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CLOUD TOP PROPERTIES AND CLOUD PHASE  
ALGORITHM THEORETICAL BASIS DOCUMENT

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## 1.0 Introduction

Cloud top properties (height, temperature, and effective emissivity) will be generated using the CO<sub>2</sub> slicing algorithm that corrects for possible cloud semi-transparency. The MODIS infrared CO<sub>2</sub> channels will be used to investigate clouds at 5 km resolution and to generate a global cloud climatology at .5 degree resolution. Additionally, cloud phase will be obtained by MODIS 8, 11 and 12 micron brightness temperature differencing at 5 km resolution. This document describes both algorithms, details the MODIS applications, and sizes the possible errors. Several references are available for further reading; for cloud top properties they are

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## 2.0 Overview

Cirrus clouds are crucially important to global radiative processes and the heat balance of the Earth; they allow solar heating while reducing

infrared radiation to space. Models of climate changes will have to correctly simulate these clouds to have the proper radiative terms for the Earth's heat budget. Past estimates of the variation of cloud cover and the earth's outgoing longwave radiation have been derived primarily from the longwave infrared window (10-12 microns) radiances observed from polar orbiting and geostationary satellites (Rossow and Lacis, 1990; Gruber and Chen, 1988). The occurrence of semi-transparent clouds is often underestimated in these single channel approaches. Recently, multispectral techniques have been used to better detect cirrus in global (Wylie et al., 1993; Wu and Susskind, 1990) and North American (Wylie and Menzel, 1989) cloud studies.

Cloud phase also plays a role in regulating the earth's energy budget; ice and water clouds react differently to similar incident radiation. In the infrared window region, changes in microphysical properties from 8 to 11 microns and 11 to 12 microns allow three carefully chosen bands to differentiate cloud phase. Past infrared single band and bi-spectral split window cloud detection techniques (Booth, 1978; Inoue, 1987; Inoue, 1989) cannot fully take advantage of these properties; to date, no single operational satellite contains three bands these spectral ranges. Visible channel cloud phase detection techniques (Pilewskie and Twomey, 1987; King, 1992) exist, but cannot provide complete temporal coverage.

MODIS offers the opportunity to investigate seasonal and annual changes in the cirrus or semi-transparent global cloud cover and cloud phase with multispectral observations at high spatial resolution (one km rather than the current operational 20 km). Transmissive clouds that are partially transparent to terrestrial radiation can be separated from opaque clouds in the statistics of cloud cover (Wylie and Menzel, 1989). To date semi-transparent or cirrus clouds have been found in roughly 40% of all HIRS observations (Wylie et al., 1993).

### 3.0 Algorithm Description

The theoretical basis of the algorithms and practical considerations are contained in this section.

#### 3.1 Theoretical Description

This section will discuss the physics of deriving cloud height and amount, and cloud phase from multispectral infrared radiances from a given field of view, present the application with MODIS data, and estimate different sources of error.

##### 3.1.1.a Atmospheric Physics of Cloud Top Properties Algorithm

The CO<sub>2</sub> slicing technique is founded in the calculation of radiative transfer in an atmosphere with a single cloud layer. For a given cloud element in a field of view (FOV) the radiance observed,  $R(\nu)$ , in spectral band  $\nu$  can be written

$$R(\nu) = (1 - NE) R_{clr}(\nu) + NE * R_{bcd}(\nu, P_C) \quad (1)$$

where  $R_{clr}(\nu)$  is the corresponding clear sky radiance,  $R_{bcd}(\nu, P_C)$  is the corresponding radiance if the field of view were completely covered with an



opaque or "black" cloud at pressure level  $P_C$ ,  $n$  is the fraction of the field of view covered with cloud, and  $E$  is the cloud emissivity. It is apparent from this expression that for a given observed radiance, if the emissivity is overestimated, then the cloud top pressure is also (putting it too low in the atmosphere).

The opaque cloud radiance can be calculated

$$R_{bcd}(\nu, P_C) = R_{clr}(\nu) - \int_{P_C}^{P_S} t(\nu, p) \frac{dB[\nu, T(p)]}{dp} dp \quad (2)$$

where  $P_S$  the surface pressure,  $P_C$  the cloud pressure,  $t(\nu, p)$  the fractional transmittance of radiation of frequency  $\nu$  emitted from the atmospheric pressure level ( $p$ ) arriving at the top of the atmosphere ( $p = 0$ ), and  $B[\nu, T(p)]$  is the Planck radiance of frequency  $\nu$  for temperature  $T(p)$ . The second term on the right represents the decrease in radiation from clear conditions introduced by the opaque cloud.

Following the work of Smith and Platt (1978), to assign a cloud top pressure to a given cloud element, the ratio of the deviations in observed radiances,  $R(\nu)$ , and the corresponding clear air radiances,  $R_{clr}(\nu)$ , for two spectral channels of frequency  $\nu_1$  and  $\nu_2$  viewing the same FOV can be written as

$$\frac{R(\nu_1) - R_{clr}(\nu_1)}{R(\nu_2) - R_{clr}(\nu_2)} = \frac{NE_1 \int_{P_C}^{P_S} t(\nu_1, p) \frac{dB[\nu_1, T(p)]}{dp} dp}{NE_2 \int_{P_C}^{P_S} t(\nu_2, p) \frac{dB[\nu_2, T(p)]}{dp} dp} \quad (3)$$

If the frequencies are close enough together, then  $E_1$  approximates  $E_2$ , and one has an expression by which the pressure of the cloud within the FOV can be specified.

Once a cloud height has been determined, an effective cloud amount (also referred to as effective emissivity) can be evaluated from the infrared window channel data using the relation

$$NE = \frac{R(w) - R_{clr}(w)}{B[w, T(P_C)] - R_{clr}(w)} \quad (4)$$

Here  $N$  is the fractional cloud cover within the FOV,  $NE$  the effective cloud amount,  $w$  represents the window channel frequency, and  $B[w, T(P_C)]$  is the opaque cloud radiance.

Effective emissivity refers to the product of the fractional cloud cover,  $N$ , and the cloud emissivity,  $E$ , for each observational area (roughly 5 km by 5 km). When  $NE$  is less than unity, MODIS may be observing broken cloud ( $N < 1$ ,  $E = 1$ ), overcast transmissive cloud ( $N = 1$ ,  $E < 1$ ), or broken transmissive cloud ( $N < 1$ ,  $E < 1$ ). With a FOV of one kilometer, it is safe to assume that more

of the semi-transparency for a given field of view is due to cloud emissivity being less than one than due to the cloud not completely covering the field of view; for most synoptic regimes, especially in the tropics and subtropics, this assumption appears to be very reasonable.

### 3.1.1.b Atmospheric Physics of Cloud Phase Algorithm

The tri-spectral technique also has its roots in the calculation of radiative transfer in the atmosphere. Single scattering processes can also be parameterized in the cloud emissivity  $E(\lambda)$  in Equation (1) (Parol et al., 1991). The single scattering properties are defined by the index of refraction, the cloud particle size distribution and the particle shape distribution. This section discusses the underlying physical principles that determine the capabilities and channel bandwidths of the proposed tri-spectral technique.

Absorption and emission by clouds are dependent upon the index of refraction of the particle

$$m = n_r - n_i, \quad (5)$$

where  $n_r$ , the real portion, represents the magnitude of scattering by the particle, and  $n_i$ , the complex portion, is an indication of absorptive properties of the material. Figure 1 depicts the real and imaginary portions of the index of refraction (after Warren, 1984) over the atmospheric window for both ice and liquid water. Differences in the values of the indices for water versus ice will result in distinctive reactions to similar incident radiation.

Minimum values of the imaginary portion of the index of refraction occur from 8-10 microns indicating weaker particle absorption. The ice and water indices increase and diverge beyond this spectral region. Based solely on the imaginary indices of refraction, more absorption will take place in ice cloud between 10-12 microns than in water clouds of equal water content. This results in lower blackbody temperatures for ice than water clouds of similar height and thickness. Ackerman et al. (1990), noted that blackbody temperature decreases with increasing wavelength for thick cirrus between wavelengths of 10 and 12 microns. This is due to the increase in the absorption coefficient,

$$K(\lambda) = \frac{4\pi n_i}{\lambda} \quad (6)$$

whose shape closely resembles that of the imaginary index of refraction over this interval.

Cloud radiative processes are also dependent upon the size of particles in the cloud. Modeled results indicate single scattering processes closely match the general shape of the indices of refraction for ice and water until reaching a size of 30 microns (Strabala et al., 1994). Scattering processes are at a maximum from 8-9 microns and a minimum from 10.5-12 microns, however they are generally less important than absorptive properties in the window region.

Cloud particle shape investigations revealed no significant differences in the spectral signature of the single scattering properties between ice spheres and infinite cylinders. Takano et al. (1992) showed similar results using spheroidal and hexagonal particles; scattering was greater at 8 microns than at 11 or 12 microns.

In the absence of clouds, Equation (1) reverts to the standard clear sky form of the radiative transfer equation

$$R_{clr}(\lambda) = B(\lambda, T(p_s))t(\lambda, p_s) + \int_{p_s}^{p_0} B(\lambda, T(p)) \frac{dt(\lambda, p)}{dp} dp \quad (7)$$

Scattering is negligible in the infrared region for a clear atmosphere since the wavelengths are much greater than the size of air molecules. As a result, differences in brightness temperature can be related to the amount of transmission of energy in each layer.

Total transmittances of a standard atmosphere are computed using FASCOD2 for the 8-13 micron spectral region using data gathered from the High-spectral resolution Interferometer Sounder (HIS) (Smith et al., 1991) and the resultant spectra is depicted in Figure 2. From 8 to 12 microns, the transmittance is generally greater than .7, with most of the absorption due to water vapor molecules. In a clear atmosphere over a surface with an emissivity of 1, the 8 minus 11 micron brightness temperature difference will be near zero or negative due to the stronger water vapor absorption that occurs at 8 than 11 microns.

Combining the results of gaseous absorption with simulations of single scattering properties, regions of the infrared spectrum were selected that would be most useful for the detection of cloud.

In the 8-9 micron region, ice/water particle absorption is a minimum, while atmospheric water vapor absorption is moderate. In the 11-12 micron region, the opposite is true; particle absorption is maximum and atmospheric water vapor absorption is relatively small. Using bands in these two regions in tandem, cloud properties can be distinguished. Large positive brightness temperature differences of 8 minus 11 microns indicate the presence of cirrus clouds. This is due to the larger increase in the imaginary index of refraction of ice over that of water. For clear conditions, the 8 minus 11 micron brightness temperature difference will be small or even negative due to stronger atmospheric water vapor absorption at 8 microns than 11 microns. A third band in the 12 micron region will enable cloud phase delineation. Water particle absorption increases more between 11 and 12 microns than between 8 and 11 microns, while the increase of ice particle absorption is greater between 8 and 11 microns than between 11 and 12 microns. Thus, the 11 minus 12 micron brightness temperature differences of water clouds are greater than the 8 minus 11 micron differences. Conversely, 8 minus 11 micron brightness temperature differences of an ice cloud scene are greater than coincident 11 minus 12 micron differences. Therefore, ice and water clouds will separate in a scatter diagram of 8 minus 11 micron versus 11 minus 12 micron brightness temperature differences, with ice cloud scenes lying above the unity slope and

water clouds below. Mixed phase or partial radiometer filled ice over water clouds will exhibit characteristics of both ice and water clouds in this format, grouping near the unity slope.

### 3.1.2.a Mathematical Application of Cloud Top Properties Algorithm

The MODIS radiometer senses infrared radiation in seventeen spectral bands that lie between 3.75 and 14.24 microns at 1 km resolution (depending upon viewing angle) in addition to visible reflections at the same or better resolution. The four channels in the CO<sub>2</sub> absorption band (13.34, 13.64, 13.94, 14.24 microns) are used to differentiate cloud altitudes and the longwave infrared window channel (11.03 microns) identifies the effective emissivity of the cloud in the MODIS field of view (FOV). Figure 3 indicates the weighting functions for the CO<sub>2</sub> absorption channels on MODIS.

The left side of Equation (3) is determined from the satellite observed radiances in a given FOV and the clear air radiances inferred from spatial analyses of satellite clear radiance observations. Equation (3) can only be solved for a portion of the atmosphere where there is a one to one relationship between temperature and pressure. The right side of Equation (3) is calculated from a temperature profile and the profiles of atmospheric transmittance for the spectral channels as a function of  $P_C$ , the cloud top pressure (the integration through the atmosphere is accomplished at discrete 50 mb intervals). It is anticipated that global analyses of temperature and moisture fields from the National Meteorological Center (NMC) will be used to define the initial fields of temperature and moisture. The left side of Equation (3) is determined from the MODIS measured radiances in a given FOV and the clear air radiances inferred from spatial analyses of satellite clear radiance observations. The  $P_C$  that best matches measured and calculated ratios is the desired solution; the search is restricted between the surface pressure (or the top of the inversion layer) and the tropopause.

Using the ratios of radiances of the three CO<sub>2</sub> spectral channels, five separate cloud top pressures can be determined (14.24/13.94, 13.94/13.64, 13.94/13.34, 13.64/13.34, and 13.34/11.03). Whenever  $(R-R_{clr})$  is within the noise response of the instrument (conservatively estimated at roughly .5 mW/m<sup>2</sup>/ster/cm-1), the resulting  $P_C$  is rejected. Using the infrared window and the five cloud top pressures, as many as five effective cloud amount determinations can also be made using Equation (4). As described by Menzel (1983), the most representative cloud height and amount are those that best satisfy the radiative transfer equation for the four CO<sub>2</sub> channels and the infrared window.

Once  $P_C$  is determined, then NE is solved using the infrared window channel radiance observations and Equation (4). The cloud top temperature is also readily inferred from a representative temperature profile.

If no ratio of radiances can be reliably calculated because  $(R-R_{clr})$  is within the instrument noise level, then a cloud top pressure is calculated directly from the comparison of the MODIS observed 11.03 micron infrared window channel brightness temperature with an in situ temperature profile and the effective emissivity (NE) is assumed to be unity. In this way, all clouds are assigned a cloud top pressure either by CO<sub>2</sub> or infrared window calculations. Very thin high cloud are sometimes mistaken for low level

opaque clouds; Wylie and Menzel (1989) found that this occurred for about half of the very thin clouds with NE less than 10%.

Fields of view are determined to be clear or cloudy through inspection of the 11.03 micron brightness temperature with an 8.55 or 12.02 micron channel correction for moisture absorption. The channel brightness temperature differences (11.03 - 8.55 micron and 11.03 - 12.02 micron) are used to lower the 11.03 micron brightness temperature threshold for clear-cloudy decisions in areas where water vapor affects the window channel. This threshold change can vary from 0 C near the poles in dry air masses to as high as 7 C in the moist tropical atmospheres. If the moisture corrected 11.03 micron brightness temperature is within 2 degrees Kelvin of the known surface temperature (over land this is inferred from the NMC Medium Range Forecast (MRF) model analysis; over the oceans this is the NMC sea surface temperature analysis), then the FOV is assumed to be clear ( $P_C = 1000$  mb) and no cloud parameters are calculated.

The calibrated and navigated MODIS data will be processed for 5 km by 5 km areas. The data also will be corrected for zenith angle, to minimize any problems caused by the increased path length through the atmosphere of radiation upwelling to the satellite. Global coverage is expected every two days with one satellite.

Morning orbits over land must be rejected if the surface temperature analysis over subtropical deserts is warmer than the cloud cleared MODIS data; this causes cloud free areas to be mistaken as clouds. However, morning orbits over the oceans can be used because no diurnal temperature change of the surface is assumed.

In the Arctic and Antarctic, the MODIS channels will be inspected for the presence of surface temperature inversions. Over high altitude areas of Antarctica and Greenland, the MODIS 700 mb channel is often warmer than the window channel. We assume that this indicates the presence of surface inversions from radiative cooling under clear skies. Surface inversions normally can not be seen by the MODIS because the 700 mb and window channels are looking at two distinctly different levels of the troposphere which have large temperature differences due to the prevailing lapse rates. However, over polar high altitude continents, the surface is closer to 700 mb and the inversions can be detected. When the 700 mb channel is warmer than the window channel, the observation is classified as cloud free. When isothermal conditions are found and the 700 mb channel is within 2 K of the window channel, we assume that both channels see the top of a cloud and the observation is classified as cloudy.

#### 3.1.2.b Mathematical Application of Cloud Phase Algorithm

The essence of the tri-spectral method consists of interpreting a scatter diagram of 8 minus 11 micron versus 11 minus 12 micron brightness temperature differences, as from the 5 December 1991 MODIS Airborne Simulator (MAS) FIRE flight over the Gulf of Mexico (Figure 4). The 50 m visible channel (.68 micron) and the 11 micron 10 x 10 pixel averaged channel image are shown in Figure 5. The images are divided into smaller sub scenes according to cloud type.

The clear region is identified by near zero or negative values of 8 minus 11 micron and small 11 minus 12 micron differences (Figure 6, scene 1). The magnitude of these differences depend upon the total column water vapor amount. Water and ice cloud separate in distinct clusters with transmissive ice clouds grouped along a slope greater than one (Figure 6, scene 2) and water cloud less than one (Figure 6, scenes 4 and 5). Mixed phase cloud, or mixed cloud scenes, are identified by values in between, near the slope of unity (Figure 6, scene 6). Ice and water cloud with emissivities less than one are discerned by large positive values; large 8 minus 11 micron differences for ice cloud (Figure 6, scene 2 top pixels) and large 11 minus 12 micron differences for water cloud (Figure 6, scene 5). High emissivity cloud exhibit small values for both brightness temperature differences (Figure 6, scenes 3 and 4); most water vapor is trapped below an opaque cloud, creating a black cloud scene, where the same cloud temperature is sensed by all three channels.

The MODIS 8.55, 11.03 and 12.02 micron bands will be used to determine cloud phase over a 5 km x 5 km area. The brightness temperature for each band for a given FOV will be averaged over each 5 km by 5 km box. In turn, the standard deviation of the 8 micron radiance for each 5 x 5 km box will be evaluated, to determine scene uniformity; which aids in clear sky and opaque cloud determinations. The 8 micron channel is used with MAS data, however the 11 micron MODIS channel may be a better choice because it will also be evaluated for use with other techniques. A series of these boxes spanning a 2 degree x 2 degree latitude area will be combined for one 8 minus 11 micron versus 11 minus 12 micron brightness temperature difference scatter diagram. This scatter diagram will contain around 1600 averaged scenes from which a series of thresholds, or maximum likelihood estimator (MLE), will be used to determine cloud phase. An outline of the technique applied to MAS data is shown in Table 1.

Clear and opaque cloud are distinguished from mixed and thin cloud by an 8 micron radiance standard deviation threshold of 0.5 mW/m<sup>2</sup>/ster/cm-1. Clear is then further defined by 8 minus 11 micron brightness temperature differences less than .5 K and 11 minus 12 micron differences less than 2.4 K with a further requirement that 11 micron brightness temperatures be greater than 277 K. The thresholds were formed after examining differing MAS cloud scenes over a warm water background. If the clear requirements are not met, 11 micron brightness temperature are used to discern thick water from thick ice cloud. The ice/water cloud division line in the brightness temperature difference scatter diagram will lie near the unity slope. Mixed phase cloud will exhibit characteristics of both ice and water clouds, with points falling near this line. Once the 8 micron radiance standard deviation surpasses the threshold of uniformity, points falling within .3 K of this line, and greater than an 8 minus 11 micron brightness temperature difference of 1.25 K, are identified as mixed phase cloud.

Lastly, pixels not meeting the mixed cloud scene requirements are identified as thin ice cloud if the difference between the 8 minus 11 micron versus the 11 minus 12 micron brightness temperature difference is greater than .3 K (above the unity slope on the scatter diagram), or non-opaque water cloud if the difference is less than .3 K (below the unity slope).



Table 1. Thresholds of the tri-spectral technique as applied to 10x10 pixel MAS 50 m pixel areas, where SD is the Standard Deviation, BT is the Brightness Temperature, BTDIF is the Brightness Temperature Difference and ABS is the Absolute Value.

Tri-Spectral Technique
<p>Clear over water (code 0)</p> <ul style="list-style-type: none"> <li>if <math>8\mu\text{m}</math> radiance SD <math>&lt; .5</math> and</li> <li>if <math>8-11\mu\text{m}</math> BTDIF <math>&lt; .5</math> and</li> <li>if <math>11-12\mu\text{m}</math> BTDIF <math>&lt; 2.4</math> and</li> <li>if <math>11\mu\text{m}</math> BT <math>&gt; 277</math> K</li> </ul>
<p>Water cloud with emissivity near one (code 1)</p> <ul style="list-style-type: none"> <li>if <math>8\mu\text{m}</math> radiance SD <math>&lt; .5</math> and</li> <li>if clear <math>8-11\mu\text{m}</math> threshold not met and</li> <li>if <math>11-12\mu\text{m}</math> BTDIF threshold not met and</li> <li>if <math>260</math> K <math>&lt; 11\mu\text{m}</math> BT <math>&lt; 280</math> K</li> </ul>
<p>Ice cloud with emissivity near one (code 2)</p> <ul style="list-style-type: none"> <li>if <math>8\mu\text{m}</math> radiance SD <math>&lt; .5</math> and</li> <li>if clear <math>8-11\mu\text{m}</math> threshold not met and</li> <li>if <math>11-12\mu\text{m}</math> BTDIF threshold not met and</li> <li>if <math>11\mu\text{m}</math> BT <math>&lt; 260</math> K</li> </ul>
<p>Mixed phase cloud (code 3)</p> <ul style="list-style-type: none"> <li>if <math>8\mu\text{m}</math> radiance SD <math>&gt; .5</math> and</li> <li>if <math>8-11\mu\text{m}</math> BTDIF <math>&gt; 1.25</math> and</li> <li>if the ABS of <math>8-11\mu\text{m}</math> BTDIF minus <math>11-12\mu\text{m}</math> BTDIF <math>&lt; .3</math></li> </ul>
<p>Ice cloud with emissivity less than one (code 4)</p> <ul style="list-style-type: none"> <li>if <math>8\mu\text{m}</math> radiance SD <math>&gt; .5</math> and</li> <li>if <math>8-11\mu\text{m}</math> BTDIF minus <math>11-12\mu\text{m}</math> BTDIF <math>&gt; .3</math></li> </ul>
<p>Water cloud with emissivity less than one (code 5)</p> <ul style="list-style-type: none"> <li>if <math>8\mu\text{m}</math> radiance SD <math>&gt; .50</math> and</li> <li>if <math>8-11\mu\text{m}</math> BTDIF minus <math>11-12\mu\text{m}</math> BTDIF <math>&lt; .3</math></li> </ul>

### 3.1.3.a Estimate of Errors of Cloud Top Properties Algorithm

In the study of Wylie and Menzel (1989), the CO<sub>2</sub> cloud heights derived from VAS (VISSR Atmospheric Sounder) data over North America were found to be of good quality when compared to three other independent sources of cloud height information. Results showed: (a) for about thirty different clouds, the CO<sub>2</sub> heights were within 40 mb rms of cloud heights inferred from radiosonde moisture profiles; (b) in 100 comparisons with lidar scans of clouds, the CO<sub>2</sub> heights were 70 mb lower on the average and were within 80 mb rms; (c) satellite stereo parallax measurements in 100 clouds compared to within 40 mb rms. The CO<sub>2</sub> heights appeared to be consistent with other measurements within 50 mb and the effective fractional cloud cover within 0.20 in most cloud types.

#### 3.1.3.a.1 Errors Associated with the Assumption of Constant Emissivity

Spectrally close channels are used to minimize differences in the real and imaginary parts of the index of refraction for ice crystals and water droplets. Calculations by Jacobowitz (1970) indicate that negligible errors occur for the CO<sub>2</sub> channels between 13.3 and 14.2 microns for water and/or ice cloud determinations. This is not a source of error in the VAS cloud property calculations.

#### 3.1.3.a.2 Errors Associated with the Assumption of a Thin Cloud Layer

The CO<sub>2</sub> slicing algorithm assumes that all of the radiative effects of the cloud occur in the top thin layer. This makes the mathematics tractable. If the radiative transfer integral of Equation (3) were to include a cloud term where the cloud has finite depth, then a knowledge of the vertical structure of the cloud would be required. There are an infinite variety of combinations of cloud depths and vertical combinations that could produce the same integrated radiative signature; a unique solution is not possible. Any initial assumption of cloud structure biases the cloud top and bottom solution derived in the radiative transfer formulation.

The thin layer cloud approximation is investigated in Smith and Platt (1978). They found that errors in the height assignment approaching one-half (one-quarter) the thickness of the cloud were introduced for optically thin (thick) clouds where the integrated emissivity is less than (greater than) .6. The largest errors will be associated with physically thick but optically thin cirrus clouds. For optically thin (very transparent) cirrus with 100 mb depth the error in the height estimate is roughly 50 mb.

Wielicki and Coakley (1981) also discussed the consequences of the thin layer cloud approximation. They concluded that the algorithm solution ( $P_C$ ) would be near the center of the cloud for thin clouds and near the top of the cloud for dense clouds. For an optically thick cloud, the equation would obviously yield the cloud top. But for an optically thin cloud, the radiative effects of the cloud are forced into one layer. This is similar to a center of mass concept. The algorithm solution will thus be close to the "radiative center" of the cloud. Thus,  $P_C$  is somewhere between the cloud top and its center varying with the density of the cloud.



Cirrus height errors are also discussed in Wylie and Menzel (1989) where comparisons were made to cloud tops measured by lidars and by the stereo parallax observed from the images of two satellites at two different viewing angles. In the lidar comparison, the VAS inferred cloud top pressure over an observation area was compared to the highest lidar observation in the same area; these clouds had to be radiatively thin for the lidars to see through to the tops. Definition of a single cloud top was often difficult within a cloud layer; the lidar heights varied considerably (by more than 50 mb) from one cloud element to another in the same cloud layer. On the average, the VAS  $P_C$  was found to be 70 mb larger (lower cloud altitude) than the tops seen on the lidars. The CO<sub>2</sub> slicing technique was sensing the mean height; the VAS heights were comparable to the lidar top heights to within half the cloud thickness. In the comparisons to stereo parallax measurements for thin transmissive clouds, the VAS heights showed little bias. It was often difficult to measure parallax for thin transmissive clouds, as they appeared fuzzy with poorly defined boundaries in the images. Since the image of the clouds is more indicative of the center of the diffuse cloud mass than its outer boundaries, the parallax method is also sensitive to the radiative center of mass rather than the physical tops of these clouds. Thus, in these intercomparisons of actual measurements, the CO<sub>2</sub> cloud top pressures were found to be within the accuracy suggested by theoretical considerations.

### 3.1.3.a.3 Errors Associated with the Presence of a Lower Cloud Layer

The algorithm assumes that there is only one cloud layer. However, for over 50% of satellite reports of upper tropospheric opaque cloud, the ground observer indicates additional cloud layers below (Menzel and Strabala, 1989). To understand the effects of lower cloud layers, consider the radiation sensed in a cloudy field of view. For a semi-transparent or cirrus cloud layer, the radiation reaching the satellite,  $R$ , is given by

$$R = R_a + E \cdot R_C + (1-E) \cdot R_b \quad (8)$$

where  $R_a$  is the radiation coming from above the cloud,  $R_C$  is the radiation coming from the cloud itself,  $R_b$  is the radiation coming from below the cloud, and  $E$  is the cloud emissivity. When a lower cloud layer is present under the semi-transparent or cirrus cloud,  $R_b$  is smaller (i.e., some of the warmer surface is obscured by the colder cloud). If prime indicates a two layer cloud situation of high semi-transparent cloud over lower cloud, and no prime indicates the single layer high semi-transparent cloud, then

$$R_b' < R_b, \quad (9)$$

which implies

$$R' < R. \quad (10)$$

Thus the difference of cloud and clear radiance is greater for the two layer situation,

$$[R_{clr} - R'] > [R_{clr} - R]. \quad (11)$$

The effect of two cloud layers is greater for the 13.3 micron channel than for the other CO<sub>2</sub> micron channels, because the 13.3 micron channel "sees"

lower into the atmosphere (Figure 3 shows the weighting functions where the 13.3 peaks lower in the atmosphere than the other CO<sub>2</sub> channels). So using the 13.9/13.3 ratio as an example

$$[R_{\text{clr}}(13.3) - R'(13.3)] > [R_{\text{clr}}(13.9) - R'(13.9)]. \quad (12)$$

This reduces the ratio of the clear minus cloud radiance deviation in Equation (3) because the denominator is affected more than the numerator (when the less transmissive channel is in the numerator),

$$\frac{[R_{\text{clr}}(13.9) - R'(13.9)]}{[R_{\text{clr}}(13.3) - R'(13.3)]} < \frac{[R_{\text{clr}}(13.9) - R(13.9)]}{[R_{\text{clr}}(13.3) - R(13.3)]}, \quad (13)$$

or  $\text{Left}' < \text{Left}$ , where  $\text{Left}$  refers to the left side of Equation (3). An example plot of  $P_c$  versus  $\text{Right}$  (where  $\text{Right}$  refers to the right side of Equation (3)), shown in Figure 7, indicates that  $\text{Left}' < \text{Left}$  implies  $P_c' > P_c$ . Thus, when calculating a cloud pressure for the upper semi-transparent cloud layer in a two cloud layer situation, the CO<sub>2</sub> slicing algorithm places the upper cloud layer too low in the atmosphere.

An example from 25 October 1990 using VISSR Atmospheric Sounder (VAS) data is presented to illustrate further the magnitude of the errors that can be induced by lower level clouds (results for other days and other situations were found to be comparable). Ground observers in Omaha, Nebraska reported thin cirrus clouds with no other underlying clouds present. The ratio of the 13.9 to 13.3 micron satellite observed radiance differences between clear and cloudy FOVs (the left side of Equation (3)) is 0.36 on 25 October. This implies single layer cloud at 300 mb (solving the right side of Equation (3) for  $P_c$  as shown in Figure 7).

$R'$  has been modelled for a semi-transparent cloud at 300 mb with an underlying opaque cloud layer at 920, 780, 670, 500, and 400 mb (each configuration produces a different ratio in the left side of Equation (3),  $\text{Left}'$ ). The different  $\text{Left}'$  suggest different  $P_c'$  solutions as  $\text{Left}'$  is matched to  $\text{Right}$ , the right side of Equation (3). In the absence of any knowledge of a lower layer, the CO<sub>2</sub> algorithm integrates the right side of Equation (3) from the surface to an incorrect  $P_c'$ . Figure 7 shows  $\text{Right}$  as a function of  $P_c$  for the situation of 25 October. The errors in calculated cloud top pressure from the original 300 mb solution,  $P_c' - P_c$ , are shown as a function of height of the underlying opaque cloud layer in Figure 8 for 25 October.

In the two cloud layer situation, the position of the lower cloud layer affects the accuracy of the estimate of the height of the upper cloud layer. Opaque clouds in the lower troposphere near the surface underneath high cirrus have little affect on the cirrus  $P_c$ . Inspection of the spectral transmittance show that neither the 14.2 or the 13.9 micron channels are very sensitive to radiation from low in the troposphere, while the 13.3 micron channel senses only about half of the radiation from below 800 mb. Opaque clouds in the middle troposphere, between 400 and 800 mb, underneath high cirrus, cause the cirrus  $P_c$  to be overestimated (lower in the atmosphere) by up to 220 mb (this extreme occurs for the very thin high cirrus cloud with NE of .10). The decreases in  $R_b$  produce smaller ratios for the left side of Equation (3) which

in turn produces larger estimates of  $P_C$ . Opaque clouds high in the atmosphere, underneath higher cirrus, have little effect on the cirrus  $P_C$ , since the height of the lower opaque layer approaches the height of the semi-transparent upper cloud layer and the  $CO_2$  algorithm is going to estimate a height in between the two layers.

The errors in  $P_C$  were also examined for different emissivities of transmissive clouds (see Figure 9). This was modelled by varying the emissivity in Equation (8) and forming new ratios on the left side of Equation (3). The maximum cloud top pressure error of roughly 220 mb occurred in very thin cloud with emissivity of .10. The error in  $P_C$  reduced as the emissivity of the transmissive clouds increased. For a cloud with emissivity of 0.5, the maximum error in  $P_C$  is about 100 mb. For more dense clouds with emissivity of 0.9, the maximum error in  $P_C$  is less than 20 mb. The VAS data have shown a nearly uniform population of emissivity center around 0.5 (Wylie and Menzel, 1989), so one can conclude that the errors in the cloud top pressure caused by underlying clouds should average under 100 mb.

Multi-layer cloud situations (transmissive over opaque cloud) cause the height estimate of the upper cloud to be about 100 mb too low in the atmosphere on the average. The error in transmissive cloud height is largest when the underlying opaque layer is in the middle troposphere (400- 700 mb) and small to negligible when the opaque layer is near the surface or close to the transmissive layer. The error in effective emissivity increases as the opaque layer approaches the transmissive layer; when they are coincident, the effective emissivity is assumed to be one. In summary the cloud forcing from two layers is greater than the cloud forcing from one layer; assuming only one cloud layer when two exist causes the  $CO_2$  solution to put the cloud between the two layers with larger effective emissivity. This suggests that, overall, global cloud parameter estimates will be a little low in the atmosphere and with an effective emissivity a little too high.

Recent work has suggested that the radiative transfer equation in a two layer cloud situation can be solved from the  $CO_2$  radiance observations. The two layer cloud forcing can be written, where  $u$  is the upper cloud layer and  $l$  is the lower cloud layer,

$$R - R_{clr} = N_l E_l [1 - N_u E_u] \int_{P_s}^{P_{cl}} t \, dB + N_u E_u \int_{P_s}^{P_{cu}} t \, dB \quad (14)$$

Thus the two layer cloud forcing is characterized by four unknowns  $N_l E_l$ ,  $N_u E_u$ ,  $P_{cl}$ , and  $P_{cu}$ . Using the measured cloud forcing in the  $CO_2$  channels, a solution for upper and lower cloud pressures and effective cloud amounts is calculated. The algorithm selects spectrally close pairs of  $CO_2$  channels. For each pair of cloud forcing measurements, all possible  $N_l E_l$ ,  $N_u E_u$  are calculated as a function of  $P_{cl}$ ,  $P_{cu}$ . From this array of possible solutions, the selected solution best satisfies the radiative transfer equation for all spectral channels. Since four unknowns offer more degrees of freedom than two unknowns, the two layer solution is preferred over the one layer solution. Indication of when to use the two layer solution is sought through inspection of 4.0 micron versus 11.0 micron radiance scatter plots for the 5 x 5 km area (when radiances for the two spectral channels lie on two or more straight lines then the presence of two or more cloud layers is suggested).

Considerably more development work remains, before the two layer solution can be incorporated into the cloud parameter algorithm.

#### 3.1.3.a.4 Errors from an Inaccurate Estimate of the Surface Temperature

The CO<sub>2</sub> slicing algorithm has little sensitivity to surface temperature. The weighting functions for the CO<sub>2</sub> channels indicate that very little radiation from the earth surface is detected by the satellite radiometer in these spectral bands (14.2 and 13.9 micron observations don't even see the ground). Table 2 indicates the changes in cloud top pressure associated with changes in estimates of surface temperature inferred from a recalculation of the right side of Equation (3); the atmospheric profile of 25 October was used as an example (other situations yield similar results). When the surface temperature  $T_{\text{sfC}}$  is assumed to be 5 C too warm, the cloud top pressure  $P_{\text{C}}$  is 32 mb smaller (higher in the atmosphere); when  $T_{\text{sfC}}$  is assumed to be 5 C too cold,  $P_{\text{C}}$  is 26 mb larger (lower in the atmosphere). In other words, when the surface temperature guess doesn't track surface warming (cooling), then the cloud layer is calculated to be too low (high).

Table 2 also indicates an additional effect that arises when the surface temperature is assumed to be too cold. In the cloud screening process, some cloudy FOVs are inferred to be clear and  $R_{\text{clr}}$  is reduced for all spectral channels. Thus the left side of Equation (3) is reduced (when the less transmissive channel is in the numerator) and  $P_{\text{C}}$  goes even larger (lower in the atmosphere). The last four columns of Table 2 show the total error when 25% of the FOVs are incorrectly inferred to be clear for a guess that is 5 C too cold; when high clouds at 300 mb contaminate the clear radiance determination,  $P_{\text{C}}$  is 39 mb larger (representing an additional error of 13 mb), and when low clouds at 700 mb contaminate the clear radiance determination,  $P_{\text{C}}$  is 20 mb larger (representing an offsetting error of 6 mb).

The surface temperatures are monitored hourly with the SVCA conventional observations; errors of 5 C are unusual, but do occur in the western mountains where surface observations are too sparse to accurately represent the varying altitude conditions. We conclude that nominal diurnal changes in surface temperature will not affect the CO<sub>2</sub> slicing solutions of  $P_{\text{C}}$  by more than 50 mb.

Furthermore, fictitious reports of transmissive clouds cannot be produced by changes in the ground surface temperature, since two of the three channels do not see the ground. As witnessed in Table 2, effective emissivity estimates are relatively insensitive to surface temperature excursions of 5 C; Ne changes of about .10 are found.

Table 2. The changes in cloud top pressures ( $P_c$ ) and effective emissivities determined from the CO<sub>2</sub> slicing algorithm after changes to the estimated temperature profile and surface temperature (using the data of 25 October 1990)

Guess Error (guess - truth)		Cloud Top Pressure and Effective Emissivity Error							
		with additional errors from faulty cloud screening for contaminating clouds at							
met	sfc	atm			300mb		700mb		
cond	DTs	DT(p)	$DP_c$	DNe	$DP_c$	DNe	$DP_c$	DNe	
a	+5 K	0 K	-32 mb	-.09					
b	-5	0	+26	+.13	+39 mb	+.13	+20 mb	+.09	
d	0	+2	+10	+.03					
c	0	-2	-13	-.03					
ad	+5	+2	-20	-.07					
ac	+5	-2	-44	-.11					
bd	-5	+2	+37	+.19	+50	+.19	+31	+.14	
bc	-5	-2	+16	+.09	+28	+.09	+09	+.06	

Possible meteorological conditions that could cause indicated errors in the guess

- a indicates nocturnal cooling
- b indicates solar heating
- c indicates warm frontal passage
- d indicates cold frontal passage

### 3.1.3.a.5 Errors from an Inaccurate Estimate of the Temperature Profile

Table 2 also shows the changes in cloud top pressure associated with changes in estimates of temperature profile as well as surface temperature for the example of 25 October. When the entire temperature profile was changed by +/- 2 K in the calculation of the right side of Equation (3), the resulting changes were very small; about 10 mb for  $P_c$  and 0.03 for Ne. These errors are roughly equal to the lapse rate at the altitude of the cloud. When the surface temperature and the atmospheric temperature were adjusted by 5 and 2 K respectively, maximum errors of roughly 40 mb in  $P_c$  and .20 in Ne were found for the situation where the surface temperature was underestimated and the atmospheric temperature was overestimated (perhaps possible in nearly clear sky with strong solar heating producing a very large lapse rate in the lower atmosphere). Where the surface temperature and the atmospheric temperature were both underestimated (possible in a warm frontal passage), the cloud was estimated to be too low in the atmosphere by 20 mb in  $P_c$  and too opaque by .10 in Ne.

Experiments were also conducted simulating errors localized to only one level of the temperature profile. The results (not shown) were modified minimally. Little sensitivity is apparent for temperature errors low in the

atmosphere ( $P_C > 700$ ), as expected from inspecting the transmittances of the MODIS CO<sub>2</sub> channels. An error of 2 C for a level between 700 and 300 mb can produce a shift of up to 30 mb in the cloud top pressure. This should be viewed in conjunction with the lapse rate of 5 C per 50 mb for the example of 25 October. Here and in other situations inspected, the errors in the CO<sub>2</sub> slicing cloud top pressure estimate,  $DP_C$ , caused by sounding errors,  $DT$ , in layers where the CO<sub>2</sub> spectral channels have sensitivity, are found to be roughly proportional to the lapse rate at the level of the cloud,  $L$ ; this can be expressed as  $DP_C = DT/L$ .

#### 3.1.3.a.6 Errors Associated with Instrument Noise

The VAS radiometer is accurate to better than 1 mW/m<sup>2</sup>/ster/cm<sub>1</sub>. This corresponds to less than 1 K in the CO<sub>2</sub> channels for temperatures ranging from 220 to 320 K. Noise affects the ability of the VAS to detect thin cirrus. Noise of 1 K implies that effective cloud emissivities of less than 10% cannot be resolved for high clouds (using  $DNE = DR/(R - R_{clr})$ ). In our earlier work of 1989, it was found that about half of the very thin clouds with NE less than .10 were classified incorrectly as low opaque cloud observations (this represented about 5% of all observations); it was also found that about half of these very thin clouds were correctly classified by the CO<sub>2</sub> slicing algorithm.

The CO<sub>2</sub> slicing technique cannot measure the properties of clouds where the contrast of radiation from cloud free and cloud obscured observations is too small for reliable discrimination in the satellite CO<sub>2</sub> spectral radiances (when radiance differences are less than .5 mW/m<sup>2</sup>/ster/cm<sup>-1</sup> cloud properties are not calculated). This occurs for very thin cirrus (as discussed in the previous paragraph) and for some low clouds below 700 mb. Clouds below 700 mb were assumed to have an effective emissivity of one, thus preventing the interpretation of low broken cloud as cirrus. Occasionally, low clouds were also reported in situations of clear sky with tropospheric temperature inversions; this created problems in early morning statistics during the winter months.

When noise is introduced in one channel of the CO<sub>2</sub> radiance ratio, the left side of Equation (3) changes. Using the example of 25 October once again, Figure 7 shows the noise induced changes in the ratio. The extremes produce a  $P_C$  that is 50 mb lower or make it impossible to have a solution in the atmosphere. This example is representative of further noise investigations in the CO<sub>2</sub> slicing algorithm; the effect of sensor noise is typically less than 50 mb.

#### 3.1.3.a.7 Conclusions of the Cloud Top Pressure and Emissivity Error Studies

(i) Errors associated with the assumption of constant emissivity for the CO<sub>2</sub> channels are negligible.

(ii) The CO<sub>2</sub> slicing algorithm determines the height of the radiative center of the cloud; for optically thick clouds this is near the cloud top while for optically thin clouds it is near the cloud middle.

(iii) Multi-layer cloud situations where an opaque cloud underlies a transmissive cloud cause errors in the height of the transmissive cloud of



about 100 mb for most cases (the cloud is determined to be too low in the atmosphere). The error in transmissive cloud height is largest when the underlying opaque layer is in the middle troposphere (400- 700 mb) and small to negligible when the opaque layer is near the surface or close to the transmissive layer.

(iv) When the surface temperature guess doesn't track surface warming (cooling), then the cloud layer is calculated to be too low (high). Nominal diurnal changes in the ground temperature are typically tracked to better than 5 C in the CO<sub>2</sub> slicing algorithm, so that they have little effect on the ability to detect transmissive clouds or to determine their heights.

(v) The CO<sub>2</sub> solution is largely insensitive to errors in the temperature sounding in the lower troposphere. There are often compensating effects in the integration of the atmospheric column. The errors in the CO<sub>2</sub> slicing cloud top pressure estimate caused by sounding errors in layers where the CO<sub>2</sub> spectral channels have sensitivity are roughly proportional to the lapse rate at the level of the cloud.

(vi) Instrument noise causes the CO<sub>2</sub> slicing algorithm to miss roughly half of the thin cirrus with effective emissivity less than .10; this represents about 5% of all observations.

#### 3.1.3.b Error Estimates of Cloud Phase Algorithm

No quantitative evaluations of cloud phase error estimates have been made to date, due to the lack of coincident observations. Confirmation of cloud phase has been made primarily through inspection of collocated visible MAS data, comparison with a visible channel technique (Strabala et al. 1994), and comparison with lidar cloud height determinations (Ackerman et al. 1990). Error estimates will become available as observations become available, however certain sources of error are known to exist.

##### 3.1.3.b.1 Errors Due To Clear Sky Thresholding

Clear sky determination is based on a single threshold in both the 8 minus 11 and 11 minus 12 micron brightness temperature differences. This will not be effective for a global data set in which total water vapor, and hence absorption, will vary considerably. A new approach which varies the thresholds according to the amount of precipitable water determined in a column of atmosphere, is being developed. This method of clear sky determination will initially be used in place of the MODIS cloud mask to determine its effectiveness, and because the clear sky evaluations and precipitable water amounts determine the divergence from unity of the ice and water cloud slopes (see Figures 4-6).

##### 3.1.3.b.2 Errors Due to Mixed Phase Cloud Scenes

Errors in cloud phase determination will also take place due to scatter diagram thresholding of mixed cloud phase in the 8 minus 11 versus 11 minus 12 micron brightness temperature differencing. Some overlap will occur between pure ice/water cloud and the mixed phase cloud scenes due to the variance in scatter around the unity slope. The extent of the error will depend on the

amount of mixed phase versus pure ice/water scenes in each 2 degree by 2 degree array of scenes.

#### 3.1.3.b.3 Errors Due to Non-uniform Surface Emissivities

The current version of the tri-spectral technique assumes a uniform surface emissivity for all three channels. This is certainly not the case for many different ground surface types, including bare soils and deserts. Studies will be undertaken with MAS data over varying background scenes to determine if any surface or vegetation types need to be avoided.

#### 3.1.3.b.4 Errors Due to Instrument Noise

An investigation into the effects of MAS pixel averaging on brightness temperature differencing was conducted, with distinct cloud signals becoming apparent after averaging over a 5 x 5 box. This lowers the NEDT values for the 8, 11 and 12 micron channels to .13, .09 and .15 K respectively. The MODIS NEDT specifications of these infrared bands at 300 K is .05 K, suggesting that the noise will be within the limits for cloud phase delineation.

### 3.2 Practical Considerations

#### 3.2.1.a Radiance Biases and Numerical Considerations of Cloud Top Properties Algorithm

The MODIS measured radiances will have biases with respect to the forward calculated radiances using model estimates of the temperature and moisture profile for a given field of view. There are several possible causes for this bias: these include calibration errors, spectral response uncertainty, undetected cloud in the FOV, and model uncertainty. Solution of Equation (3) uses measured and calculated cloud forcing (clear minus cloudy FOV radiances) and thus requires that this bias be minimized. Techniques developed at the European Centre for Medium range Weather Forecast to characterize the HIRS radiance bias with respect to the ECMWF model (Eyre, 1992) will be employed in the MODIS cloud algorithm.

Even when the radiance bias has been reduced, the measured and the calculated cloud forcing ratios in Equation (3) do not always converge within the allowable pressure bounds (between the tropopause and the top of the inversion layer or the surface). Solutions are not accepted if the minimum of measured minus calculated in Equation (3) is found at the boundary, even though there may be a good meteorological reason to accept these values. In these cases the opaque cloud solution from the window channel is used.

Evaluation of the integrals in the right side of Equation (3) are performed at 50 mb increments. As the instrument noise is reduced through averaging the data to 5 kilometer areas, it may be appropriate to reduce the increment to 25 mb.

When the slope in Figure 7 increases, instrument noise causes more error in the cloud top pressure determination. It has been found that mid-latitudes have greater slopes than the tropics, thus cloud top pressures in the tropics might be slightly less error prone.



### 3.2.1.b Numerical Considerations of Cloud Phase Algorithm

The simplicity of the cloud phase algorithm, which relies on data averaging, determining radiance standard deviation, and simple subtractions, make it very numerically stable. This simple algorithm will evolve to include dynamic brightness temperature difference thresholds related to synoptic conditions, and may employ an MLE technique. This updated version will be available upon software delivery in second quarter 1994. Simple post launch adjustments may be made initially to fine tune the thresholds, due to band differences between the MAS and MODIS instruments.

### 3.2.2.a Programming Considerations of Cloud Top Properties Algorithm

Processing will be accomplished globally at 5 km resolution. It still remains to be determined whether the data will be averaged (to reduce instrument single sample noise) or sampled (to maintain the cloud census at 1 km FOV). Spectral channel registration must occur, so that FOVs can be collocated with ancillary data.

The CO<sub>2</sub> slicing algorithm has been used for the past six years on VAS data over North America and for the past four years on global HIRS data. It is a robust algorithm. The census of cirrus clouds derived from both of these efforts has been published in refereed literature.

The HIRS data has been processed on the IBM 4381 (Man computer Interactive Data Access System - McIDAS) at the Space Science and Engineering Center. The data have been sampled to include only data from every third FOV on every third line (roughly 50 km resolution) with zenith angle less than 10 degrees. With two satellites, about one half of the Earth is sampled each day. The CPU time required daily is 36 minutes. Thus to produce global cloud parameter determinations with the CO<sub>2</sub> slicing algorithm using MODIS data at 5 km resolution should require about 200 times more IBM 4381 CPU time (7200 minutes).

### 3.2.2.b Programming Considerations for Cloud Phase Algorithm

Processing will be accomplished globally at 5 km resolution. The brightness temperatures will be averaged (to make it compatible with the cloud top properties processing) and cloud parameters will be determined from a scatter diagram of 2 x 2 degree latitude/longitude box. Spectral channel registration must occur before, so that FOVs can be collocated with ancillary data.

The CPU required to currently produce cloud phase is 4 minutes on an IBM 4381 computer, for each three channel 1380 10 x 10 averaged pixel area. For a global 5 x 5 km averaged pixel area, data averaging will take one quarter the CPU time (25 as opposed to 100 scenes). There will be 16200 2 degree latitude x 2 degree longitude boxes consisting of approximately 1600 5 km x 5 km averaged areas (this value will be much smaller near the poles). One half global coverage daily reduces the total to 8100 boxes. At one quarter the processing time per box, this results in approximate CPU usage of 8000 minutes per day.

### 3.2.3.a Calibration Validation of Cloud Top Properties Algorithm

The CO<sub>2</sub> slicing algorithm uses calibrated radiances; bias adjustment with respect to the NMC forward calculations of clear sky radiances will be made. Also the spectral cloud forcing is used in the algorithm (clear minus cloudy fov radiances). These two considerations mitigate the algorithm dependence on extremely accurate calibration, although it is highly desirable.

### 3.2.3.b Calibration Validation for Cloud Phase Algorithm

The cloud phase algorithm uses calibrated radiances which will be converted into brightness temperatures, and averaged over a 5 x 5 degree box. The use of temperature differences between the 8, 11, and 12 micron channels averaging also stresses the algorithm dependence on very accurate relative calibration between channels.

### 3.2.4.a Quality Control of Cloud Top Properties Algorithm

As indicated in section 3.1.3.a., the accuracy of the cloud top pressures have been found to be 50 mb root mean square with respect to radiosonde, stereo, and lidar estimates; the effective emissivity determinations have been found to be correlate within 20% root mean square of lidar visible estimates of optical thickness.

Quality control within the software checks for cloud forcing greater than the instrument noise and cloud top pressure within the atmospheric layer where temperature and pressure enjoy a one to one relationship. Additionally, cloud top pressures will be stratified as a function of satellite viewing angle to make sure that the atmospheric transmittance corrections for viewing angle are not introducing a bias.

Beyond these simple tests, quality control is accomplished by manual inspection of the data and comparison to other sources of cloud information. MODIS cloud top pressures and effective emissivities will be compared to those determined from the NOAA HIRS and the GOES sounder. Additional data from field experiments using the MODIS Airborne Simulator on the ER2 will assist with quality assessment of the MODIS cloud parameter determinations

### 3.2.4.b Quality Control of Cloud Phase Algorithm

Quality control will also include comparison with cloud phase determination using visible channel ratios (King, 1992) during daylight hours. The remainder of the quality control will take place by manual inspection.

### 3.2.5 Exception Handling

If the required radiance data is not available, then the algorithm will record the cloud products missing for that 5 km area.

### 3.2.6.a Data Dependencies of Cloud Top Properties Algorithm

The CO<sub>2</sub> slicing algorithm needs calibrated, navigated, coregistered one km FOV radiances from channels 29 (8.6 micron for moisture correction), 31 (11.03 micron infrared window), 32 (12.02 micron for moisture correction), 33-

36 (13.335, 13.635, 13.935, and 14.235 microns CO<sub>2</sub> absorption band channels). Visible reflectances at 250 meter resolution from channel 1 (.66 microns) and at one km resolution from channel 26 (1.375 microns) will be also used for cloud screening. Navigation implies knowledge of the surface terrain (whether land or sea). The MODIS viewing angle for a given FOV must be known. The cloud mask from visible and infrared radiance considerations will be used as a initial test for cloud cover within a given one km FOV. The NMC global model estimates of surface temperature and pressure as well as profiles of temperature and moisture will be initially used in the calculation of the cloud forcing as a function of pressure and effective emissivity (in Equation (3)); as the AIRS/AMSU profiles become available, they will be used also. Table 3 summarizes the input data dependencies.

There has been some consideration for using the short wavelength CO<sub>2</sub> spectral bands 22 through 25 in parallel with the long wavelength CO<sub>2</sub> bands in a composite CO<sub>2</sub> slicing algorithm. The shortwave CO<sub>2</sub> algorithm has problems with reflected solar contributions during daylight hours, but is useful additional information at night. Current plans do not include these bands, but future versions of the software might.

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Table 3. MODIS Cloud Parameter Input Data Dependencies

MODIS data channels	1, 26, 29, 31-36
Navigation	lat, lon, land, sea
MODIS viewing angle	lin, ele, ang
Cloud mask	yes, no, type
Surface data	temp, press, topography, vegetation type
model profiles	temp (20 levels), moisture (15 levels)

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### 3.2.6.a Data Dependencies of Cloud Phase Algorithm

The tri-spectral cloud phase algorithm needs calibrated, navigated, coregistered one km FOV radiances (for FOV uniformity screening and conversion to brightness temperatures) from channels 29 (8.6 micron), 31 (11.03 micron) and 32 (12.02 micron). The MODIS viewing angle for a given FOV must be known. The NMC global model estimates of surface temperature and the Reynolds blended global Sea Surface Temperatures will be used to eventually develop clear brightness temperature difference thresholds for each 5 km x 5 km box. As the algorithm develops, a global vegetation index will be needed to adjust thresholds according to surface emissivities. Table 4 is a summary of the input data dependencies.

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Table 4. MODIS Cloud Phase Input Data Dependencies

MODIS data channels	29, 31, 32
Navigation	lat, lon, land, sea
MODIS viewing angle	lin, ele, ang
Surface data	NMC surface temp, SST, vegetation type

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### 3.2.7 Output Product of Cloud Top Properties and Cloud Phase Algorithm

The output from these algorithms will eventually be merged. However, in the near term the cloud top properties algorithm and the cloud phase algorithm are being developed separately, so the output files are also listed separately.

#### 3.2.7.a Output Product of Cloud Top Properties Algorithm

The output file for each 5 km area (when cloud is present) is summarized in Table 5.

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Table 5. Cloud Parameter Output File Contents

word	content
1	time and day of observation
2	location latitude longitude
3	location line element
4	satellite zenith angle
5	solar zenith angle
6-7	solar reflectance of channels 1 and 26
8-17	brightness temperature of channels 27 through 36
18	flag for land or sea
19	surface temperature estimate
20	surface pressure estimate
21	tropopause height estimate
22-28	spectral cloud forcing for channels 29, 31 through 36
29	method of cloud height determination (CO <sub>2</sub> slicing or IR window)
30	cloud effective emissivity
31	cloud top pressure
32	cloud top temperature
33-37	cloud height from the five ratios
38	cloud height from the IR window

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### 3.2.7.b Cloud Phase Output Products

The cloud phase output file for each 5 km area is summarized in Table 6.

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Table 6. Cloud Phase Output File Contents

word	content
1	time and day of observation
2	location latitude longitude
3	location line element
4	satellite zenith angle
5	solar zenith angle
6-7	image line and element number
8-10	brightness temperature of channels 29, 31 and 32
11-13	radiance variance for channels 29, 31 and 32
14	flag for land or sea
15	flag for clear versus cloud
16	flag for vegetation type
17	surface temperature
18	channel 29 minus channel 31 brightness temperature difference
19	channel 31 minus channel 32 brightness temperature difference
20	cloud phase code

As further versions progress, the computed total column precipitable water, and clear/cloud thresholds which correspond to these values will also be output.

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### 3.3 References for sections 2 and 3.

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#### 4.0.a Assumptions of Cloud Top Properties Algorithm

The data is assumed to be calibrated (within the instrument noise), navigated (within one FOV), and coregistered (within two tenths of a FOV). The algorithm assumes the presence of only one cloud layer of infinitesimal thickness; adjustments for the presence of multiple cloud layers are under investigation. The cloud need not cover the entire FOV. Spectral cloud forcing must be greater than the instrument noise.

#### 4.0.b Assumptions of Cloud Phase Algorithm

Assumptions are discussed in the estimate of error section 3.1.3.b.

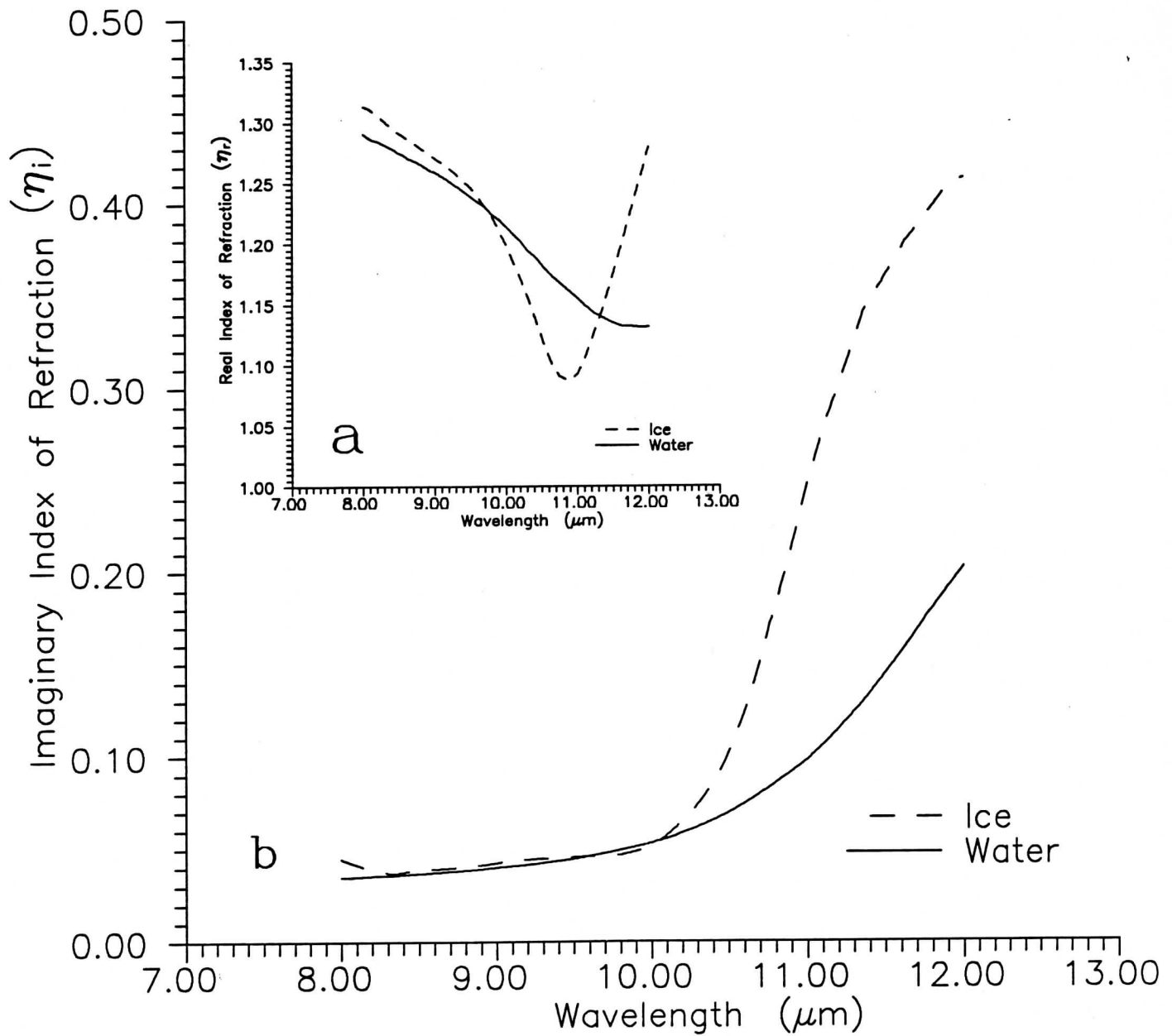


Figure 1: Indices of refraction of ice and water across the atmospheric window, (a) real portion, (b) imaginary portion.



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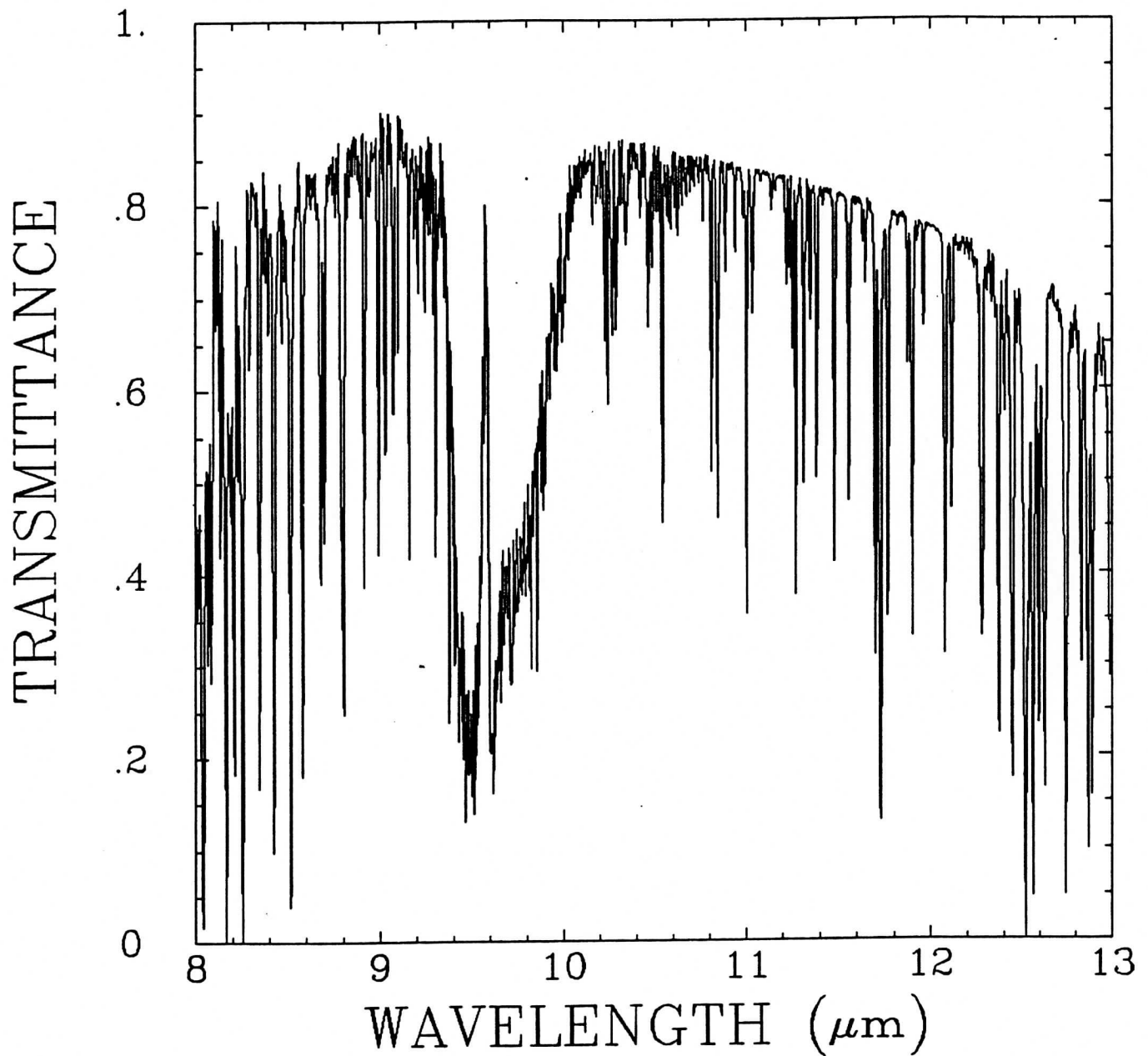


Figure 2. HIS total transmittance spectra for a standard atmosphere across the 8-13 $\mu\text{m}$  spectral region.

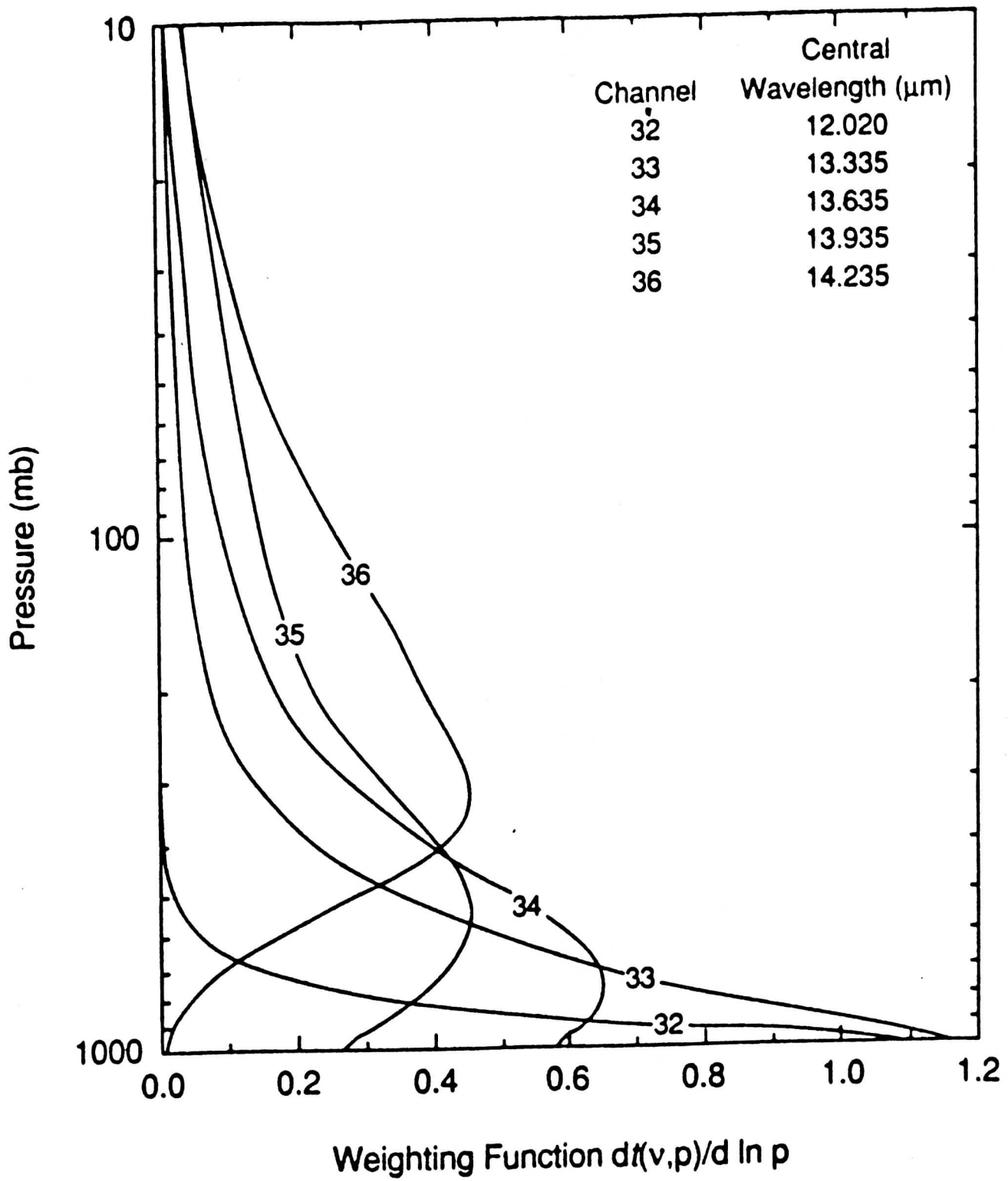


Figure 3.

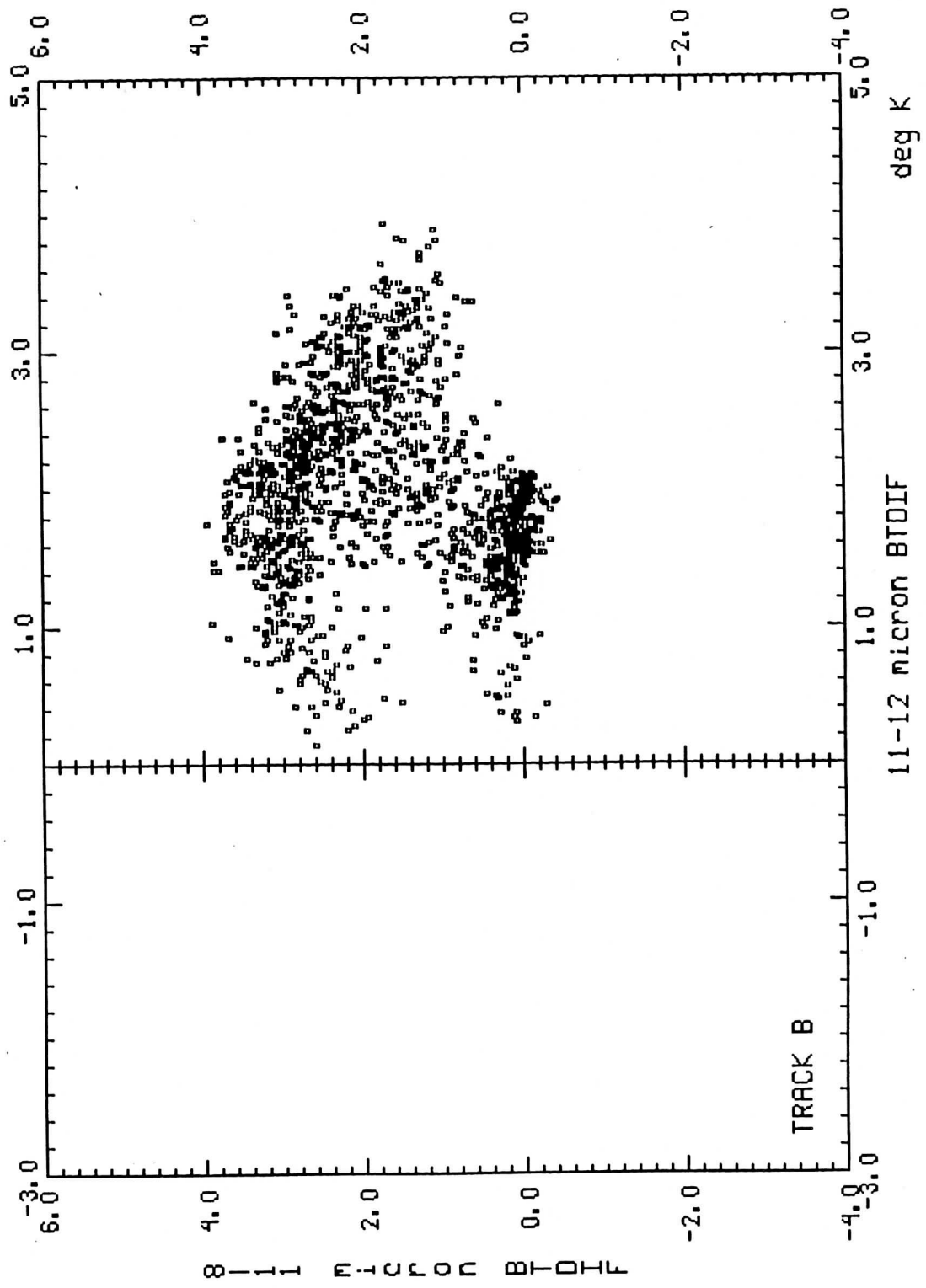


Figure 4. Scatter diagram of averaged brightness temperature differences 8-11 $\mu$ m versus 11-12 $\mu$ m of the multi-phase cloud scene of Figure 5 taken from the 5 December 1991 15:38 UTC MAS flight track data set (Track B).

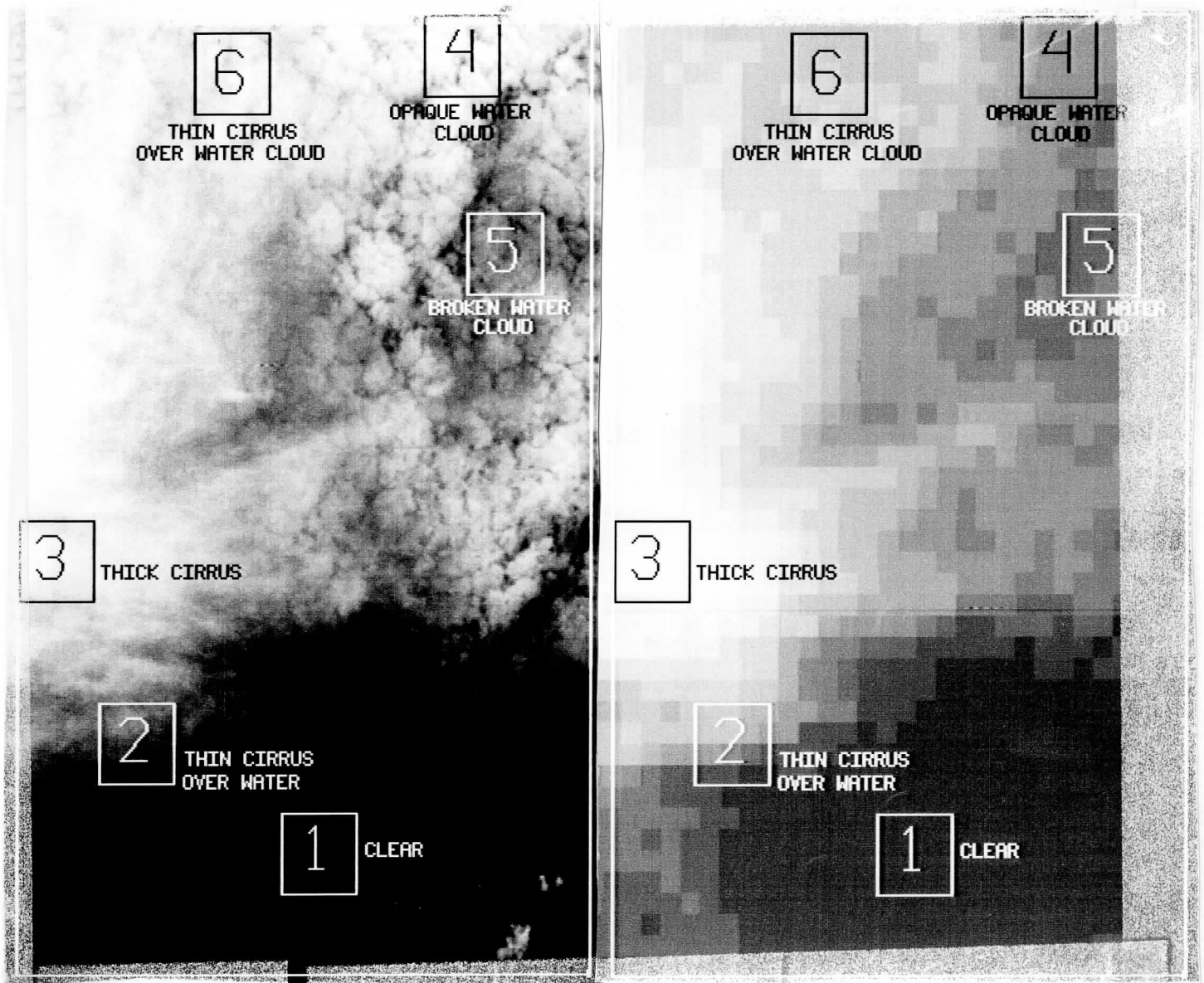


Figure 5. MAS mixed cloud scene 50m resolution visible (left panel) and 10 x 10 pixel averaged 11 $\mu$ m (right panel) images from a portion of the 5 December 1991 data at 15:38 UTC (Track B). Boxes represent differing cloud regimes used in the brightness temperature scatter diagram of Figure 6.

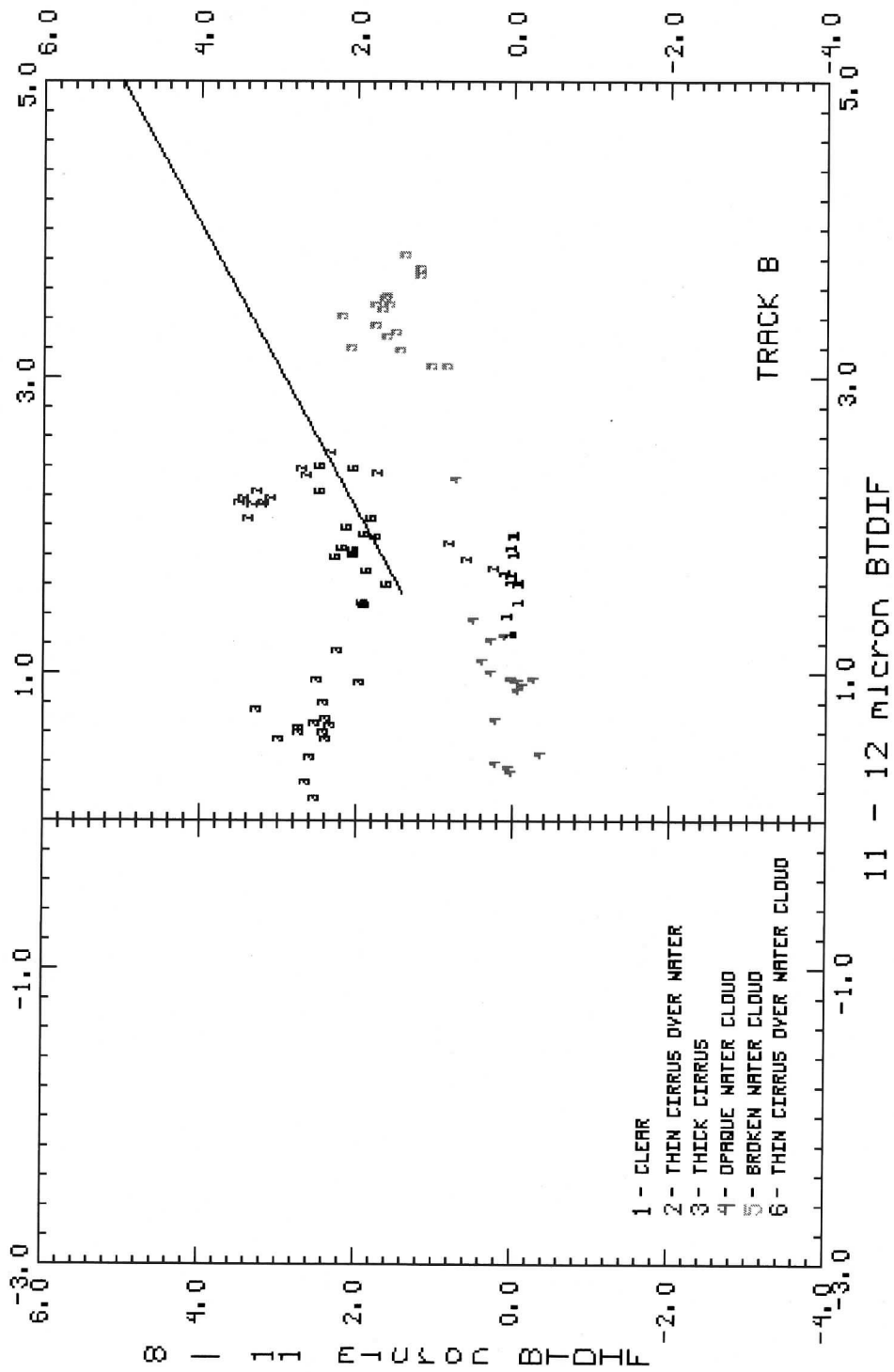


Figure 6. Same as Figure 4, except limited to the cloud scenes identified in Figure 5. Also shown for reference is a line with a slope of one.

25 OCT 90

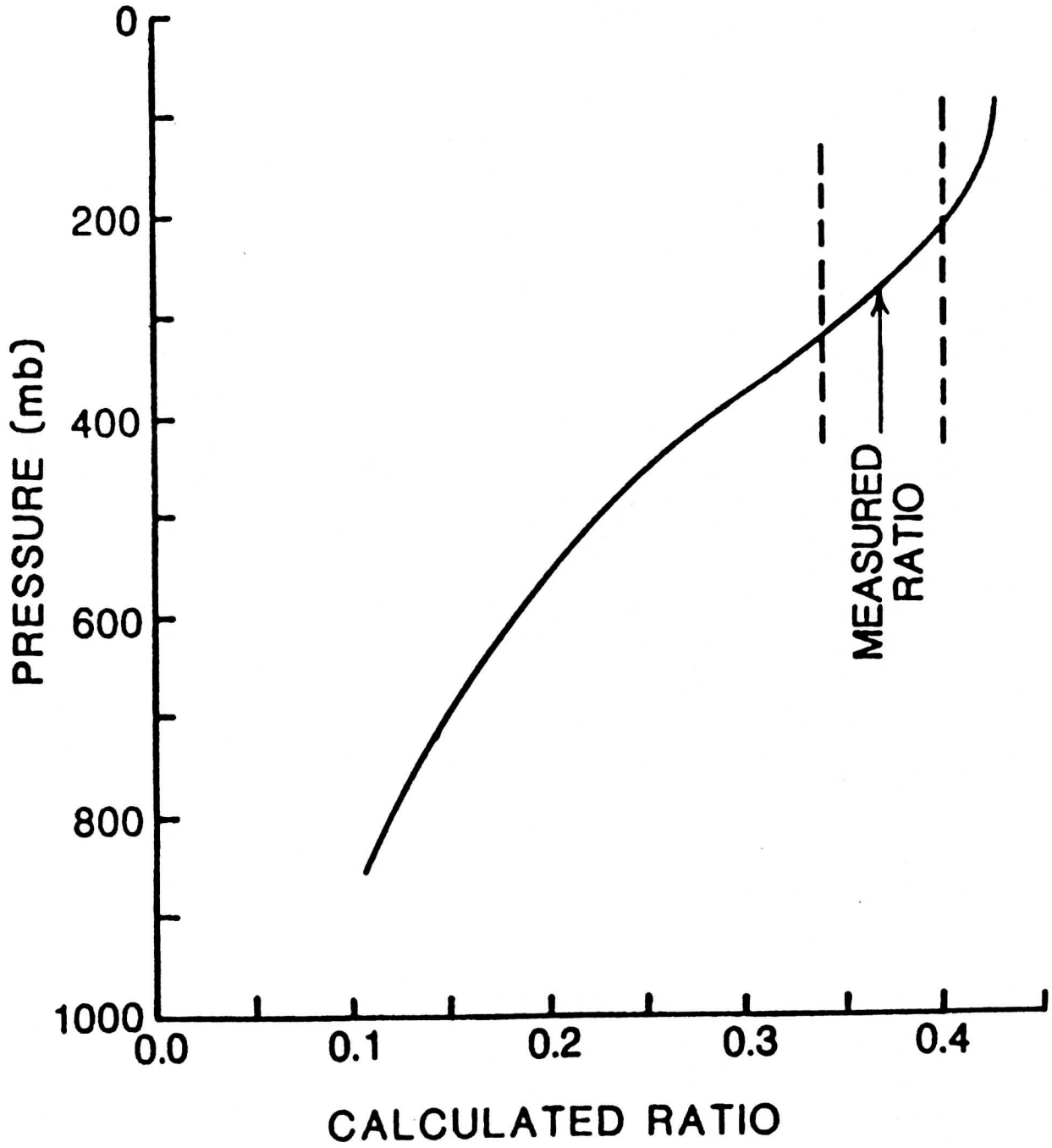
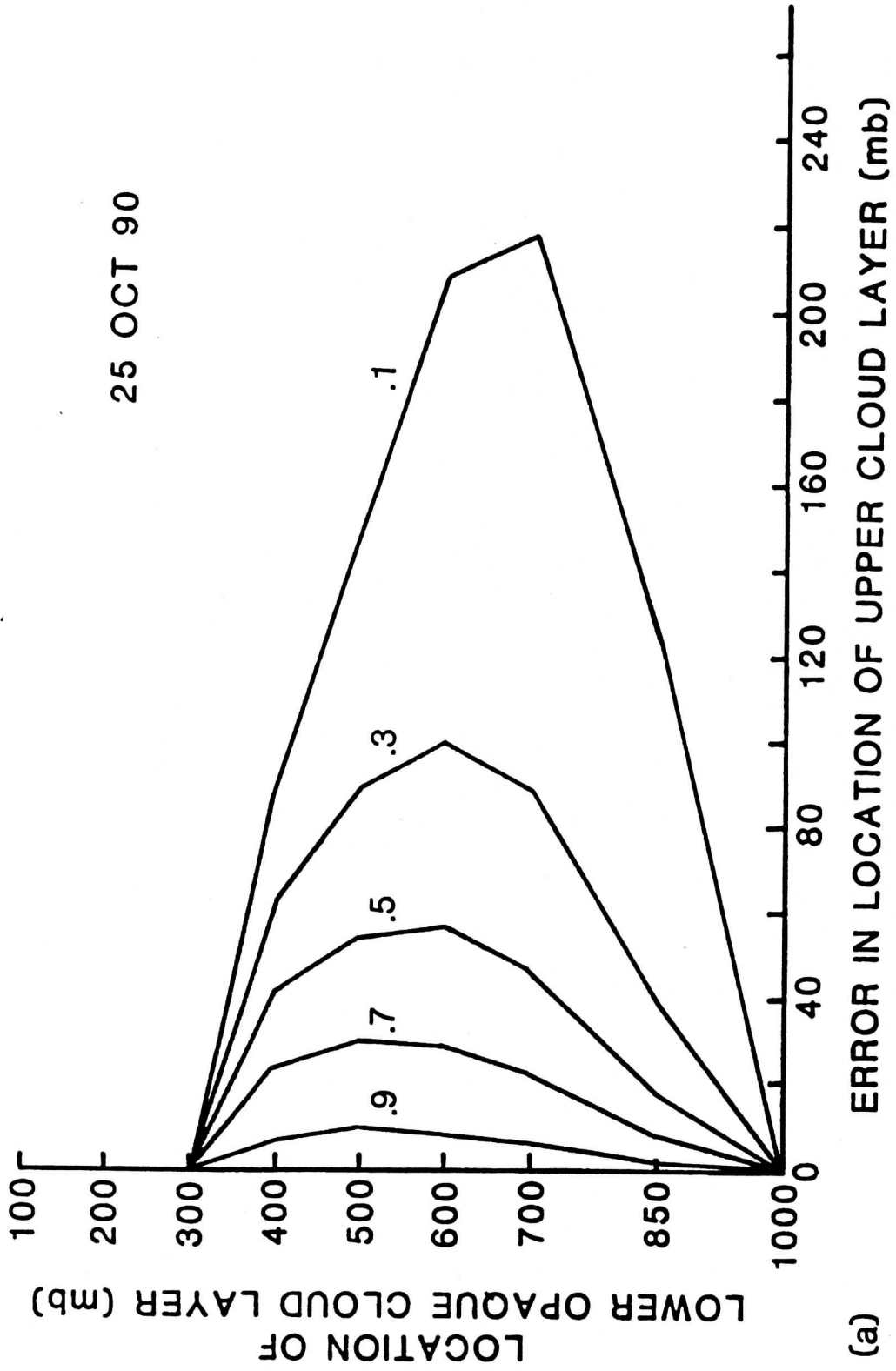


Figure 7.

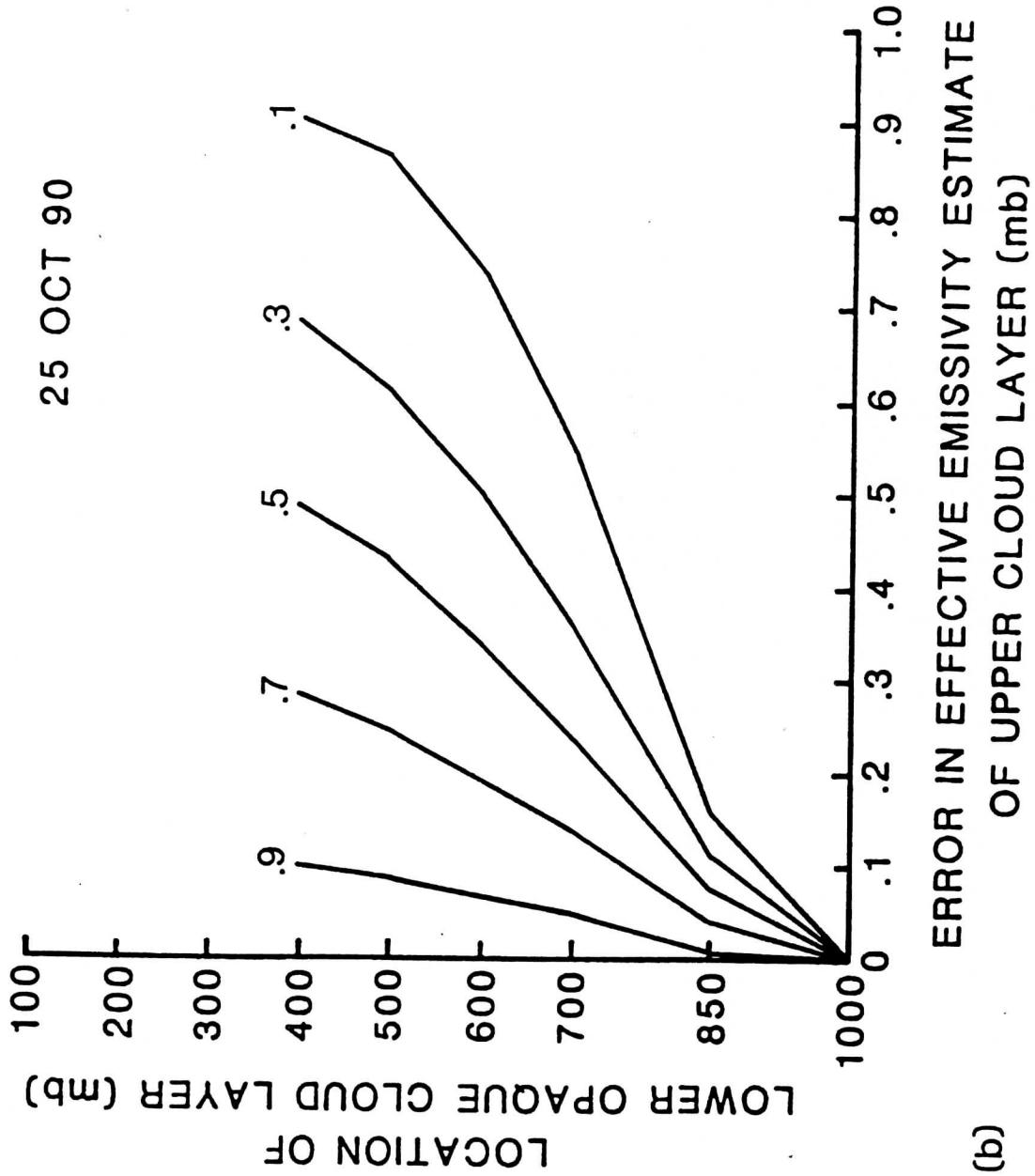
25 OCT 90



(a)

Figure 8.

25 OCT 90



(b)

Figure 9.