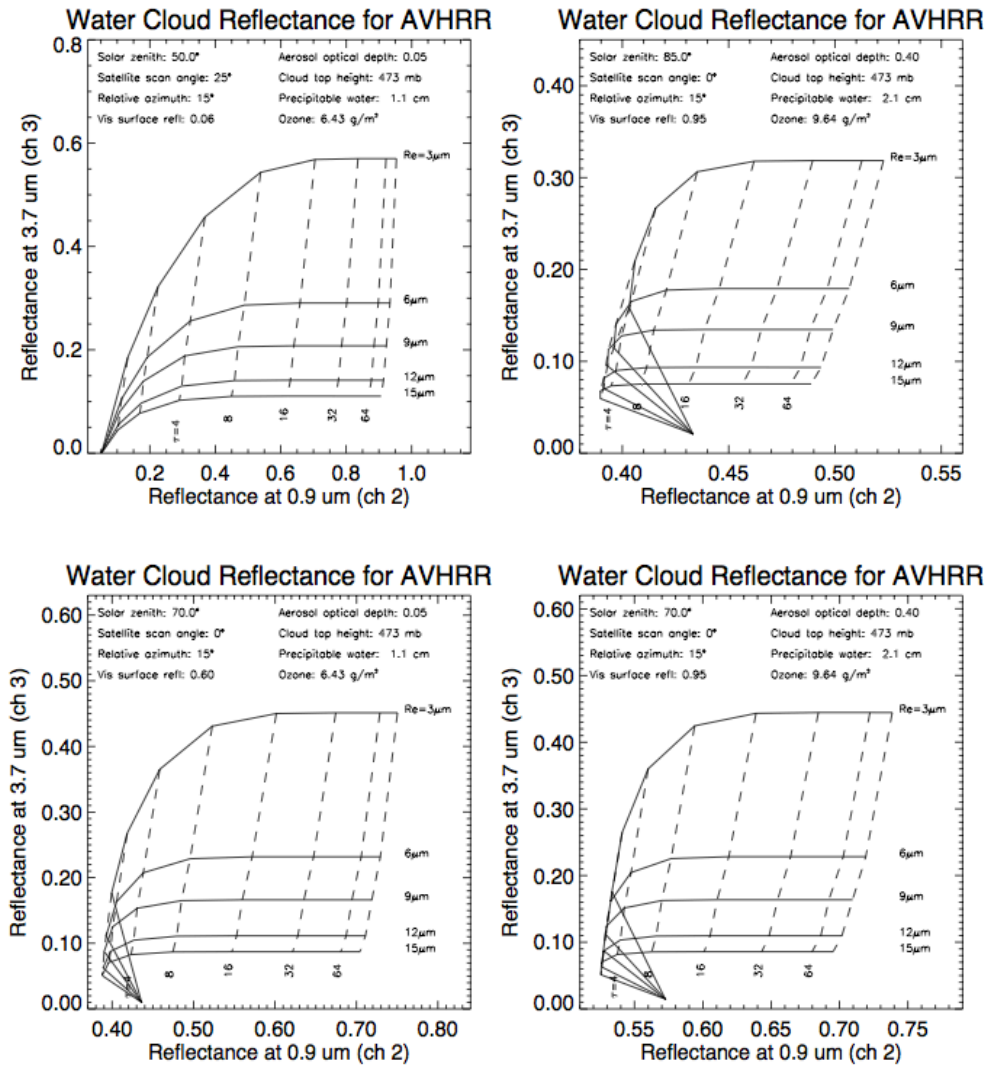


Figure 12. The relationship between two AVHRR reflective channels (2 and 3) as a function of water cloud optical depth and droplet effective radius over different surface types.

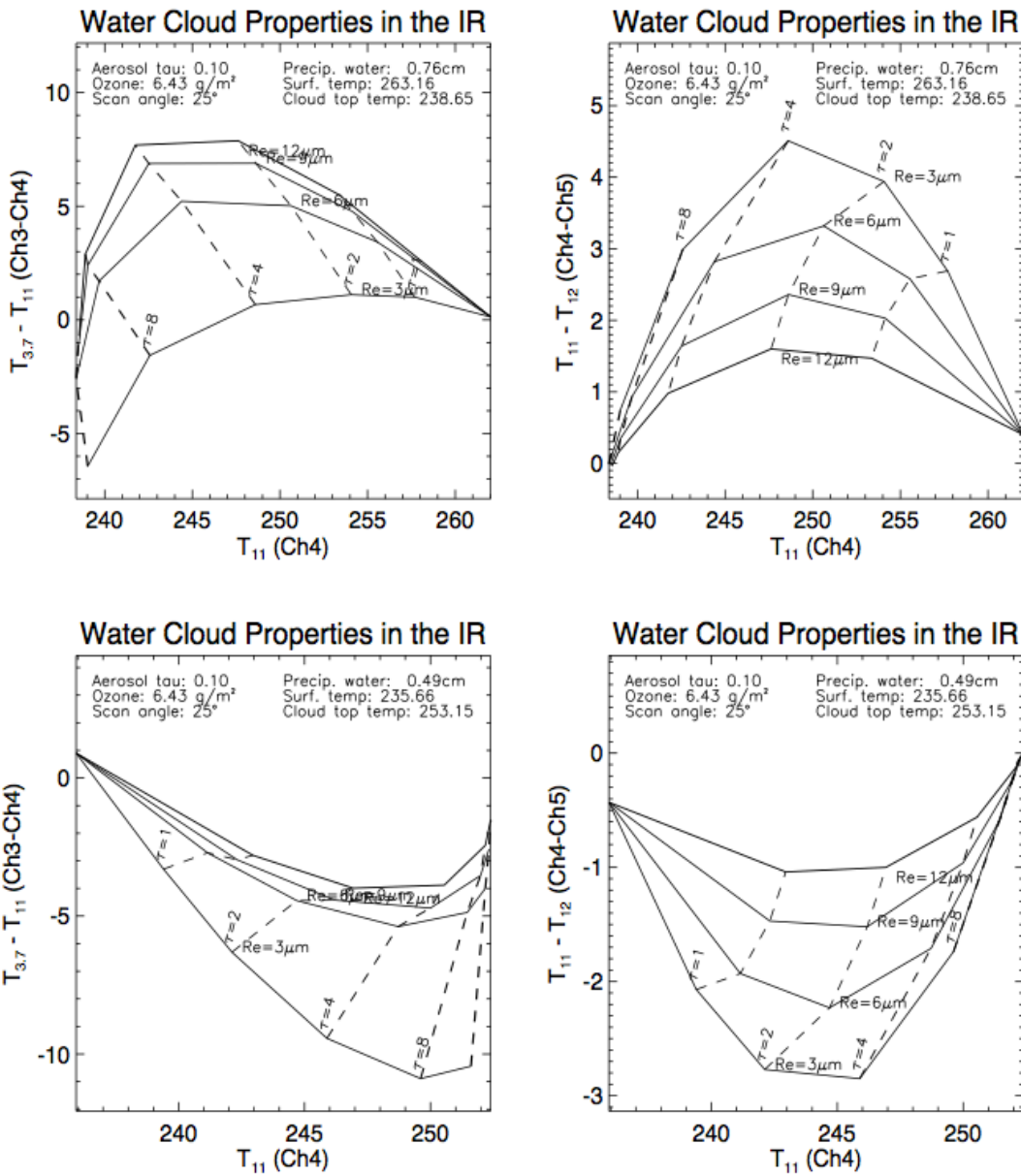


Figure 13. The relationship between the AVHRR channel 4 brightness temperature and the channels 4-5 difference as a function of water cloud optical depth and effective radius.

3.10.2 Numerical Strategy

Not applicable.

3.10.3 Calculations

The AVHRR reflectances, brightness temperatures, and viewing and illumination geometry are input. Previously calculated surface albedo, surface temperature, and cloud particle phase are used. Cloud optical depth and effective radius are retrieved simultaneously.

3.10.4 Look-Up Table Description

A look-up table of simulated AVHRR reflectances and brightness temperatures was generated with the Streamer radiative transfer model. Channel data are stored as a function of sensor scan angle, solar zenith angle, sun-satellite relative azimuth angle (5 degree bins), surface albedo, and surface temperature (file `retaudat.sav`).

3.10.5 Parameterization

There are no parameterizations for the cloud optical depth and effective radius algorithm.

3.11 Theoretical Description: Cloud Temperature and Pressure

3.11.1 Physical and Mathematical Description

The cloud temperature is determined from the channel 4 brightness temperature, the clear sky brightness temperature (not corrected for the atmosphere), and the visible cloud optical depth. The infrared optical depth is determined from the visible optical depth using parameterizations of cloud optical properties. The thermal cloud optical depth, which in the retrieval is a nadir (vertical) optical depth, is converted to an optical depth along the slant (viewing) path by dividing it by the cosine of the sensor scan angle. If this adjusted cloud optical depth is less than some threshold, the brightness temperature is assumed to be a function of both the cloud temperature and the upwelling radiation from the surface and atmosphere below the cloud. The threshold is taken from the ISCCP D-series cloud processing scheme, chosen such that clouds with optical depths greater than the threshold have transmittances of less than 1% (equivalent to an optical depth of 4.6) and are considered opaque. For opaque clouds the cloud top temperature is simply the channel 4 temperature. If the cloud is not opaque, then the cloud temperature is determined by first computing the cloud transmittance, t from the infrared optical depth, then calculating the cloud radiance that would be required to produce the observed radiance of the cloudy pixel, given the cloud optical thickness and the observed clear sky radiance (as an approximation of the surface radiance under the cloud):

$$L_c = \frac{L_4 - tL_{clear}}{1 - t} \quad 3.28$$

where L_c is the cloud radiance, L_4 is the channel 4 radiance, and L_{clear} is the clear sky radiance. If the estimated surface temperature is too low and the cloud is thin, then the cloud top temperature will be too high and vice versa. If the adjusted cloud top temperature is either lower than the tropopause temperature or higher than the maximum temperature from 950 mb to the tropopause, then it is reset to either the minimum or maximum temperature, as appropriate.

This scheme does not necessarily determine the cloud top temperature, but rather the effective radiating cloud temperature. While this may be close to the top temperature, it will generally represent a temperature somewhere beneath the cloud top. The differences between the retrieved cloud temperature and the actual cloud top temperature are illustrated in Figure 14 for two cases. For thin clouds the difference is greatest. Fortunately, the effect of this "error" on longwave radiative fluxes is small, because the thinner the cloud, the lesser its influence.

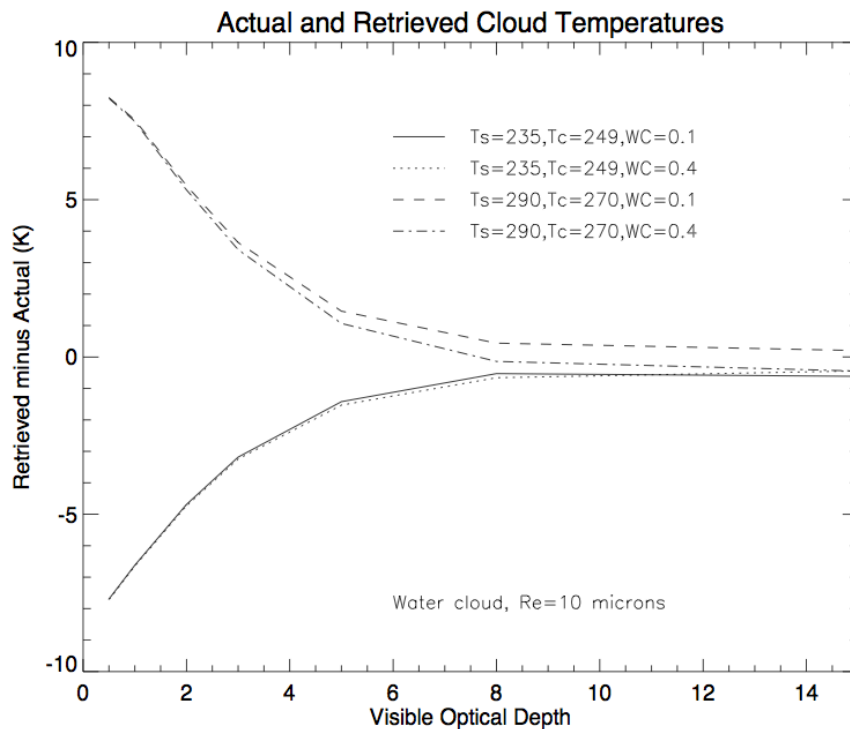


Figure 14. The difference between the retrieved cloud temperature and the actual cloud top temperature as a function of cloud optical depth. Differences are based on model simulations (Streamer) for two cloud-surface temperature relationships and for two cloud water contents (g m^{-3}).

The vertical location of the cloud, expressed as the cloud pressure, is determined by searching the temperature profile from the tropopause (or top of profile if below the tropopause) down. With this scheme, if a cloud has a temperature that could be either within or above an inversion, it will be placed below, i.e., closer to the surface (arbitrary).

3.11.2 Numerical Strategy

Not applicable.

3.11.3 Calculations

The AVHRR channel 4 brightness temperature, the clear sky brightness temperature (not corrected for the atmosphere), and the visible cloud optical depth are input to the algorithm. Cloud temperature is calculated as described above, and the temperature is located in a temperature profile (input model data) to retrieve the cloud top pressure.

3.11.4 Look-Up Table Description

There are no look-up tables for the cloud top temperature/pressure algorithm.

3.11.5 Parameterization

There are no parameterizations for the cloud top temperature/pressure algorithm.

3.12 Theoretical Description: Radiative Fluxes and Cloud Forcing

3.12.1 Physical and Mathematical Description

Upwelling and downwelling shortwave and longwave fluxes at the surface are computed with a neural network trained to simulate a radiative transfer model. The neural network, called FluxNet ([Key and Schweiger, 1998](#)), is also available as a stand-alone program. The radiative transfer model that FluxNet is trained to simulate is Streamer ([Key and Schweiger, 1998](#)). Relative differences between the neural network and the radiative transfer model for surface radiative fluxes are shown in Figure 15. Errors in top-of-atmosphere fluxes are similar. FluxNet is 100 to 10,000 times faster than Streamer, and is nearly as accurate. See the web pages at <http://stratus.ssec.wisc.edu> for more information.

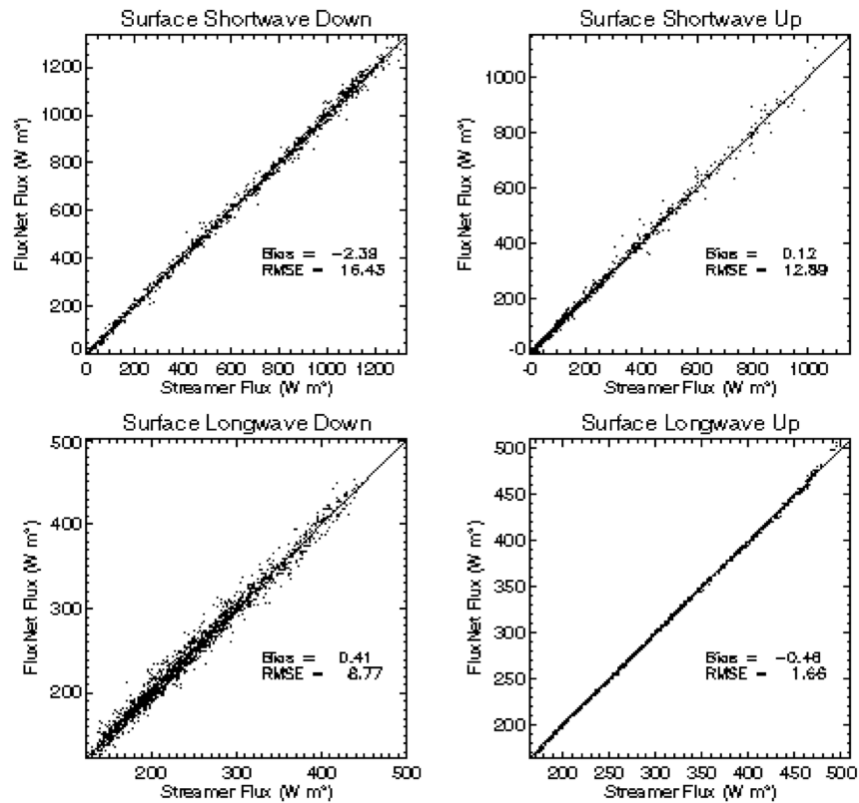


Figure 15. Comparison of FluxNet and Streamer fluxes for a wide range of atmospheric conditions.

The cloud radiative effect, more commonly called "cloud forcing", is computed from the net shortwave and longwave fluxes at the surface and TOA. It is defined as

$$CF_{\lambda, z} = \int_0^{A_c} \frac{\partial F_{\lambda, z}}{\partial a} da = F_{\lambda, z}(A_c) - F_{\lambda, z}(0) \quad 3.29$$

where $F_{\lambda, z}$ is the net flux (W m^{-2}) for shortwave or longwave radiation at the surface and A_c is the cloud fraction in the scene. The net flux is equal to the downwelling minus the upwelling fluxes. Because pixels are assumed to be either completely cloudy or completely clear, the right side of the equation is simply the net flux (shortwave or longwave) for a cloudy pixel minus the net flux if the pixel were clear. The clear sky net flux for cloudy pixels is calculated with FluxNet by simply setting the cloud fraction to zero and other cloud properties to values used in training FluxNet for clear sky conditions. Analogous to net radiation, the all-wave net cloud forcing can be calculated from

$$CF_z = CF_{shortwave} + CF_{longwave}$$

3.30

3.12.2 Numerical Strategy

Not applicable.

3.12.3 Calculations

The surface and cloud parameters described earlier in this document are input to FluxNet, which calculated the surface and TOA radiative fluxes and cloud radiative forcing. AVHRR channel information is not used.

3.12.4 Look-Up Table Description

There are no look-up tables for radiative flux retrieval.

3.12.5 Parameterization

There are no parameterizations for the radiative flux retrieval, other than the fact that FluxNet is itself a parameterization of a radiative transfer model.

4. Test Datasets and Outputs

4.1 Test Input Datasets

The primary input dataset for the generation of APP-x is APP. Two examples of APP are shown in Figures 16 and 17. APP is described in detail in a separate C-ATBD.

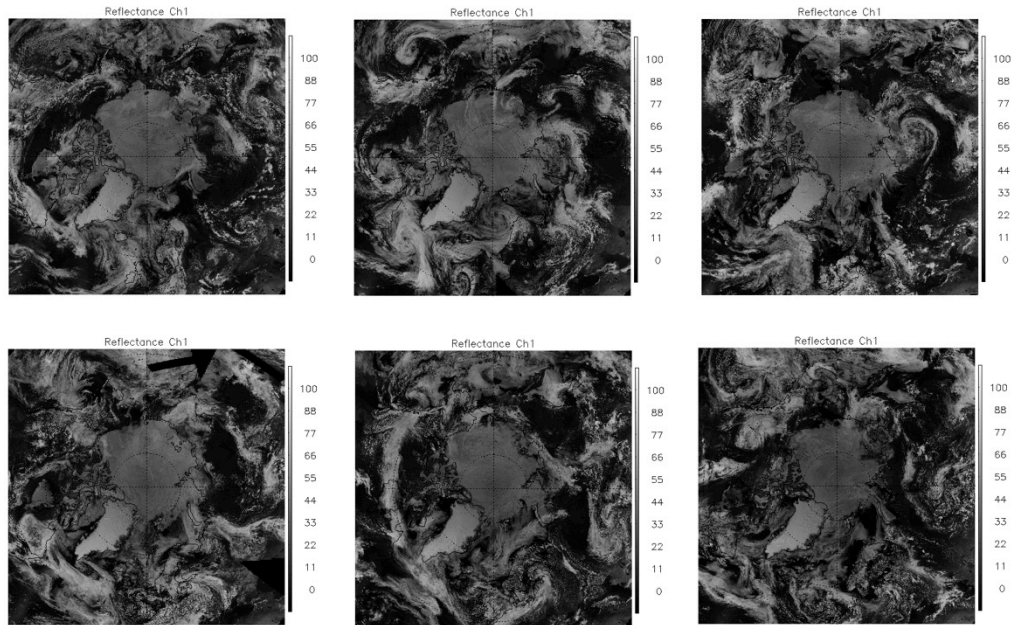


Figure 16: APP channel 1 reflectance (%) at 1400 SLT of north pole on July 1st of the year 1982, 1986, 1989, 1996, 2002, and 2007.

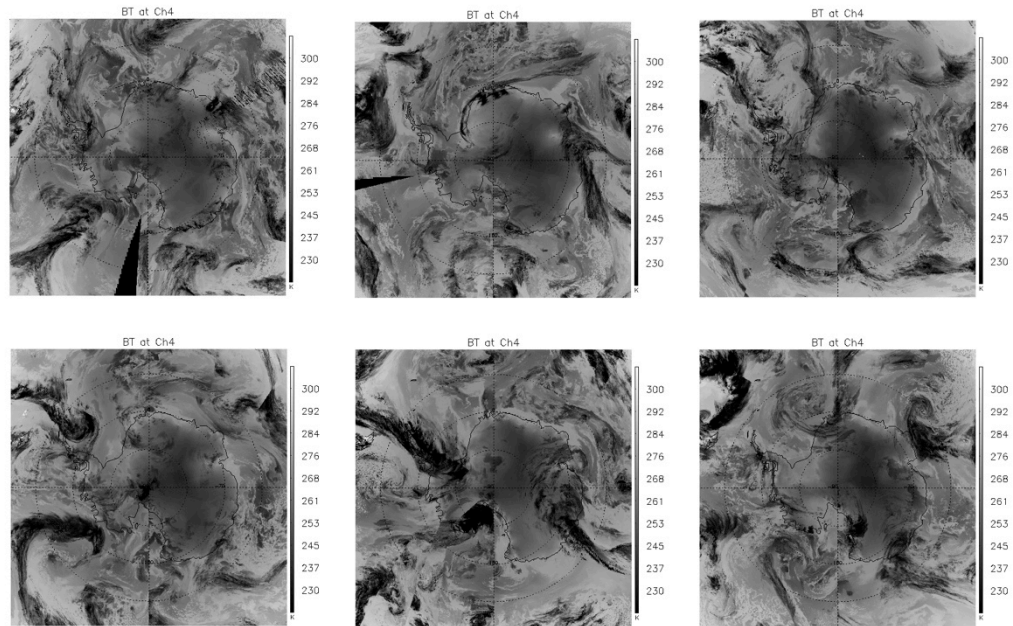


Figure 17: APP channel 4 BT (K) at 1400 SLT of south pole on January 1st of the year 1982, 1986, 1989, 1996, 2002, and 2007.

4.2 Test Output Analysis

4.2.1 Reproducibility

Reproducibility is monitored and ensured by three methods. Extraction of validation matchups during reprocessing, comparison to same day reference data from other resources like a Pan-Arctic Ice-Ocean Modeling and Assimilation System (PIOMAS) (Zhang and Rothrock, 2001, 2003) and CryoSat-2, and finally trend analysis of the product with time. An example is provided here only for sea ice thickness (SIT).

For each day or month, a vector of zonal averages of SIT data can be computed. When the SIT time series are complete, these vectors are assembled to construct a Hovmöller diagram to ensure consistency of the SIT CDR. At the end of a given processing run, a Hovmöller diagram is produced that allows trends in latitude and time to be analyzed.

4.2.2 Precision and Accuracy

To estimate the performance of the OTIM, we have used the comprehensive numerical model simulations, submarine and moored Upward Looking Sonar (ULS) measurements, and meteorological station measurements to assess and validate the OTIM. Figure 18 shows an example of OTIM retrieved sea ice thickness with APP-x data in comparison with PIOMAS simulated sea ice thickness for March 21, 2014.

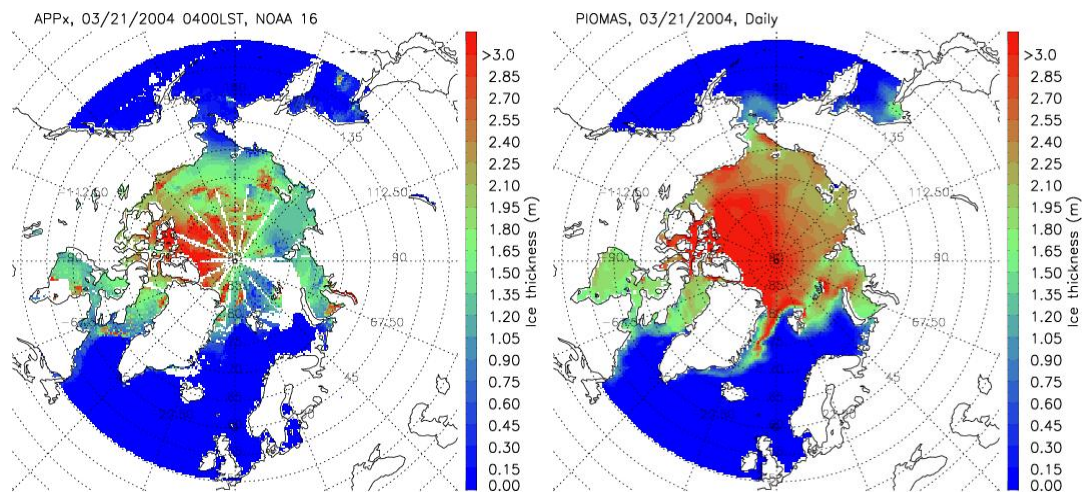


Figure 18. OTIM retrieved ice thickness with APP-x data and PIOMAS simulated ice thickness for March 21, 2004 under all-sky conditions. Additional details are given in Wang et al. (2010).

Table 10, 11, and 12 list the comparisons of OTIM retrieved sea ice thickness with submarine, mooring site, and station measurements, respectively, in terms of SIT mean, bias mean, bias absolute mean, bias standard deviation, and accuracy.

Table 10. OTIM validation results against submarine measurements made during Scientific Ice Expeditions (SCICEX-99) in 1999.

	OTIM	Submarine
Thickness Mean (m)	1.73	1.80
Bias Mean (m)	-0.07	
Bias Absolute Mean (m)	0.31	
Bias Standard Deviation	0.42	
Accuracy	83%	

Table 11. OTIM validation results against mooring measurements made from Beaufort Gyre Exploration Project (BGEP) over 2003-2004.

Mooring Location OTIM	Thickness mean (m)	Bias mean (m)	Bias absolute mean (m)
Site A (75°0.499'N, 149°58.660'W)	1.24	-0.02 (-1.2%)	0.19 (15.3%)
OTIM	1.22		
Site B (78°1.490'N, 149°49.203'W)	1.32	-0.15 (-11.4%)	0.29(21.9%)
OTIM	1.17		
Site C (76°59.232'N, 139°54.562'W)	1.32	-0.12 (-9.1%)	0.28 (21.2%)
OTIM	1.20		
ALL MOORING AVERAGE	1.29	-0.09 (-6.9%)	0.25 (19.4%)
OTIM AVERAGE	1.20		

Table 12. OTIM validation results against station measurements made at 8 Canadian meteorological stations starting from 2002 at the Canadian Ice Service (CIS)

OTIM Station Name	OTIM ALERT LT1	OTIM ALERT YLT	OTIM CAMBRIDGE BAY YCB	OTIM CORAL HARBOUR YZS	OTIM EUREKA WEU	OTIM HALL BEACH YUX	OTIM RESOLUTE YRB	OTIM YELLOWK NIFE YZF
Thickness Mean (m)	1.17 1.23	1.21 1.26	1.48 1.51	1.17 1.20	1.36 1.54	1.37 1.46	1.21 1.50	0.91 0.93
Bias Mean (m)	-0.06 (-4.8%)	-0.06 (-4.8%)	-0.04 (-2.6%)	-0.03 (-2.5%)	-0.18 (-11.7%)	-0.07 (-4.8%)	-0.29 (-19.3%)	-0.01 (-1.1%)
Bias absolute Mean (m)	0.14 (11.4%)	0.16 (12.7%)	0.58 (38.4%)	0.32 (26.7%)	0.27 (18.0%)	0.32 (32.0%)	0.31 (20.7%)	0.31 (33.3%)

4.2.3 Error Budget

The APP-x data set is created from APP data that is based on the AVHRR 5 channel data. The uncertainties in AVHRR channel data will inevitably propagate into the APP data set, and eventually affect APP-x data as well. Table 13 lists the estimated AVHRR 5 channel estimated uncertainties from different authors. [Brest and Rossow \(1997\)](#) estimated the uncertainties for AVHRR five channels for both visible and infrared channels.

Table 13. Relative uncertainties in AVHRR channels reported in the literature.

	Visible Channels (1, 2)	Thermal Channels (3, 4, 5)
Rao and Chen (1994, 1995, 1999)	0.7% (1), 1.5% (2)	---
Walton et al. (1998)	---	0.37 K, 0.15 K and 0.17 K.
Brest and Rossow (1997)	±3-5%	±1-2 K

Most of APP-x parameters were compared with field campaign and meteorological station measurements as shown in Table 14 that provide bias and uncertainty (root-mean-square error) for quantitative information of error budget.

Table 14. Biases and uncertainties (root-mean-square error) for APP-x variables.

<i>Quantity</i> [*]	<i>Bias</i> [#]	<i>RMSE</i> [§]
Surface temperature	0.20 K	1.98 K
Surface broadband albedo	-0.05 (absolute)	0.10 (absolute)
Downwelling shortwave radiation flux at the surface	9.8 W/m ²	34.4 W/m ²
Downwelling longwave radiation flux at the surface	2.1 W/m ²	22.4 W/m ²
Upwelling shortwave radiation flux at the surface	4.4 W/m ²	26.6 W/m ²
Upwelling longwave radiation flux at the surface	1.9 W/m ²	9.4 W/m ²
Cloud fraction	0.14 (absolute)	0.26 (absolute)

**: Satellite-derived quantities are for the 25 x 25 km² area centered on the SHEBA ship.*

#: Bias is defined as difference between satellite-derived quantities and SHEBA ship measurements. §: RMSE stands for Root Mean Square Error.

In estimating sea ice thickness using the OTIM, many factors affect the accuracy of ice thickness. The uncertainties from all of the input controlling variables in the OTIM will finally propagate into ice thickness through the ways of parameterizations and model algorithms. In the OTIM model we used parameterization schemes as described in previous sections to calculate radiative fluxes. Therefore in essence, ice thickness is the function of 12 controlling variables that are ice and snow broadband albedo (α_s), ice transmittance (i_0), surface downwelling shortwave radiation flux (F_r), surface skin and air temperatures (T_s , T_a), surface air pressure (P_a), surface air relative humidity (R), ice temperature (T_i), wind speed (U), cloud amount (C), snow depth (h_s), and residual heat flux (F_a).

$$\hat{h}_i = f(\hat{\alpha}_s, \hat{i}_0, \hat{F}_r, \hat{T}_s, \hat{T}_i, \hat{T}_a, \hat{P}_a, \hat{R}, \hat{U}, \hat{C}, \hat{h}_s, \hat{F}_a) \quad 4.1$$

where the variables with carets “^” stand for the variables with estimated values, other than the variables with “true” values. Then the partial derivative of ice thickness against each of the controlling variables can be used for the calculation of the sensitivity of the ice thickness to the error in the controlling variable. Tables 15 and 16 list the controlling variables used in ice thickness sensitivity study for daytime and nighttime cases with aforementioned uncertainties in controlling variables and their impacts for typical ice thickness of 1 meter.

Table 15. Sensitivity of ice thickness estimates to uncertainties in the controlling variables during daytime case with reference ice thickness of 1 meter.

Name	Ref. Value	Error (Dx)*	IceThk_Dh*	IceThk_Dh/h	IceThk_Dh/Dx
T_s (K)	253.23	+2.000 -2.000	-0.235 +0.245	-0.235 +0.245	-0.117 -0.122
T_i (K)	253.23	+5.000 -5.000	-0.008 +0.008	-0.008 +0.008	-0.002 -0.002
h_s (m)	0.20	+0.100 -0.100	-0.654 +0.654	-0.654 +0.654	-6.544 -6.544
R (%)	90.00	+9.000 -9.000	+0.024 -0.024	+0.024 -0.024	+0.003 +0.003
U (m/s)	5.00	+1.000 -1.000	+0.316 -0.208	+0.316 -0.208	+0.316 +0.208
P_a (hPa)	1000.00	+50.00 -50.00	+0.066 -0.063	+0.066 -0.063	+0.001 +0.001
α_s (0~1)	0.85	+0.100 -0.100	-0.757 +2.195	-0.757 +2.195	-7.566 -21.953
T_r (0~1)	0.05	+0.050 -0.050	-0.086 +0.092	-0.086 +0.092	-1.711 -1.848
F_r (w/m ²)	101.44	+20.288 -20.288	+0.395 -0.295	+0.395 -0.295	+0.019 +0.015
F_a (w/m ²)	0.00	+2.000 -2.000	-0.212 +0.260	-0.212 +0.260	-0.106 +0.130
C (0~1)	0.50	+0.250 -0.250	+0.297 -0.639	+0.297 -0.639	+1.189 +2.555

*: Dx stands for the uncertainty of the controlling variable, IceThk_Dh is the corresponding sea ice thickness uncertainty, and h is the reference sea ice thickness that is 1 m.

Table 16. Sensitivity of ice thickness estimates to uncertainties in the controlling variables during nighttime case with reference ice thickness of 1 meter.

<i>Name</i>	<i>Ref. Value</i>	<i>Error (Dx)</i>	<i>IceThk_Dh</i>	<i>IceThk_Dh/h</i>	<i>IceThk_Dh/Dx</i>
$T_s (K)$	241.09	+2.000 -2.000	-0.172 +0.179	-0.172 +0.179	-0.086 -0.090
$T_i (K)$	241.09	+5.000 -5.000	-0.008 +0.008	-0.008 +0.008	-0.002 -0.002
$h_s (m)$	0.20	+0.100 -0.100	-0.667 +0.667	-0.667 +0.667	-6.666 -6.666
$R (\%)$	90.00	+9.000 -9.000	+0.006 -0.006	+0.006 -0.006	+0.001 +0.001
$U (m/s)$	5.00	+1.000 -1.000	+0.166 -0.133	+0.166 -0.133	+0.166 +0.133
$P_a (hPa)$	1000.00	+50.00 -50.00	+0.043 -0.041	+0.043 -0.041	+0.001 +0.001
$F_a (w/m^2)$	0.00	+2.000 -2.000	-0.137 +0.155	-0.137 +0.155	-0.068 0.078
$C (0\sim 1)$	0.50	+0.250 -0.250	+0.248 -0.476	+0.248 -0.476	+0.992 +1.903

5. Practical Considerations

5.1 Numerical Computation Considerations

APP-x is implemented sequentially, as many there are a number of parameter dependencies. For example, the calculation of ice surface temperature requires a cloud mask, and the calculation of radiative fluxes and cloud forcing requires all cloud and surface properties (Figure 2).

The APP-x effective pixel size of 25 km, which is based on sampling the 5 km APP data rather than averaging, was chosen for computational reasons only. Generating a 5 km APP-x product is possible, but would be computationally time consuming.

5.2 Programming and Procedural Considerations

Not applicable.

5.3 Quality Assessment and Diagnostics

The following procedures are recommended for diagnosing the performance of the APP-x:

- Monitor the percentage of pixels retrieved for ice thickness, and check the value uniformity over the small and smooth area without cracks, melting ponds, and leads.

- Periodically image the individual test results to look for artifacts or non-physical behaviors.
- Maintain a close communication and/or collaboration with users using the sea ice thickness product in their studies.

5.4 Exception Handling

The APP-x processing includes checking the validity of input data (APP) before using it. The main processing system flags any pixels with missing geo-location or viewing geometry information, or out-of-range reflectances or brightness temperatures.

5.5 Algorithm Validation

In this section algorithm biases and uncertainties (root-mean-square differences) are estimated through comparisons of satellite retrievals and in situ measurements.

Surface Temperature

Comparisons with SHEBA surface observations were done by inverting measurements of the upwelling longwave flux to obtain temperature. Details are given in Key et al. (1997). An example of the comparison is shown in Figure 19. Results over all-sky conditions (i.e., clear and cloudy) yielded a bias (mean error) of -1.6 K and a root-mean-square-error (RMSE) of 6 K for the all-sky surface temperature. A negative bias indicates that the satellite retrieval is less than the surface observation. Comparisons to three International Arctic Buoy Program (IABP) buoys located from approximately 20 km to 450 km from the SHEBA icebreaker Des Groseilliers in April-July 1998 show that the AVHRR temperatures track the buoy temperatures quite well, with mean monthly differences typically less than 2 K. Retrievals for clear sky conditions have much smaller uncertainties than for all-sky conditions, on the order of 0.3 K for the bias and 1.9 K for the RMSE (Key et al., 1994).

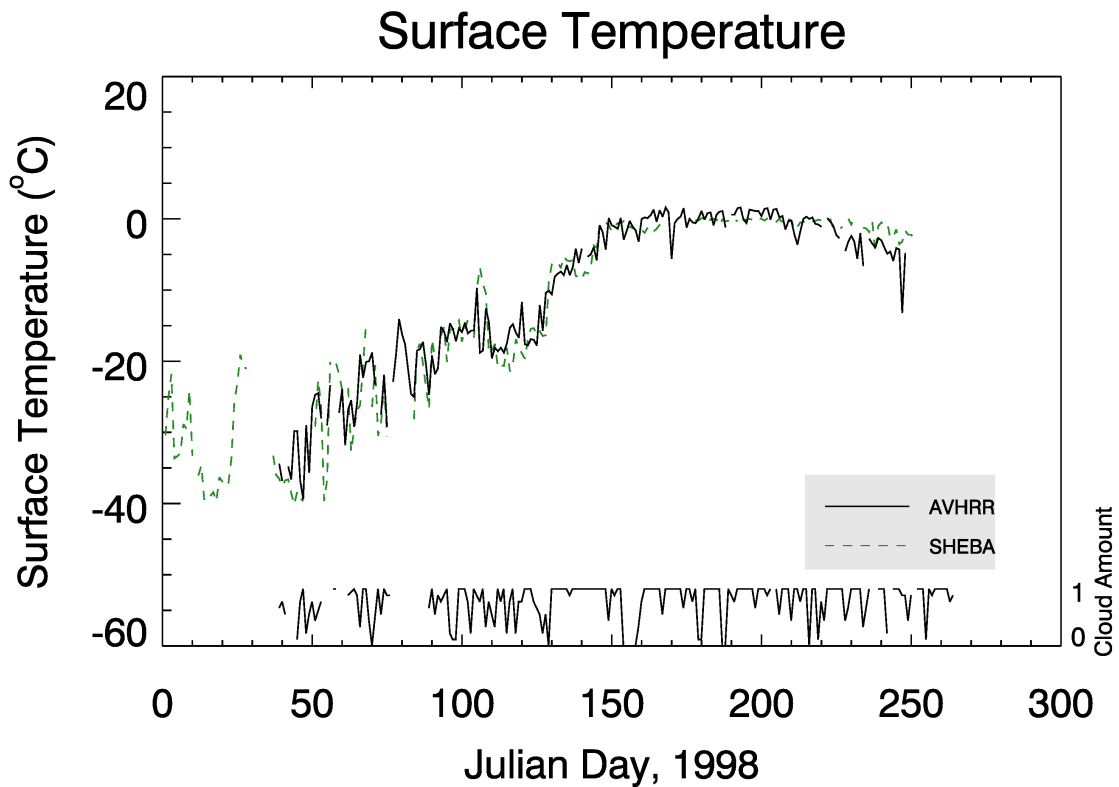


Figure 19. Comparison of satellite-derived and surface measurements of the surface skin temperature during SHEBA. Cloud amount is also shown.

Surface Albedo

Measurements of the upwelling and downwelling shortwave flux measured at the SHEBA camp were used to compute an all-sky albedo. Satellite-derived and surface measurements are shown in Figure 20. This comparison yields a bias on the order of 0.01 and a RMSE of 0.126 for the all-sky surface albedo. Retrievals for clear sky conditions have smaller uncertainties than for all-sky conditions.

The RMSE value is partially caused by spatial variability at the SHEBA site after JD 205. Ship sensors observed snowfall on JD 205-210, which increased local surface albedo, but did not significantly change albedo in the 25x25km area. The onset of freeze-up occurred on day 210, freezing the numerous melt ponds around the SHEBA site. The radiometers on the ship's instrument tower were likely sensitive to the heterogeneity in local surface types. The extent of melt ponds and open water around the observation site is visible in Figure 21.

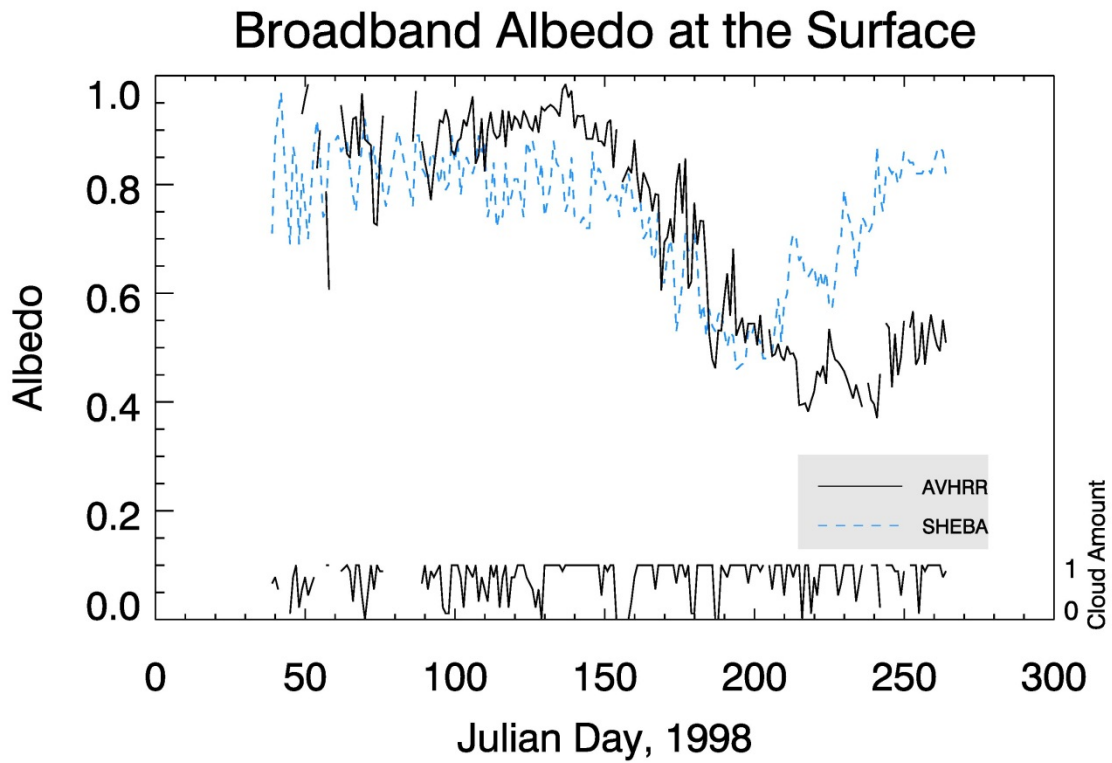


Figure 20. Comparison of satellite-derived and surface measurements of the surface broadband albedo during SHEBA. Cloud amount is also shown.

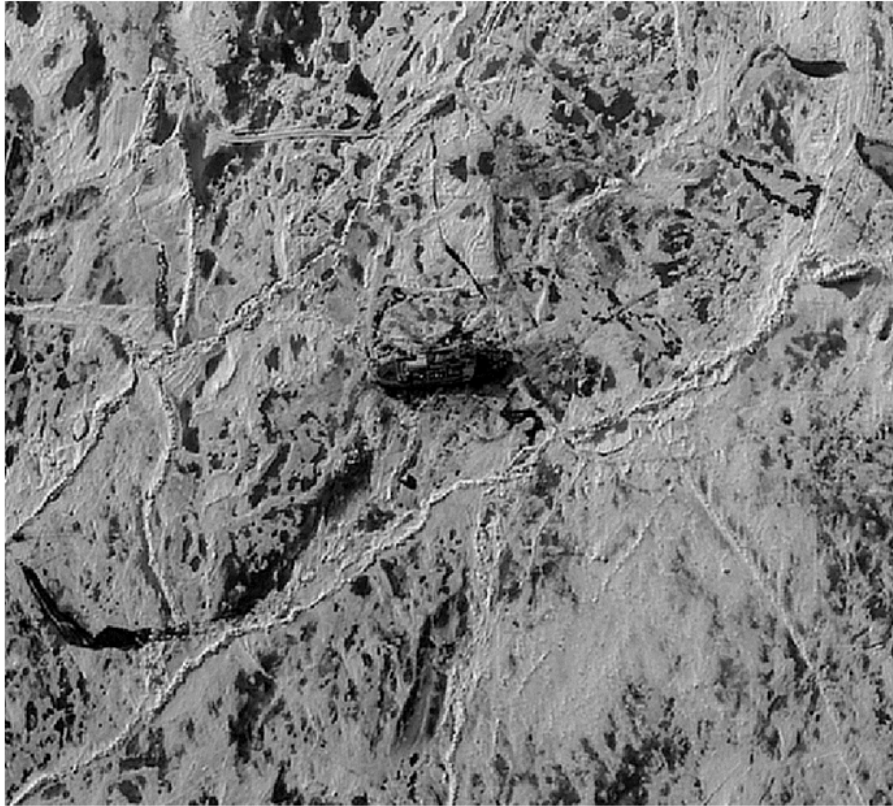


Figure 21. Close-up view of SHEBA measurement site on June 18, 1998. Melt ponds (dark areas) around the ship [center] still had over one month of melt season remaining.

Cloud Detection

Cloud amount at the SHEBA camp is based on three-hourly synoptic observations (human observer). Comparisons with satellite-derived cloud amount for 25 x 25 km area centered on the SHEBA ship (not shown) from September 1997 through August 1998 yield a bias of 0.1 and a RMSE of 0.3. Additional details are given in [Key et al. \(2001\)](#).

Cloud Particle Phase

The Depolarization and Backscatter Unattended Lidar (DABUL) instrument was deployed as part of SHEBA. Small raindrops, water cloud droplets, and fog are considered spherical and have depolarization ratios that theoretically approach 0. Non-spherical particles such as ice crystals and snowflakes contain a cross-polarized component produced by internal reflections and refractions and can exhibit depolarization ratios greater than 0.30. By data point inspection and comparisons with the microwave radiometer liquid water column

measurements, it was determined that DABUL depolarization values of less than 0.11 indicate liquid water phase.

Figure 22 gives a comparison of AVHRR-derived cloud phase and lidar depolarization ratio during the SHEBA year. The lidar results are for the highest altitude layer detected. Multilayer, multiphase cases were excluded from the analysis. The AVHRR results are for a 50 x 50 km area around the lidar location were used, but only for scenes with a cloud fraction of at least 0.6 (60%). The AVHRR phase labeling is zero for water and one for ice; intermediate values correspond to scenes with both phases present in varying proportions. The figure illustrates that for homogeneous scenes there is almost perfect agreement between the lidar and satellite determinations of phase; i.e., all cases labeled as water (ice) cloud by the AVHRR algorithms, day or night, are also labeled as water (ice) cloud by the lidar method. For the cases where the AVHRR algorithm found both phases present but more water than ice cloud - as indicated by an area average phase value less than 0.5 - the lidar cloud type was usually water. The results for the cases with more ice than water cloud show a similar pattern. Overall the satellite retrievals of cloud particle phase have an accuracy of approximately 95% (Key and Intrieri, 2000).

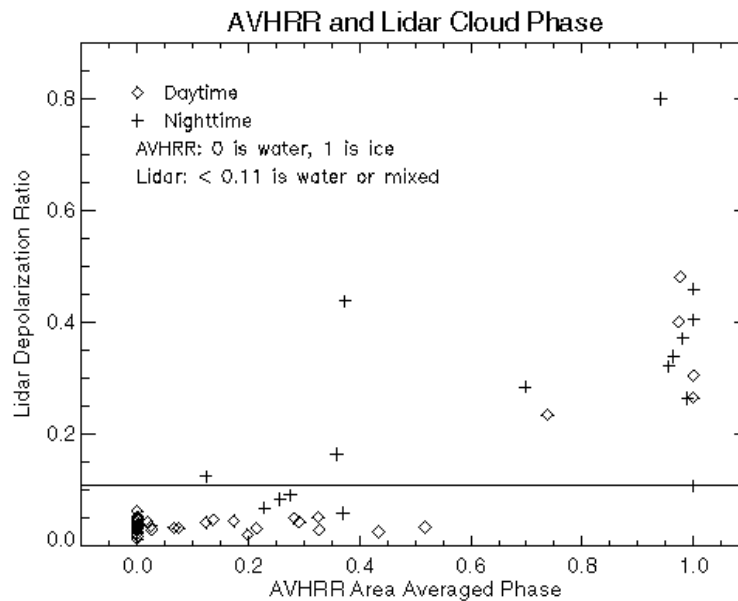


Figure 22. Cloud particle phase from the AVHRR and lidar depolarization ratio during the SHEBA year. Depolarization ratios less than 0.11 are primarily water or mixed-phase clouds. The AVHRR results use a value of zero for water and one for ice; intermediate values correspond to scenes with both phases present.

Cloud Optical Depth and Particle Size

Cloud optical depth and particle size retrievals have not been examined in detail due to the lack of in situ measurements. Some comparisons have been done with aircraft observations during SHEBA, particularly with the Canadian National Research Council (NRC) Convair.

The effective radius for water (liquid) clouds from the AVHRR were comparable to those measured by the Convair, typically within 1-2 μm for clouds with effective radii in the 8-10 μm range. For ice clouds the differences are larger, on the order of 10 μm for particles with effective “radii” in the range of 30-100 μm (Gultepe et al., 2003). Figure 23 provides one example from SHEBA.

Cloud Top Pressure

Cloud top pressure is currently being validated with SHEBA lidar and radar measurements. Figure 24 shows the monthly mean cloud top pressure estimated with data from the TIROS Operational Vertical Sounder (TOVS), the AVHRR, and surface-based lidar. The two satellite estimates are similar even though the retrieval methods are very different. The lidar estimate is considerably higher (estimated cloud top is at a lower altitude) during the summer, most likely because summertime clouds tend to be thicker on average, and the lidar cannot penetrate to the tops of clouds with optical thicknesses larger than approximately 3. It is difficult to provide an uncertainty with this limited comparison, but a value of 50-75 mb is probably reasonable.

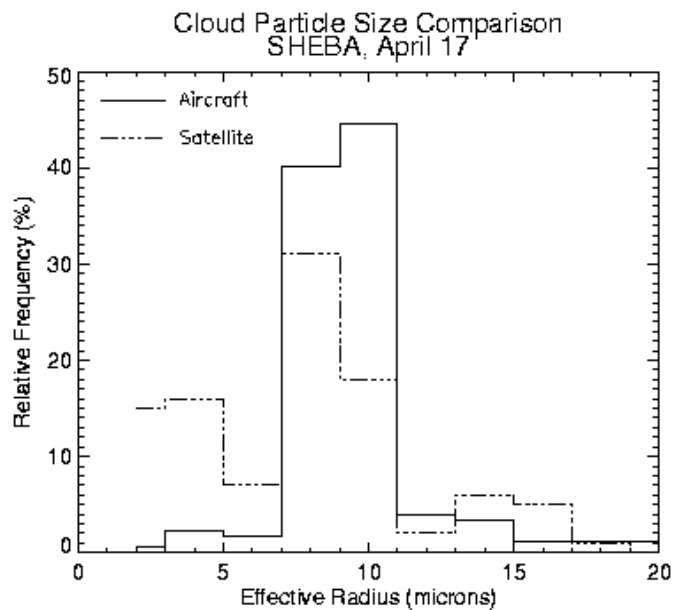


Figure 23. Relative frequency distribution of satellite-derived and aircraft measurements of liquid cloud particle effective radius for one case study from SHEBA.

**SHEBA: Monthly Mean Cloud Top Pressure from TOVS, Lidar and AVHRR (CASPR)
Average for 50 km radius around station**

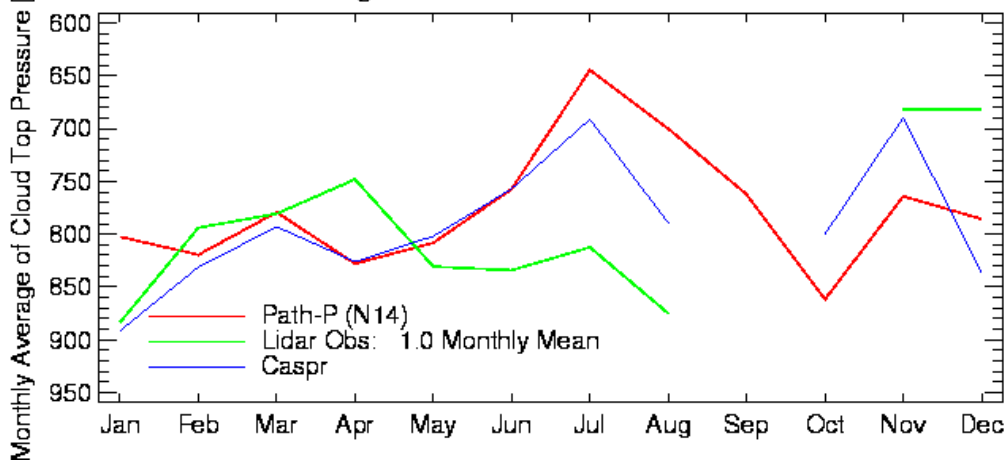


Figure 24. Monthly mean cloud top pressure from TOVS, AVHRR, and lidar during SHEBA.

Radiative Fluxes

Radiative fluxes are calculated with the neural network procedure called FluxNet. Root mean square differences between the neural network and the radiative transfer model for downwelling shortwave and longwave fluxes at the surface are on the order of 2-3% with biases near zero. Comparisons of instantaneous satellite-derived surface fluxes with SHEBA surface measurements yield a bias of 9.8 W m^{-2} and an RMSE of 34.4 W m^{-2} for downwelling shortwave radiation. For the downwelling longwave flux the bias and RMSE are 2.1 and 22 W m^{-2} , respectively. Figure 25 shows the results for SHEBA.

Comparisons of monthly mean values with measurements at Neumayer Station, Antarctica show differences of less than 10 W m^{-2} for the net shortwave flux and less than 8 W m^{-2} for the net longwave flux. For South Pole Station the longwave results are similar but the shortwave differences are somewhat higher. Figure 26 shows the results for Neumayer Station. See Pavolonis and Key (2003) for more information.

Key et al. (1997) address the combined uncertainties in satellite estimates of the surface radiation fluxes from a statistical perspective. The propagation of errors in the individual surface and cloud property retrievals is assessed as a function of the individual errors and the sensitivity of surface fluxes to changes in each variable. The method produced uncertainties in the range of $30\text{-}50 \text{ W m}^{-2}$ for the downwelling shortwave flux, $10\text{-}25 \text{ W m}^{-2}$ for the downwelling longwave flux, and $30\text{-}40 \text{ W m}^{-2}$ for the net flux.

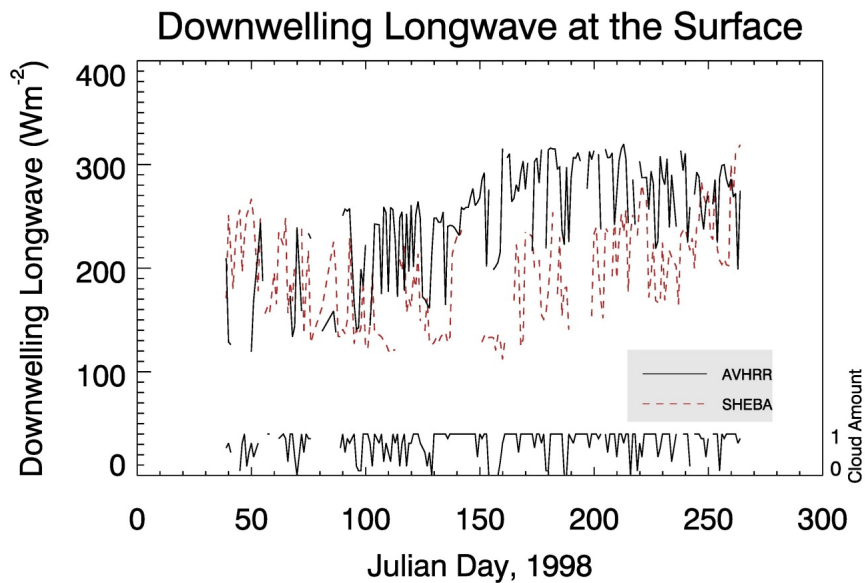
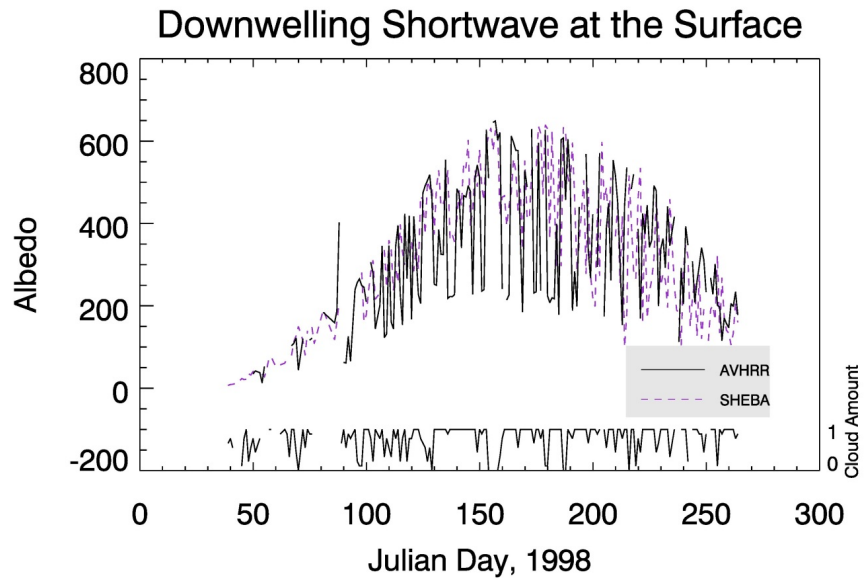


Figure 25. Comparison of satellite-derived and surface measurements of the downwelling shortwave flux at the surface (top) and the downwelling longwave flux at the surface (bottom). Cloud amount is also shown.

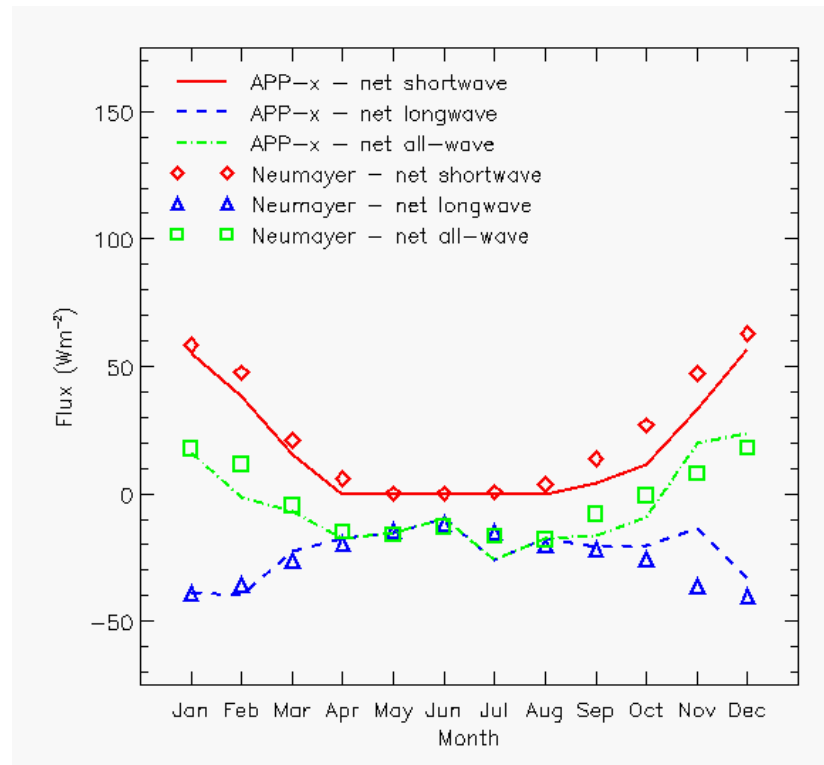


Figure 26. Comparison of monthly mean satellite-derived (APP-x) and surface measurements of the net radiative fluxes at Neumayer Station, Antarctic.

Day-Night Differences

Some algorithms use different spectral channels in the presence/absence of sunlight. Cloud detection, optical depth, effective radius, and particle phase all take advantage of reflective channels during the day. How consistent are the results for daytime and nighttime retrievals? Because these algorithms all use the AVHRR 3.7 μm channel in both day and night retrievals, a portion of the spectrum that includes both emitted thermal and reflected solar radiation, it is not possible to test the day-night differences simultaneously. Instead we provide the validation information detailed in the previous sections, and a few illustrations of retrievals for images that were part dark and part sunlit. Such comparisons are, of course, qualitative. Figure 27 shows retrievals for the cloud mask, cloud optical depth, particle effective radius, and particle phase for one winter day over the Arctic. The lower latitudes are sunlit; the area above approximately 80 degrees latitude is dark. There are no obvious day-night dependencies in the retrieval results.

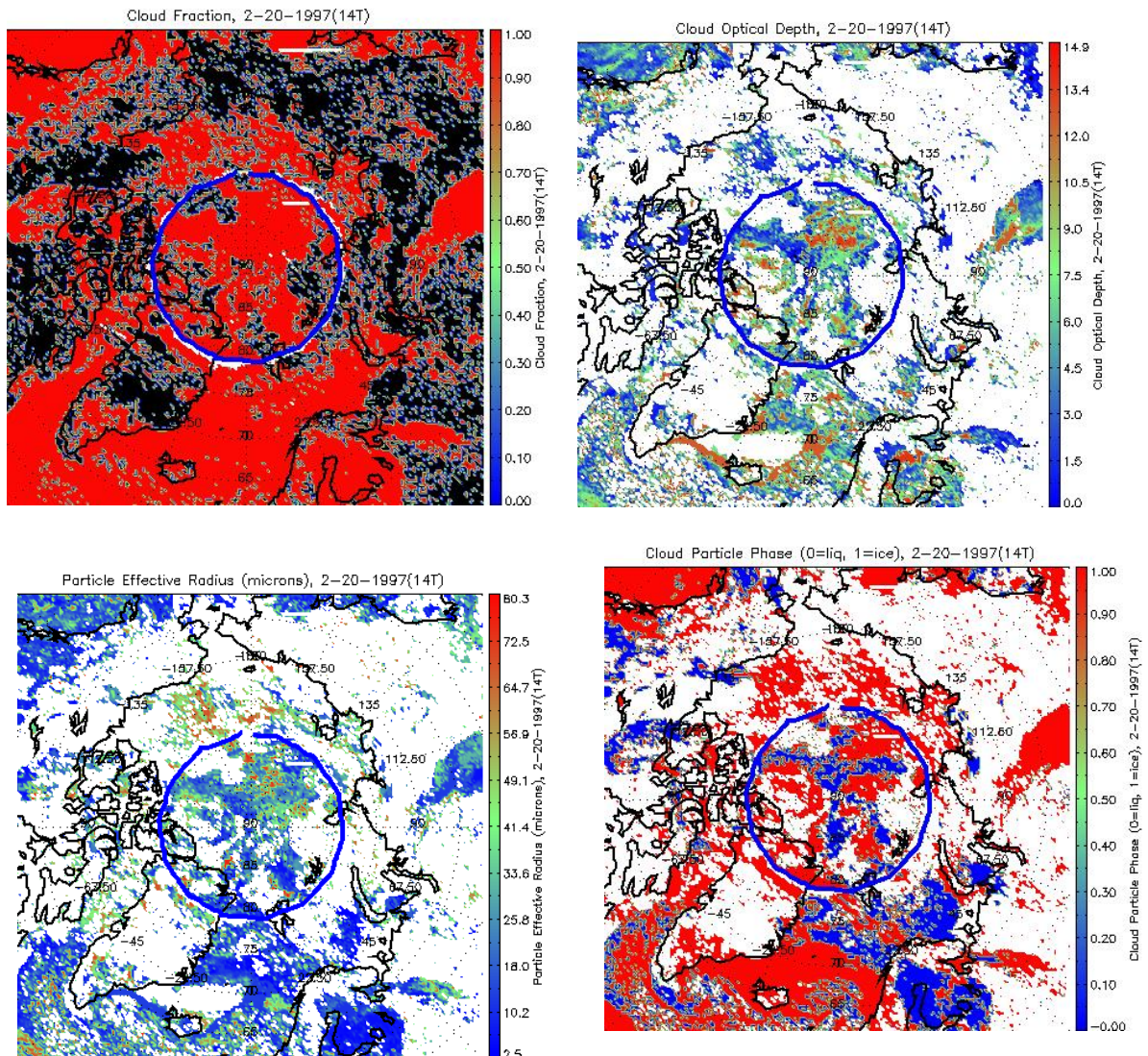


Figure 27. Retrievals for the cloud mask (upper left), visible cloud optical depth (upper right), particle effective radius (lower left), and particle phase (lower right) for one winter day over the Arctic. The lower latitudes are sunlit; the area above approximately 80 degrees latitude is dark, as denoted by the blue circle.

Validation is ongoing using data and methods such as those described above.

5.6 Processing Environment and Resources

The current computing environment is:

- Computer Hardware: MAC Pro 2 x 2.4 GHz Quad-Core Intel Xeon, 16GB memory
- Operating System: Mac OS X Lion 10.7.5
- Programming Language: IDL

- Compiler: IDL
- External Libraries: NetCDF 4.1.1
- Temporary Storage: ~500 GB for 33 years, uncompressed data for both Poles.

6. Assumptions and Limitations

6.1 Algorithm Performance

The following list contains the current assumptions and proposed mitigation strategies.

- Atmospheric profile and wind speed data are available from MERRA or other reanalysis data products. In case no profile data are available, it is assumed that surface air temperature is about 0.5 ~ 2 degree higher than ice/snow surface temperature depending on the cloud conditions (e.g., [Lindsay et al., 1997](#)), and relative humidity is about 90% over ice/snow, and wind speed of 5~10 m/s. But wind speed should be observed or simulated to guarantee to be realistic.
- Snow data including map and depth data need to be known beforehand. In case no snow data is available as it is now, general assumption of 20 cm snow depth will be used over ice.
- Land mask maps are also needed to identify different surface types.
- All of the static ancillary data is available at the pixel level.

6.2 Sensor Performance

We assume the AVHRR sensors will meet their performance specifications and hence the input APP product will be suitable for use in generating APP-x. Issues with sensor calibration, particularly the drift of calibration for the visible channels, is described in the APP C-ATBD.

7. Future Enhancements

Future enhancements include:

- Algorithm improvement, primarily for surface albedo, ice thickness, and cloud detection.
- Possibly increase the spatial resolution from 25 km to 5 km.

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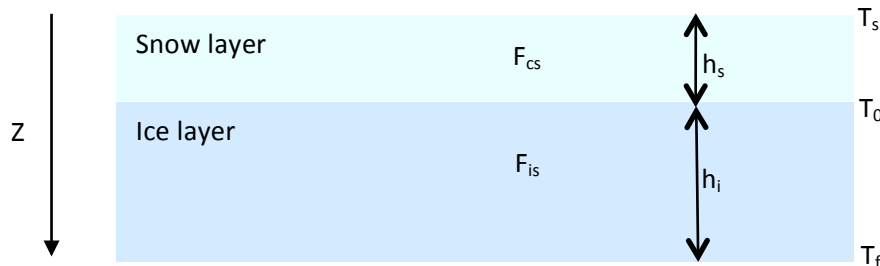
Appendix A. Acronyms and Abbreviations

Acronym or Abbreviation	Meaning
APP	AVHRR Polar Pathfinder
APP-x	eXtended AVHRR Polar Pathfinder (APP)
AVHRR	Advanced Very High Resolution Radiometer
BGEP	Beaufort Gyre Exploration Project
CASPR	Cloud And Surface Parameter Retrieval system
C-ATBD	Climate Algorithm Theoretical Basis Document
CDR	Climate Data Record
CIMSS	Cooperative Institute for Meteorological Satellite Studies
CIS	Canadian Ice Service
CSIM	Climate Sea Ice Model
CSM	Climate System Model
DABUL	Depolarization and Backscatter Unattended Lidar
DISORT	Discrete Ordinates Radiative Transfer
EASE	Equal-Area Scalable Earth
ECMWF	European Centre for Medium-Range Weather Forecasts
EUMETSAT	European Organisation for the Exploitation of Meteorological Satellites
ESA	European Space Agency
IDL	Interactive Data Language
MERRA	Modern Era Retrospective-analysis for Research and applications
MODIS	Moderate-resolution Imaging Spectroradiometer
MSG	Meteosat Second Generation
NASA	National Aeronautics and Space Administration
NCDC	National Climatic Data Center
NCEP	National Centers for Environmental Prediction
NESDIS	NOAA's Satellite and Information Service
NOAA	National Oceanic and Atmospheric Administration
PIOMAS	Pan-Arctic Ice-Ocean Modeling and Assimilation System
OTIM	One-Dimensional Thermodynamic Ice Model
SEVIRI	Spinning Enhanced Visible & InfraRed Imager
SIT	Sea Ice Thickness
STAR	The Center for Satellite Applications and Research

ULS	Upward Looking Sonar
UW-Madison	University of Wisconsin-Madison

Appendix B. Conductive heat flux for two-layer system with snow over ice

Consider a two-layer system, with a slab of ice overlaid by a layer of snow as shown below. We assume the temperature gradients in the snow and ice are each linear and thus conductive heat



flux is constant with depth. At the snow/ice interface, the conductive flux in the snow must equal the conductive flux in the ice, i.e., $F_{ci} = F_{cs}$. As we define the direction to the snow/ice is positive, so we can derive the conductive heat flux for the two-layer system with a snow layer overlaid a slab of ice as shown below. Downward direction is defined positive, so $F_c = k \cdot dT/dh$, where dT is temperature difference, and dh is the snow/ice thickness.

$F_c = k \frac{dT}{dZ}$, and so for the snow layer, we have $F_{cs} = k_s \frac{T_0 - T_s}{h_s}$, and the same for the ice slab,

$F_{ci} = k_s \frac{T_f - T_0}{h_i}$, so we have $k_s \frac{T_f - T_0}{h_i} = k_s \frac{T_0 - T_s}{h_s}$, after series of derivation, we finally get

$T_0 = \frac{k_s h_i T_s + k_i h_s T_f}{k_i h_s + k_s h_i}$, therefore $F_{cs} = \frac{k_i k_s}{k_i h_s + k_s h_i} (T_f - T_s)$, $F_c = F_{cs} = \frac{k_i k_s}{k_i h_s + k_s h_i} (T_f - T_s)$.